



**Pangolin 1.0,
a parallel
conservative
transport model**

A. Praga et al.

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Pangolin v1.0, a conservative 2-D transport model for large scale parallel calculation

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Abstract

To exploit the possibilities of parallel computers, we designed a large-scale bidimensional atmospheric transport model named Pangolin. As the basis for a future chemistry-transport model, a finite-volume approach was chosen both for mass preservation and to ease parallelization. To overcome the pole restriction on time-steps for a regular latitude-longitude grid, Pangolin uses a quasi-area-preserving reduced latitude-longitude grid. The features of the regular grid are exploited to improve parallel performances and a custom domain decomposition algorithm is presented. To assess the validity of the transport scheme, its results are compared with state-of-the-art models on analytical test cases. Finally, parallel performances are shown in terms of strong scaling and confirm the efficient scalability up to a few hundred of cores.

1 Introduction

Global three-dimensional chemistry-transport models (hereafter referred as CTMs) play an important role in monitoring and predicting the composition of the atmosphere (e.g. Chipperfield, 2006; Teyssèdre et al., 2007; Huijnen et al., 2010). Those models include large-scale transport, emissions and chemical transformations of trace species and sub-scale grid processes like convection and deposition. In CTMs, advection by large-scale winds is a key process that must be handled by numerical transport algorithms. For these algorithms, mass conservation for the considered species, monotonicity and numerical accuracy are especially important for long simulations where accumulation of errors and bias must be avoided.

In this paper, we present a conservative advection model on the sphere, which is intended to form the basic framework for a future CTM. The adopted scheme is based on a flux-form (Eulerian) tracer transport algorithm on a reduced latitude-longitude grid. A finite-volume approach was chosen as it provides an easy way to ensure mass

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preservation. Furthermore, parallelizing the model is then reduced to a domain decomposition problem.

The specificity of our model, named Pangolin¹, lies in the grid definition where the number of cells on a latitude circle is progressively decreased towards the pole in order to obtain a grid which preserves approximately the cell areas at mid- and high-latitudes. This avoids the so-called “pole problem” arising from the convergence of the meridians that severely limits the size of the time-steps for Eulerian models. Several approaches have been adopted in previous studies to cope with this issue. Finite-volume schemes on latitude-longitude grids often aggregate latitudinal fluxes near the poles (e.g. Hourdin and Armengaud, 1999) or double successively the grid size at high-latitudes (e.g. Belikov et al., 2011).

Alternatively, quasi-uniform spherical grids have been developed, such as cubed-sphere², composite mesh – Yin-Yang – or icosahedral grids³. A review of the different grids can be found in Staniforth and Thuburn (2012) or Williamson (2007). However, those approaches lose the latitudinal regularity arising from the rotation of the Earth. Furthermore, they require specific treatments at the singularities of the adopted polygons, which may also induce resolution clustering near these points. On the plus side, they allow the implementation of more accurate algorithms than the ones on reduced latitude-longitude grids. This last point is especially important for weather and climate models that solve the non-linear momentum equation but is less stringent for the two-dimensional (2-D) linear transport of trace species on the sphere.

To construct the reduced grid, one difficulty is to define a structure which avoids treating the poles as special cases, as that can impact the precision and properties of the advection algorithm. Thus we have chosen to adopt a semi-structured approach. The grid is not regular as the number of cells varies with the latitude, but the coordinates of

¹Parallel implementation of a large scale three-dimensional chemistry-transport scheme

²Each face uses Cartesian coordinates and is projected gnomonically or conformally on the sphere.

³An icosahedron is subdivided until the desired resolution and projected on the sphere.

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cell interfaces can be computed analytically. We thus avoid storing a list of neighbours as an irregular unstructured grid would normally require, hence decreasing memory costs. This was done to anticipate future parallel architectures, which may have less memory capacity than current systems.

5 Our goal is to use an adequate algorithm exploiting the grid features to achieve efficiency and scalability on massively parallel architectures. Fine control over parallelization was obtained using the Message Passing Interface (MPI) library. In that context, the advection scheme must be chosen as to balance its accuracy vs. the size of parallel communications. Furthermore, grid properties were carefully studied to improve the
10 parallel version. Especially, a custom domain decomposition consistent with our grid was designed.

The present paper is organized as follows. Section 2 recalls the basic equations and numerical methods used to solve the advection of the chemical species. In Sect. 3, results from standard test cases for advection of tracer on the sphere are reported.
15 Those cases were chosen from the test case suite proposed by Lauritzen et al. (2012). Section 4 gives details on the model implementation on parallel architectures and the results of scalability tests. In Sect. 5, we summarize the results obtained and discuss the possible extension of our method.

2 Numerical scheme

2.1 Finite-volume formulation

Our model is based on a finite-volume method to integrate the tracer advection equation. This is performed on a bi-dimensional discrete grid on the sphere, which is described in more details in Sect. 2.2. In each grid cell, the tracer concentration changes according to the divergence of the fluxes at the cell boundaries. This comes from the
25 flux-form of the continuity and tracer conservation equations:

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$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{V}) = 0, \quad (1)$$

$$\frac{\partial \rho q}{\partial t} + \nabla \cdot (\rho q \mathbf{V}) = 0, \quad (2)$$

where ρ is the air density, q the tracer mixing ratio and \mathbf{V} the winds vector field. Equations (1) and (2) are first integrated over a cell area \mathcal{A} . Noting $\partial \mathcal{A}$ the cell boundary and \mathbf{n} the local normal, the divergence theorem yields:

$$\frac{\partial m}{\partial t} = \frac{\partial}{\partial t} \int_{\mathcal{A}} \rho = \int_{\partial \mathcal{A}} (\rho \mathbf{V} \cdot \mathbf{n} \, dS), \quad (3)$$

$$\frac{\partial m q}{\partial t} = \frac{\partial}{\partial t} \int_{\mathcal{A}} \rho q = \int_{\partial \mathcal{A}} (\rho q \mathbf{V} \cdot \mathbf{n} \, dS), \quad (4)$$

where m is the total air mass in a cell and $m q$ is the total tracer mass in a cell. The right-hand side of Eqs. (3) and (4) can be seen as the integral of all the fluxes across the cell boundaries. This formulation gives a conservative scheme when the same fluxes are used for upstream and downstream adjacent cells.

The above equations are then integrated in time during a time-step:

$$[m]^{n+1} = [m]^n + \int_{t_n}^{t_{n+1}} \left(\int_{\partial \mathcal{A}} \rho \mathbf{V} \cdot \mathbf{n} \, dS \right) dt, \quad (5)$$

$$[m q]^{n+1} = [m q]^n + \int_{t_n}^{t_{n+1}} \left(\int_{\partial \mathcal{A}} \rho q \mathbf{V} \cdot \mathbf{n} \, dS \right) dt. \quad (6)$$

Equation (5) can be omitted for non-divergent flows since the divergence of the mass fluxes is null and the mass inside the cells are constant: $[m]^{n+1} = [m]^n$. In this work

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To ensure monotonicity of the solution and to prevent numerical oscillations, van Leer introduced a slope limiter. The idea is to limit the slope value within a given cell such as the tracer value in that cell does not exceed the mean value of the adjacent cells. This is more restrictive than limiting the fluxes to ensure that the tracer values remain between the maximum-minimum values of the adjacent cells but is easier to implement. The slope is given by:

$$(\delta q)_i = \min \left(\frac{1}{2}|q_{i+1} - q_{i-1}|, 2|q_{i+1} - q_i|, 2|q_i - q_{i-1}| \right) \times \text{sign}(q_{i+1} - q_i), \quad (8)$$

if q_i lies in between q_{i-1} and q_{i+1} , and $(\delta q)_i = 0$ otherwise. As discussed by Hourdin and Armengaud (1999), the slope limiter efficiently damps the numerical oscillations but introduces more diffusion of the numerical solutions. For the test cases reported in this study, the slope limiter appears to have little impact on the accuracy of the numerical solutions.

2.2 Grid

The grid used in Pangolin is completely defined by the number of cells at the north pole and the number of latitudes n_{lat} on an hemisphere. The Southern Hemisphere is simply constructed in the same way as the Northern Hemisphere. To find the number of cells at the pole, we can write the equality between cell areas at the pole and at the Equator. If we consider squared cells at the Equator, like the ones on a regular latitude-longitude grid, and small latitudinal spacing, the number of cells is approximately π . Thus we set the number of cells at the poles to 3.

At a given latitude, all cells have the same area. We can then compute the number of cells for all latitudes. Latitudinal and longitudinal spacings are no longer supposed identical, for maximum flexibility. Let us consider the area of cell (i, j) , noted \mathcal{A}_i as it does not depends on j . Let us note ϕ_i the colatitude and λ_{ij} the position of the south and east cell borders. As we suppose the cell spacings constant, we can write $\phi_i = i\Delta\phi_i$ and $\lambda_{ij} = j\Delta\lambda_j$. The area is defined on $\Omega_{ij} = [\lambda_j, \lambda_{j+1}] \times [\phi_{i-1}, \phi_i]$, so in spherical

coordinates, we have:

$$\begin{aligned} \mathcal{A}_i &= \iint_{\Omega_{ij}} r^2 \sin \phi d\lambda d\phi \\ &= r^2 \Delta\lambda_i (\cos(\phi_{i-1}) - \cos(\phi_{i-1} + \Delta\phi_i)). \end{aligned} \quad (9)$$

5 Areas are preserved so $\mathcal{A}_i = \mathcal{A}_1$:

$$\Delta\lambda_i = \Delta\lambda_1 \frac{1 - \cos(\Delta\phi_1)}{2 \sin\left(\frac{\Delta\phi_i}{2}\right) \sin\left(\left(i - \frac{1}{2}\right) \Delta\phi_i\right)}.$$

Noting n_i the number of cells at colatitude i , we get

$$\frac{n_i}{n_1} = \left[\frac{\Delta\lambda_1}{\Delta\lambda_i} \right] = \left[\frac{2 \sin\left(\frac{\Delta\phi_i}{2}\right) \sin\left(\left(i - \frac{1}{2}\right) \Delta\phi_i\right)}{1 - \cos(\Delta\phi_1)} \right]. \quad (10)$$

Now let us assume $\forall i$, $\Delta\phi_i$ and $(i - \frac{1}{2})\Delta\phi_i$ are small enough:

$$\frac{n_i}{n_1} \approx \left[\frac{2 \frac{\Delta\phi_i}{2} \left(i - \frac{1}{2}\right) \Delta\phi_i}{\frac{\Delta\phi_1^2}{2}} \right] = 2i - 1.$$

Finally, we can define the number of cells for the whole grid, with $2n_{\text{lat}}$ latitudes, as:

$$n_i = \begin{cases} 3(2i - 1) & \text{if } 1 \leq i \leq n_{\text{lat}}. \\ n_{2n_{\text{lat}}-i+1} & \text{otherwise.} \end{cases} \quad (10)$$

It follows that the total number of cells on the grid is $6n_{\text{lat}}^2$. As an illustration, the grid is shown on Fig. 13.

its extremities (one north and two south). These figures apply for the Northern Hemisphere and must be inverted in the Southern Hemisphere.

As a consequence, computing the position of the neighbours is quite efficient, involving mostly integer operations and roundings. These computations are thus done on-the-fly to reduce memory costs. In a more general way, the analytical properties of the grid are exploited as much as possible. Our parallelization strategy relies heavily on it, as shown in Sect. 4.

2.3 Discretization

For winds and tracer discretization, we adapt the Arakawa D-grid (Arakawa and Lamb, 1977) to our scheme, as shown on Fig. 5. To avoid interpolating the winds components during advection, winds are taken at the middle of the interfaces. Tracer concentrations are defined at the centres of the cells.

It is critical for mass preservation that winds have a null divergence so we correct interpolated winds (both zonal and meridional) to achieve that. The first step in our correction deals with meridional winds. If we consider all the cells on a latitude circle, the total mass variation in this “band” only comes from the north and south meridional fluxes. Now, if we consider the latitude circle containing all south meridional fluxes, it constitutes a closed contour. Therefore, the wind divergence is null and the sum of all meridional winds must be zero. Meridional winds are thus corrected by removing the mean value from the interpolated values.

Then we correct zonal winds to ensure that the sum of all fluxes is locally null in each cell. As meridional winds are already corrected, only east and west zonal winds of each cell must be modified. We take zonal winds at longitude 0 as a reference and browse each cell sequentially from west to east to correct progressively each zonal winds and ensure mass preservation.

Finally, we need to take care that fluxes in a given direction do not completely empty the cells during an advection step. For each cell, a local advective Courant number restricts the time-step to avoid this situation. As advection is performed sequentially

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between semi-Lagrangian, finite volume and wave propagation methods. A summary is given in Table 1. Other features are described below:

- FARSIGHT is a grid-point semi-Lagrangian model, running on parallel architectures,
- CLAW uses a wave propagation technique with a first-order method (donor cell upwind) in each direction,
- SLFV-ML (Slope Limited Finite Volume scheme with Method of Lines), a flux-form finite volume with simplified swept area and linear reconstruction,
- NCAR’s CAM-FV (Community Atmosphere Model Finite-Volume) is a finite-volume model on a regular latitude-longitude grid. It uses the Piecewise Parabolic Method (PPM), with the addition of a slope and curvature limiters,
- USICOM (UC Irvine Second-Order Moments scheme) is also a flux-form finite-volume. It uses an improved version of Prather’s second order moments scheme on an Eulerian regular latitude-longitude grid.

All of these models are mass-preserving so the comparison with Pangolin is relevant. CAM-FV and UCISOM are of particular interest as they also use a directional splitting algorithm. Furthermore, all models have a shape-preserving algorithm but only FARSIGHT and Pangolin do not expand the initial data range.

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3.2 Test cases

In this paper, we only consider the case of non-divergent and time-dependent winds. Zonal and meridional winds (u and v respectively) are given by:

$$u(\lambda, \theta, t) = \frac{10R}{T} \sin^2(\lambda') \sin(2\theta) \cos\left(\frac{\pi t}{T}\right) + \frac{2\pi R}{T} \cos(\theta),$$

$$v(\lambda, \theta, t) = \frac{10R}{T} \sin(2\lambda') \cos(\theta) \cos\left(\frac{\pi t}{T}\right),$$

where θ is now the latitude, and λ the longitude, both in radians. R is the Earth radius, $T = 12$ days the period, and $\lambda' = \lambda - 2\pi t/T$. With these winds, the tracer concentration first moves eastwards and is then deformed into filaments up to $t = T/2$. After that, the flux is inverted and the tracer continues to move to the east until it comes back to its initial distribution at $t = T$.

These winds provide an easy way to compute the errors as the solution after a full period can be simply compared with the initial concentration. We will use the same normalized errors as in Lauritzen et al. (2012):

$$\ell_2(q) = \sqrt{\frac{\mathcal{J}((q - q_0)^2)}{\mathcal{J}(q_0^2)}} \quad \text{and} \quad \ell_\infty(q) = \frac{\max_{\forall \lambda, \theta} |q - q_0|}{\max_{\forall \lambda, \theta} |q_0|},$$

where $q = q(\lambda, \theta, t)$ is the tracer concentration and q_0 the initial concentration. Also, \mathcal{J} is defined as the global integral:

$$\mathcal{J}(q) = \frac{1}{4\pi} \int_0^{2\pi} \int_{-\pi/2}^{\pi/2} q(\lambda, \theta, t) \cos \theta d\lambda d\theta.$$

For our model, the tracer mixing ratio is approximated as linear functions in a cell. Thus the mean value corresponds with the value at the middle of the cell, so the integral is

approximated by $\mathcal{J}(q) = \sum_{i,j} \hat{q}_{ij} \mathcal{A}_{ij}$ where \hat{q}_{ij} is the tracer mean value in cell (i, j) and \mathcal{A}_{ij} its area given by Eq. (9).

Two initial conditions are used here: a sum of two Gaussian hills and a sum of two cosine bells. We note $(\lambda_1, \theta_1) = (5\pi/6, 0)$ and $(\lambda_2, \theta_2) = (7\pi/6, 0)$ the coordinates of the two “centres” used below. Gaussian hills are defined as:

$$q(\lambda, \theta) = h_1(\lambda, \theta) + h_2(\lambda, \theta).$$

Noting $h_{\max} = 0.95$ and $b = 5$, we have for $i = 1, 2$:

$$h_i(\lambda, \theta) = h_{\max} e^{-b((X-X_i)^2 + (Y-Y_i)^2 + (Z-Z_i)^2)}.$$

where X, Y, Z are the Cartesian coordinates of (λ, θ) and X_i, Y_i, Z_i are the Cartesian coordinates of (λ_i, θ_i) for $i = 1, 2$. Cosine bells are defined by:

$$q(\lambda, \theta) = \begin{cases} b + c \times h_1(\lambda, \theta) & \text{if } r_1 < r, \\ b + c \times h_2(\lambda, \theta) & \text{if } r_2 < r, \\ b & \text{otherwise,} \end{cases}$$

with the background value $b = 0.1$ and amplitude $c = 0.9$. Noting $h_{\max} = 1$ and $r = R/2$, we also have:

$$\forall i = 1, 2, \quad h_i(\lambda, \theta) = \frac{h_{\max}}{2} \left(1 + \cos \left(\pi \frac{r_i}{r} \right) \right).$$

where the r_i are the great-circle distances to (λ_i, θ_i) on the sphere:

$$r_i(\lambda, \theta) = R \arccos(\sin \theta_i \sin \theta + \cos \theta_i \cos(\lambda - \lambda_i)).$$

Pangolin results for the Gaussian hills and cosine bells test cases are shown in Fig. 14 at $t = 0$, half the period and after a full period. The shape of the tracer is distribution is well-preserved but numerical diffusion contributes to decrease the tracer maxima, as it appear at $t = T/2$ and $t = T$. To compute the convergence rate in Sect. 3.3, results at $t = 0$ and $t = T$ will be used, while the preservation of filaments in Sect. 3.4 is computed using the results at $t = 0$ and $t = T/2$.

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3.3 Convergence rate

This test aims to check the rate at which numerical error decreases when resolution increases. Ideally, this rate should be close to the theoretical convergence rate. The Gaussian hills test case is used here, as it provides an infinitely smooth function. Results are plotted on Fig. 15 where ℓ_2 and ℓ_∞ are plotted with a varying number of cells. When available, the impact of shape-preserving filters is also represented on the plot, with the exception of UCISOM. For this choice of models, it does not reduce errors in a significant way as it can be expected from lower-order models.

For errors at low- and mid-resolutions, Pangolin is quite close to the other models, with the exception of UCISOM. However, the errors with a large number of cells are lower for models other than Pangolin. One possible explanation is the loss of accuracy due to the interpolation when computing the meridional gradient. In general, the convergence rate of Pangolin is slower. To quantify that, we use numerical optimal convergence rates corresponding to the errors ℓ_2 and ℓ_∞ . They result from a least-square linear regression on the errors plotted vs. the resolution at the Equator:

$$\log(\ell_i) = -\kappa_i \log(\Delta\lambda) + b_i \quad \text{with} \quad i = 2, \infty.$$

For Pangolin, the regression is applied after the optimal convergence was reached. This corresponds to longitudinal resolutions at the Equator in the range $[0.75^\circ, 0.1875^\circ]$. The final numerical convergence rates are shown in Fig. 16.

This selection of models and parameters show that theoretical order is not achieved for all models. For most of them, using a different Courant number does not improve the convergence speedup, with the exception of FARSIGHT and CAM-FV. Using a CN of 10.4 (resp. 1.2) greatly improves the result of FARSIGHT (resp. CAM-FV) with a CN of 1.4 (resp. 0.2).

Furthermore, we can see the numerical convergence rate of Pangolin is slower than other models. This is not surprising when comparing with similar finite-volume schemes as CAM-FV and UCISOM which use higher-order schemes in one or more directions.

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Nevertheless, Pangolin still performs in the same range as other models. Our goal is to match the performance of these models and this will be obtained with finer grids.

3.4 Preservation of filaments

Realistic distributions can be deformed into filaments when the tracer material is stretched and gradients are increased. For some applications, it is important to check how well these filaments are preserved. In the cosine bells test case, the initial concentration is deformed into thin filaments up to $t = T/2$, before being advected to the initial position. Diagnostics are thus computed at $T/2$.

Let us consider the area where the tracer is greater than a given threshold. For non-divergent flows and for all thresholds, if this area is not preserved at all times, it suggests filaments are degraded. This leads to the definition of the following diagnostic:

$$\ell_f = \begin{cases} 100 \times \frac{A(\tau, t)}{A(\tau, 0)}, \\ 0 \quad \text{otherwise,} \end{cases}$$

where $A(\tau, t)$ is the surface area for which the tracer ratio at time t is greater or equal to τ . For Pangolin and other Eulerian schemes, $A(\tau, t)$ is defined as the sum of the cell areas where $q(t) \geq \tau$. Thus the closest ℓ_f is to 100, the better the filaments are preserved.

Results are shown in Fig. 6. All models except Pangolin are compared with different numbers of cells but with the same resolution of 0.75° at the Equator. Pangolin is shown with two different numbers of cells. The first case (shown as light solid line) has a resolution of approximately 0.75° at the Equator. The second one (shown as dark solid line) is a higher-resolution version which approaches the results of more accurate models.

The behaviour of the models on non latitude-longitude grids (all models, except UCSOM and CAM-FV) is typical of diffusive schemes. They tend to diffuse the base of the distribution and reduce the maxima, thus leading to an increase of ℓ_f for small τ

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and a decrease of ℓ_f for large τ . Another information we can extract from this is the alteration of gradients. Here CAM-FV can be seen to have $\ell_f > 100$ for large τ , which results from gradients steepening. On the other hand, schemes on non-regular grids have a smooth and decreasing profile, showing the scheme diffusion is also smooth and continuous.

Furthermore, we can see the coarser version of Pangolin is quite close to models using non regular latitude-longitude grids (CLAW, FARSIGHT, SLFV-ML). ℓ_f is then increased for lower threshold values and decreased for higher τ . This behaviour is typical of highly-diffusive schemes. Also, as ℓ_f is not greater than 100 for large τ , it confirms gradients are not steepened by the scheme.

On the contrary, the preservation of filaments is improved for models using a regular latitude-longitude grid. While this comparison may look detrimental to Pangolin, a lower-order van Leer scheme was chosen to enable efficient and scalable parallel performances. Therefore, our strategy is to reach the accuracy of these models by using a finer grid. Using parallel architectures helps us to greatly reduce the computational cost of finer resolutions.

3.5 Preservation of preexisting relations

When advecting several correlated tracers, numerical transport schemes should preserve the relations between them. However, errors due to numerical diffusion can modify these relations and introduce a “mixing”. This is by no means an unphysical feature as real-life tracers can undergo some mixing too, either by chemical reactions or diffusion. This test aims to assess the amount of unphysical mixing. To that end, we follow Lauritzen et al. (2012) and use a first tracer with the cosine bells initial condition $q_{\text{cos}}(t = 0)$ and a second tracer correlated to the first:

$$q_{\text{corr}}(t = 0) = -0.8q_{\text{cos}}^2(t = 0) + 0.9. \quad (12)$$

After a half-period of advection using the non-divergent winds for each case, we plot $q_{\text{corr}}(t = T/2)$ against $q_{\text{cos}}(t = T/2)$ as a scatter plot. Depending on the position of the

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points, we can then check the mixing level. An illustration of the different zones is given in Fig. 7. The convex area shown in dark on the figure corresponds to “real” mixing as it contains all the lines between two points on the curve defined previously. The light gray area is not a physical mixing but is still in the initial range. Everything outside the box is overshooting.

Results are shown in Figs. 8 and 11. All unlimited schemes present some overshooting for low value of q_{cos} , which is then removed with a shape-preserving filter. Also, all schemes, with the exception of UCISOM, present real mixing. For this selection of models, only FARSIGHT and CAM-FV do have range-preserving unmixing. For FARSIGHT, that can be removed with a larger CN. In that case, its accuracy is on the same level as UCISOM. Concerning accuracy, the closer the points lie to the curved defined in Eq. (12), the more the scheme preserves the initial relation. In that respect, UCISOM is a clear contender but Pangolin also performs very well.

4 Parallelization

For large scale numerical simulations, using only sequential computations is no longer affordable. To use a parallel approach, we need to split and balance the computational effort among a set of computing units. For PDE-based simulations where the computational cost is evenly shared among the cells, a natural and widely used approach is to partition the computational domain into connex subdomains of similar sizes. Each subdomain is handled by a different computing unit that leads a well-balanced parallel calculation.

The original objectives in designing this model were twofold. First, we intended to have a discretization with cells of equal areas so that the CFL condition is not penalized by the smallest cells. Second, we targeted a semi-structured grid to avoid managing complex data structures as well as an extra-tool to generate it. This leads us to define the grid detailed in Sect. 2.2 where computing the neighbours of grid cells is fully analytic. In a parallel framework, this grid has an additional asset as it enables

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a custom analytic partitioning. Otherwise, mesh splitting often requires sophisticated mesh partitioning tools such as those developed by Karypis and Kumar (1995) or Pellegrini (2012).

4.1 Partitioning

In order to perform the partitioning, we first exploit the grid symmetries. The grid is composed of six identical zones as described in Sect. 2.2. We then focus on partitioning one of these zones, which contains n_{lat}^2 cells, where n_{lat} is the number of latitudes in the hemisphere. A perfect work balance occurs when there are p^2 subdomains with p dividing n_{lat} . In this case, each subdomain contains exactly $(n_{\text{lat}}/p)^2$ cells. The most natural way to gather cells to form the subdomains is to use the same algorithm as the one to build the grid. The p^2 subdomains are set on p bands, where the k th band contains $2k - 1$ subdomains ($k > 0$). Applying the same decomposition to the remaining five zones leads to the structure shown in Fig. 17.

For the sake of flexibility, this optimal situation can be slightly degenerated to accommodate any number of subdomains. For these sub-optimal situations, we consider the closest lower square p'^2 on a zone, with p' dividing n_{lat} . These p'^2 subdomains are set according to the previous strategy. The remaining $p^2 - p'^2$ cores are associated with on a special band, with less cells and thus without preserving the partition size.

These results are given for one zone only. For the complete grid, we find the optimal number of subdomains is $6p^2$ with p dividing n_{lat} . Otherwise, the model can manage any number of subdomains on one third of the grid (between longitude 0 and 120). The total number of subdomains in these optimal cases is then a multiple of 3. It is worthwhile noticing that White and Dongarra (2011) need a condition similar to our perfect case for their parallel version: the number of subdomains must be of the form $6p^2$, with p dividing the number of cells on a cube edge.

This analytical partitioning uses the regular topology of the grid to create subdomains with a regular shape. This feature ensures regular data access and allows for

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Each advection step can be decomposed into several tasks: gradient computing, fluxes computing and mass update. The first two tasks require some communication and the non-blocking approach is used for each one of them. It should be noted that meridional advection requires an extra communication as it needs a zonal gradient to perform an interpolation (see Sect. 2.3). The different tasks are shown in detail in Algorithm 10 and 12. The combination of boundary and interior cells for all these tasks is shown in Fig. 9.

The boundary zone is much larger for meridional advection as data needs to be exchanged with its four neighbours. More precisely, computation of the zonal gradient requires communication with the east and west neighbours of the subdomain. Furthermore, computing the meridional gradient and fluxes requires access to the north and south neighbours. Due to the semi-structured layout of the grid, this results in the “stair”-like structure for boundary cells in the meridional advection.

Most of the computation is performed during meridional advection. First, due to the extra step of computing the zonal gradient, meridional transport requires three send/receive (vs. two for zonal transport). Also, the number of boundary cells is larger, thus increasing the communication volume. Finally, computation in a cell is more expensive as the number of neighbours is four on average (vs. two in the zonal case).

4.3 Performances

In this section, we investigate the parallel scalability of our implementation of the numerical scheme. Tests were done on the Bull cluster at CERFACS, whose features are shown in Table 4. We consider a strong speed-up study where the size of the global grid is fixed and the number of computing cores is increased. Ideally, the parallel elapsed time should be reduced proportionally to the number of cores selected for the parallel simulation. For our experimental study, we consider the elapsed time on three cores as the reference time so that the speed-up is defined by

communication volumes only increase linearly as a function of the number of tracers, as expected.

5 Conclusions

In this paper, we have presented a parallel scalable algorithm for 2-D-transport on the sphere. We focused on making the model as parallel as possible. Pangolin uses a reduced latitude-longitude grid, which overcomes the pole issue, and a finite-volume formulation that ensures local conservation of the tracer mass. Grid features were carefully exploited to minimize memory requirements on one hand, and provide maximal efficiency on parallel architectures on the other hand. The accuracy of the scheme was also chosen as to minimize the impact on message-passing. While the accuracy may make it less appealing than other models, the goal of Pangolin is to use finer resolutions to achieve the same accuracy.

The scalability of Pangolin is already very good, providing the resolution is fine enough. We expect further improvement in terms of parallelism when chemistry is added. An ongoing work addresses a real-case atmospheric situation for the transport, with a comprehensive chemical scheme. Multi-threading in the subdomains will be enabled to mitigate the possible load balancing issues introduced by the chemistry. As a conclusion, Pangolin is a very practical model, aiming at taking advantage of present and future parallel architectures for large-scale atmospheric transport.

Code availability

The code is copyrighted to the CERFACS laboratory. The documentation is available as a user manual and as the code documentation at <http://cerfacs.fr/~praga/pangolin/index.html>. To request access to either the source code or documentation, please send a mail to A. Praga (praga@cerfacs.fr) or D. Cariolle (cariolle@cerfacs.fr). The data and scripts for the plots of this paper are also available as a Supplement.

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References

- Arakawa, A. and Lamb, V. R.: Computational design of the basic dynamical processes of the UCLA general circulation model, *Methods in Computational Physics*, 17, 173–265, 1977. 4537
- Belikov, D., Maksyutov, S., Miyasaka, T., Saeki, T., Zhuravlev, R., and Kiryushov, B.: Mass-conserving tracer transport modelling on a reduced latitude-longitude grid with NIES-TM, *Geosci. Model Dev.*, 4, 207–222, doi:10.5194/gmd-4-207-2011, 2011. 4529
- Chipperfield, M. P.: New version of the TOMCAT/SLIMCAT off-line chemical transport model: intercomparison of stratospheric tracer experiments, *Q. J. Roy. Meteorol. Soc.*, 132, 1179–1203, doi:10.1256/qj.05.51, 2006. 4528
- Collins, W. and Rasch, P.: Description of the NCAR community atmosphere model (CAM 3.0), NCAR Tech. Note, 2004. 4554
- Godunov, S., Zabrodin, A., and Prokopov, G.: A computational scheme for two-dimensional nonstationary problems of gas dynamics and calculation of the flow from a shock wave approaching a stationary state, *Zhurnal Vychislitel'noi*, 1, 1020–1050, 1961. 4532
- Hourdin, F. and Armengaud, A.: The use of finite-volume methods for atmospheric advection of trace species. Part I: Test of various formulations in a general circulation model, *Mon. Weather Rev.*, 127, 822–837, 1999. 4529, 4532, 4534
- Huijnen, V., Williams, J., van Weele, M., van Noije, T., Krol, M., Dentener, F., Segers, A., Houweling, S., Peters, W., de Laat, J., Boersma, F., Bergamaschi, P., van Velthoven, P., Le Sager, P., Eskes, H., Alkemade, F., Scheele, R., Nédélec, P., and Pätz, H.-W.: The global chemistry transport model TM5: description and evaluation of the tropospheric chemistry version 3.0, *Geosci. Model Dev.*, 3, 445–473, doi:10.5194/gmd-3-445-2010, 2010. 4528

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- Karypis, G. and Kumar, V.: METIS – Unstructured Graph Partitioning and Sparse Matrix Ordering System, Version 2.0, 1995. 4546
- Lauritzen, P. H., Skamarock, W. C., Prather, M. J., and Taylor, M. A.: A standard test case suite for two-dimensional linear transport on the sphere, *Geosci. Model Dev.*, 5, 887–901, doi:10.5194/gmd-5-887-2012, 2012. 4530, 4538, 4540, 4544
- Lauritzen, P. H., Ullrich, P. A., Jablonowski, C., Bosler, P. A., Calhoun, D., Conley, A. J., Enomoto, T., Dong, L., Dubey, S., Guba, O., Hansen, A. B., Kaas, E., Kent, J., Lamarque, J.-F., Prather, M. J., Reinert, D., Shashkin, V. V., Skamarock, W. C., Sørensen, B., Taylor, M. A., and Tolstykh, M. A.: A standard test case suite for two-dimensional linear transport on the sphere: results from a collection of state-of-the-art schemes, *Geosci. Model Dev.*, 7, 105–145, doi:10.5194/gmd-7-105-2014, 2014. 4538
- Leer, B. V.: Towards the ultimate conservative difference scheme. IV. A new approach to numerical convection, *J. Comput. Phys.*, 23, 276–299, 1977. 4532
- LeVeque, R.: *Finite Volume Methods for Hyperbolic Problems*, Cambridge University Press, 2002. 4554
- Machenhauer, B., Kaas, E., and Lauritzen, P.: Finite volume methods in meteorology, *Methods for the Atmosphere*, 14, 3–120, doi:10.1016/S1570-8659(08)00201-9, 2009. 4533
- Miura, H.: An upwind-biased conservative advection scheme for spherical hexagonal – pentagonal grids, *Mon. Weather Rev.*, 135, 4038–4044, doi:10.1175/2007MWR2101.1, 2007. 4554
- Pellegrini, F.: PT-Scotch and LibPTScotch 0.6 User's Guide, Tech. rep., 2012. 4546, 4547
- Prather, M. J.: Numerical advection by conservation of second-order moments, *J. Geophys. Res.*, 91, 6671–6681, 1986. 4554
- Rood, R. B.: Numerical advection algorithms and their role in atmospheric transport and chemistry models, *Rev. Geophys.*, 25, 71–100, 1987. 4532
- Staniforth, A. and Thuburn, J.: Horizontal grids for global weather and climate prediction models: a review, *Q. J. Roy. Meteor. Soc.*, 138, 1–26, doi:10.1002/qj.958, 2012. 4529
- Teysse re, H., Michou, M., Clark, H. L., Josse, B., Karcher, F., Oliv e, D., Peuch, V.-H., Saint-Martin, D., Cariolle, D., Atti , J.-L., N ed lec, P., Ricaud, P., Thouret, V., van der A, R. J., Volz-Thomas, A., and Ch eroux, F.: A new tropospheric and stratospheric Chemistry and Transport Model MOCAGE-Climat for multi-year studies: evaluation of the present-day climatology and sensitivity to surface processes, *Atmos. Chem. Phys.*, 7, 5815–5860, doi:10.5194/acp-7-5815-2007, 2007. 4528

White, J. and Dongarra, J.: High-performance high-resolution semi-Lagrangian tracer transport on a sphere, *J. Comput. Phys.*, 230, 6778–6799, doi:10.1016/j.jcp.2011.05.008, 2011. 4546, 4554

Williamson, D.: The evolution of dynamical cores for global atmospheric models, *J. Meteorol. Soc. Jpn.*, 85, 241–269, 2007. 4529

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Table 2. Some Pangolin configurations, with the number of latitudes on an hemisphere n_{lat} , total number of cells n_{pangolin} and resolution at the Equator in degrees.

n_{lat}	n_{pangolin}	$\Delta\phi \times \Delta\lambda$
20	2400	4.5×3.08
90	48 600	1.0×0.67
320	614 400	0.28×0.188

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Table 3. For a given resolution at the equator, we compare the total number of cells of each model n_{model} vs. the total number of cells of Pangolin n_{pangolin} .

Model	$n_{\text{model}}/n_{\text{pangolin}}$	n_{model}
FARSIGHT	2	$6 \cdot (90/\Delta\lambda)^2$
CLAW	0.68	$2 \cdot (90/\Delta\lambda)^2$
SLFV-ML	2.17	N.A
UCISOM	2.7	$[360/\Delta\lambda] \cdot [180/\Delta\lambda]$
CAM-FV	2.7	$[360/\Delta\lambda] \cdot [180/\Delta\lambda]$
Pangolin	1	$6 \cdot [0.5 \cdot [120/\Delta\lambda] + 1]^2$

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Table 4. Configuration for one of the 158 SandyBridge nodes.

- 2 Intel Sandy Bridge 8-cores CPUs
(peak performance of 330 GFlops s⁻¹)
- 32 GB of memory
- 31 KB L1 cache, 256 KB L2 cache for each core
- 20 MB L3 cache, shared by the 8 cores of each CPU

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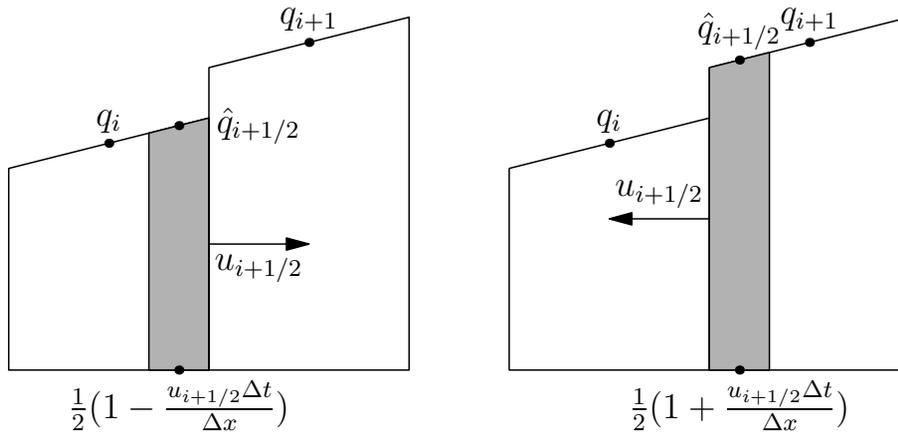


Figure 1. van Leer scheme for positive (left) and negative (rights) winds. The distribution of the tracer is shown as broken lines. The grey area is the quantity of tracer passing through the interface during a time-step.

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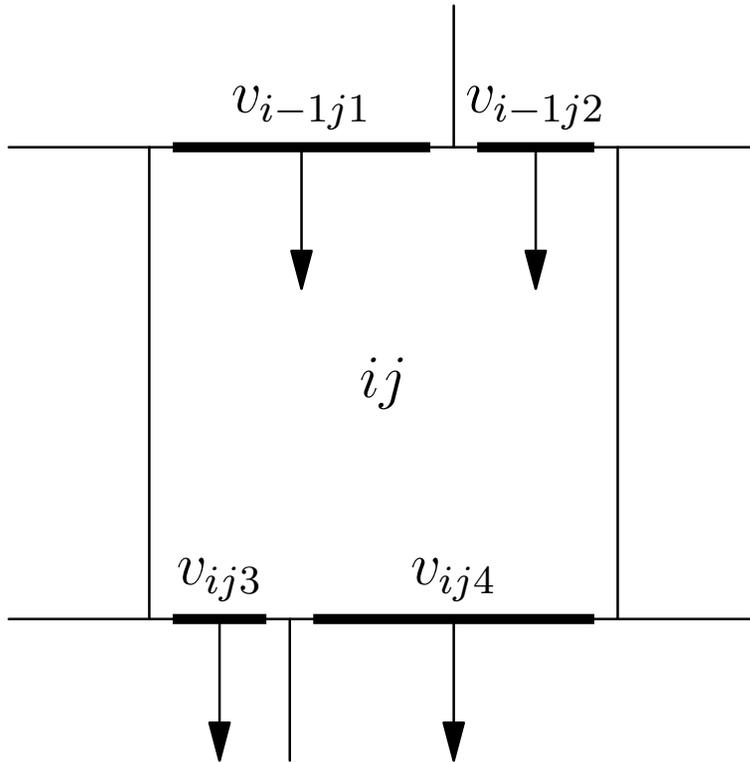


Figure 2. Meridional interfaces (bold lines) and fluxes (dark arrows) for cell (i, j) .

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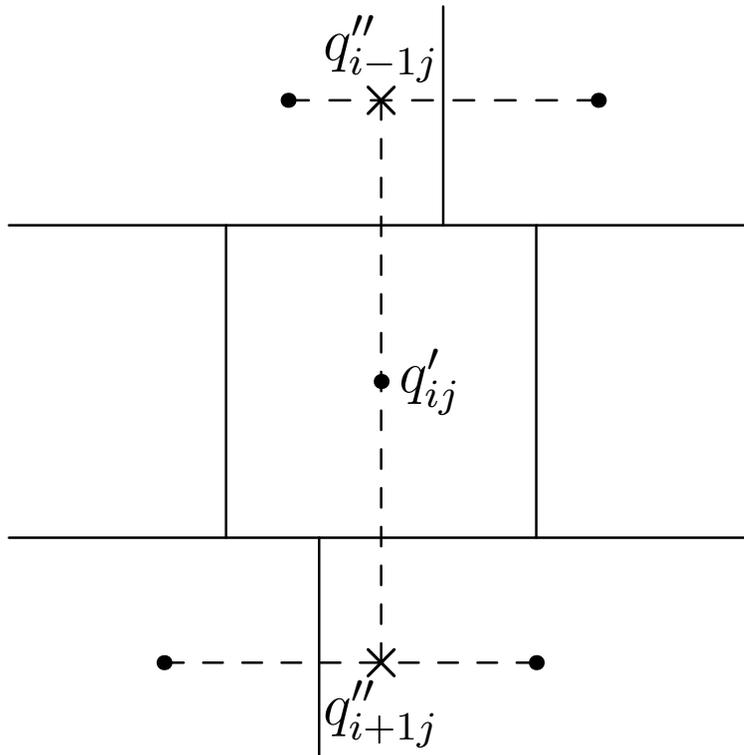


Figure 3. Zonal interpolation to compute the meridional gradient of q'_{ij} .

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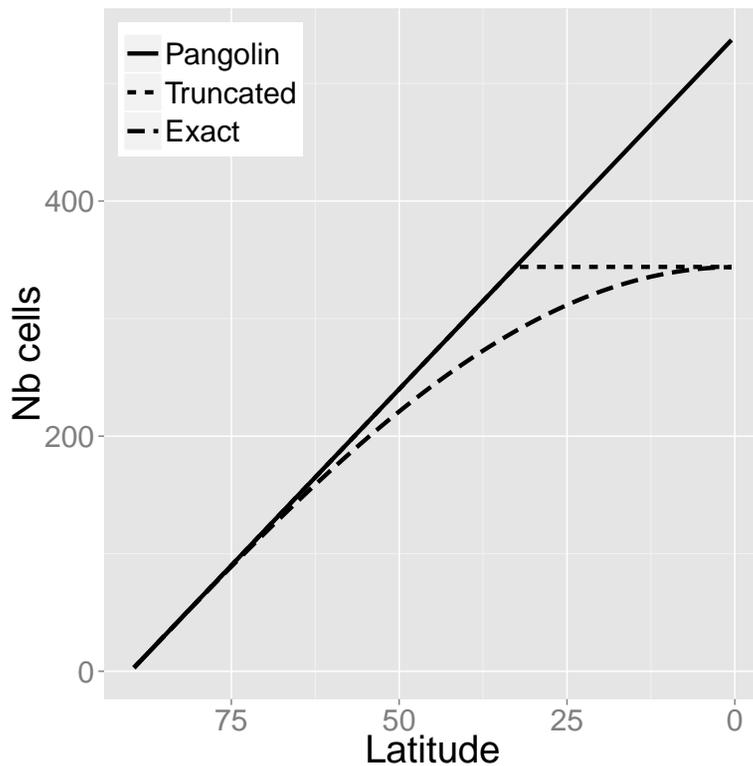


Figure 4. Number of cells for the grid used by Pangolin on one hemisphere with 90 latitudes (solid line). The truncated and “exact” version are shown as dotted and dashed lines respectively.

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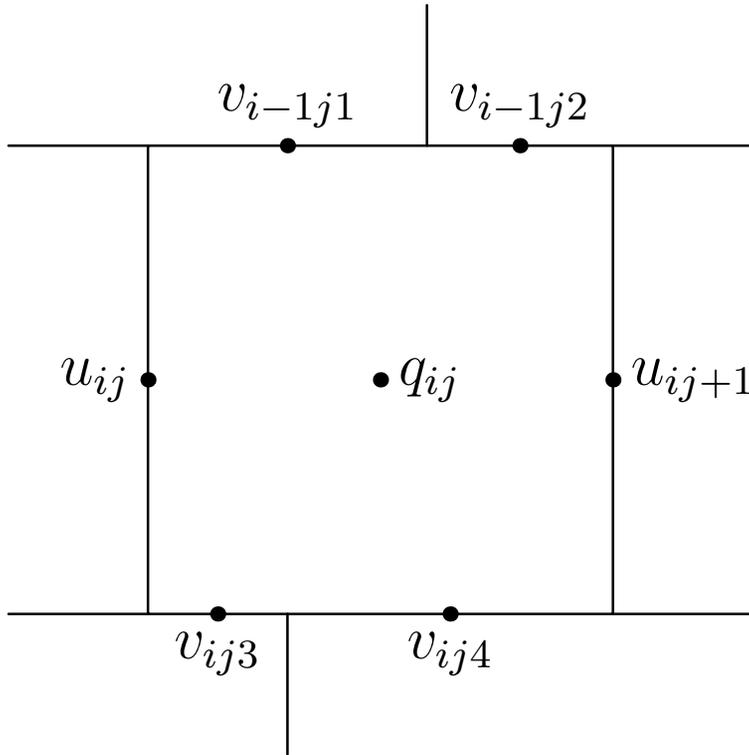


Figure 5. Discretization for zonal and meridional winds (u and v respectively) and tracer mixing ratio q .

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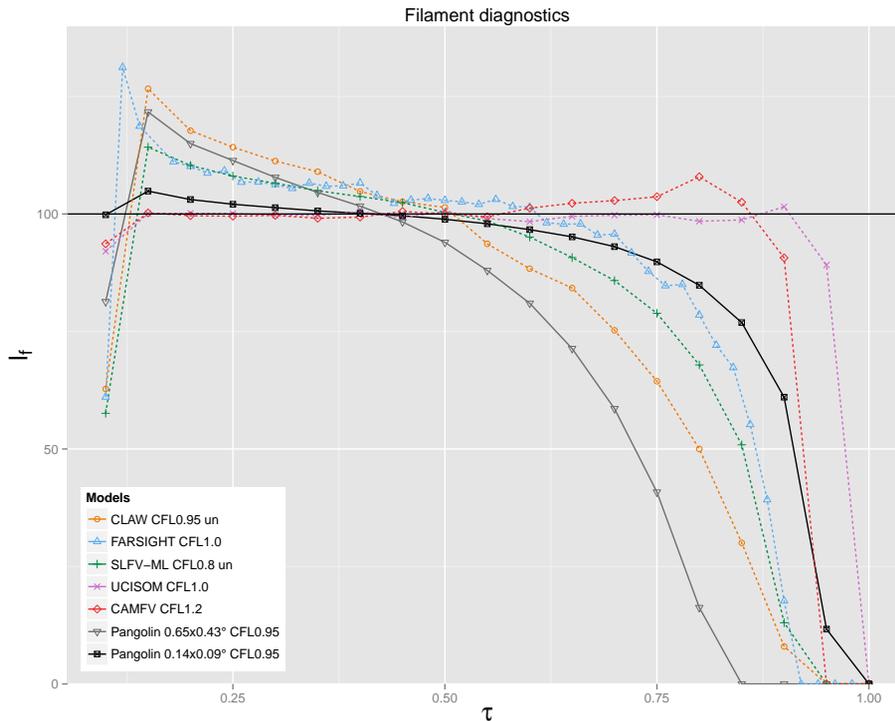


Figure 6. Filament diagnostics between for Pangolin (solid line) and other models (dashed line). By default, the shape-preserving version is used. Only CLAW and SLFV-ML use an “unlimited” version.

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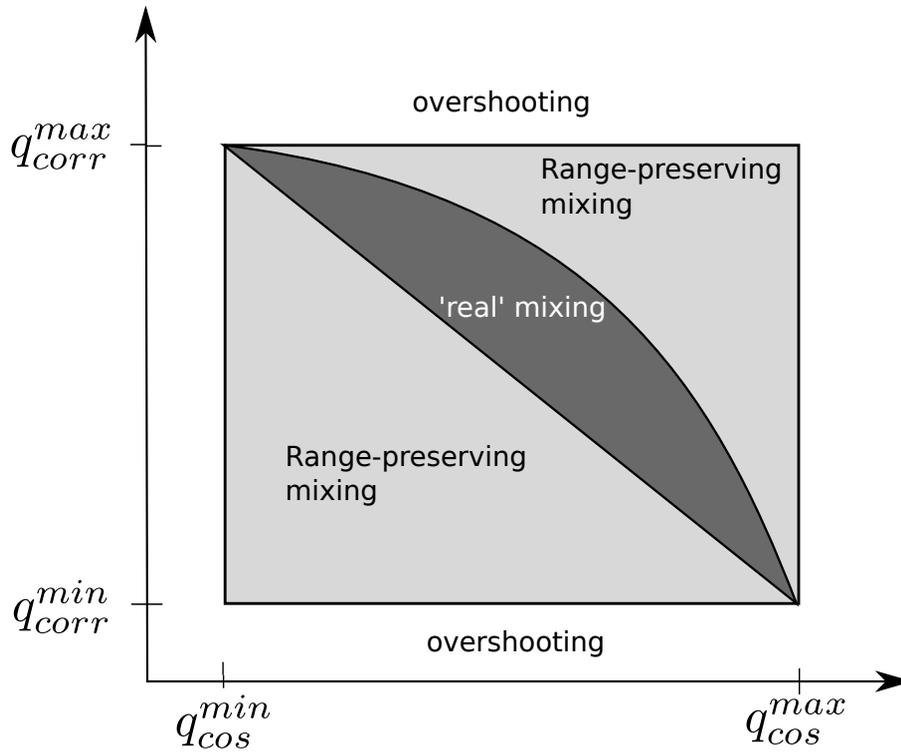


Figure 7. Different types of mixing when plotting the correlated concentration against the cosine bells distribution.

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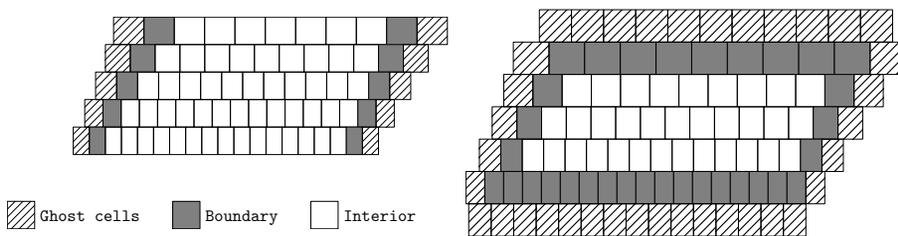


Figure 9. Ghost, boundary and interior cells for zonal (left) and meridional (right) advection.

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- 1: **subroutine** zonal_advection
- 2: Starts ratio exchange for ghost cells
- 3: Compute zonal gradient on the interior
- 4: Wait for end of communications
- 5: Compute zonal gradient on the boundary
- 6:
- 7: Starts zonal gradient exchange for ghost cells
- 8: Compute zonal fluxes on the interior
- 9: Wait for end of communications
- 10: Compute zonal fluxes on the boundary
- 11:
- 12: Update all ratios
- 13: **end subroutine**

Figure 10. Main steps of the algorithm for zonal advection.

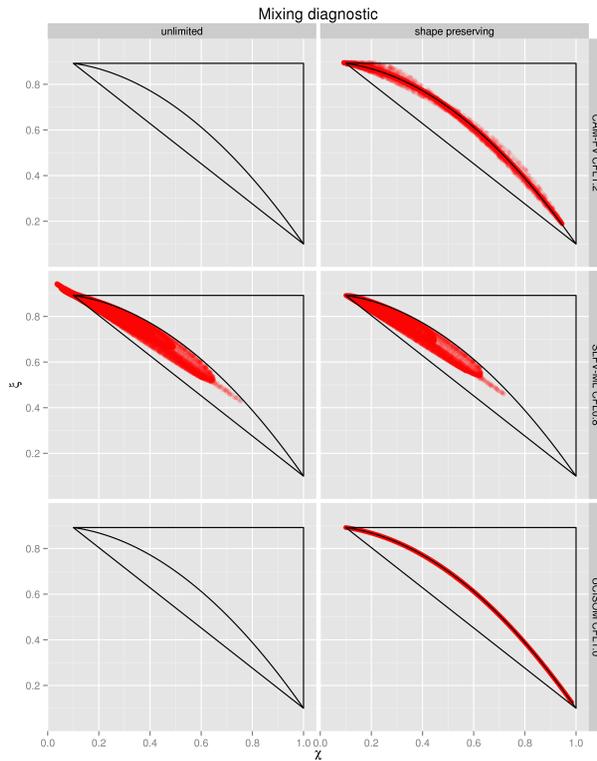


Figure 11. Mixing plots for both unlimited and shape-preserving versions. The resolution is set at 0.75° at the Equator, except for Pangolin, which has 0.376° .

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1: subroutine meridional_advection
2:   Starts ratio exchange for ghost cells
3:   Compute zonal gradient on the interior
4:   Wait for end of communications
5:   Compute zonal gradient on the boundary
6:
7:   Starts zonal gradient exchange for ghost cells
8:   Compute meridional gradient on the interior
9:   Wait for end of communications
10:  Compute meridional gradient on the boundary
11:
12:  Starts meridional gradient exchange for ghost cells
13:  Compute meridional fluxes on the interior
14:  Wait for end of communications
15:  Compute meridional fluxes on the boundary
16:
17:  Update all ratios
18: end subroutine
```

Figure 12. Main steps of the algorithm for meridional advection.

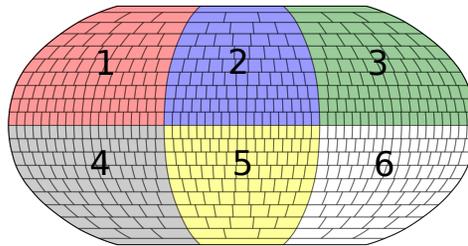
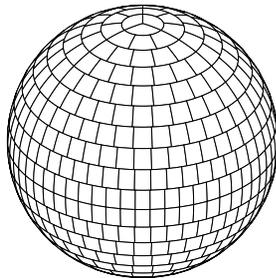


Figure 13. Grid used in Pangolin with 20 latitudes: orthographic projection (left) and Robinson projection, with the 6 identical zones highlighted (right).

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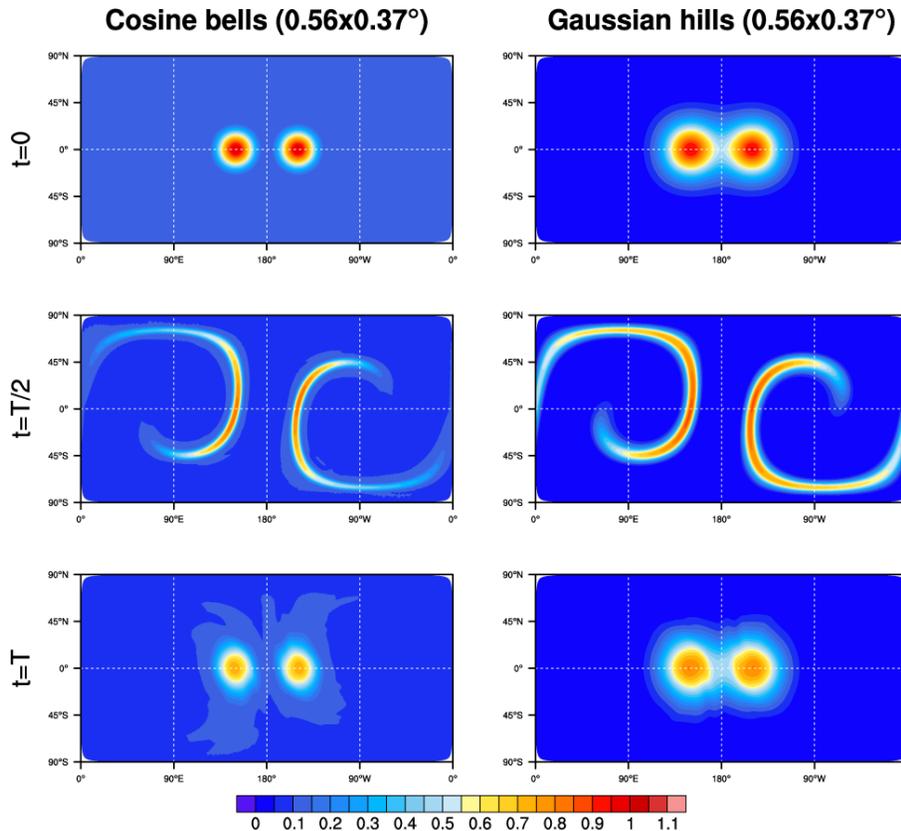


Figure 14. Cosine bells and Gaussian hills results for $t = 0$, $t = T/2$, $t = T$ (top to bottom) with Pangolin. The initial distribution is first deformed into filaments and then advected back to its initial position. The Equator resolution is $0.56^\circ \times 0.37^\circ$. For these plots, Pangolin data is interpolated to a regular latitude-longitude grid.

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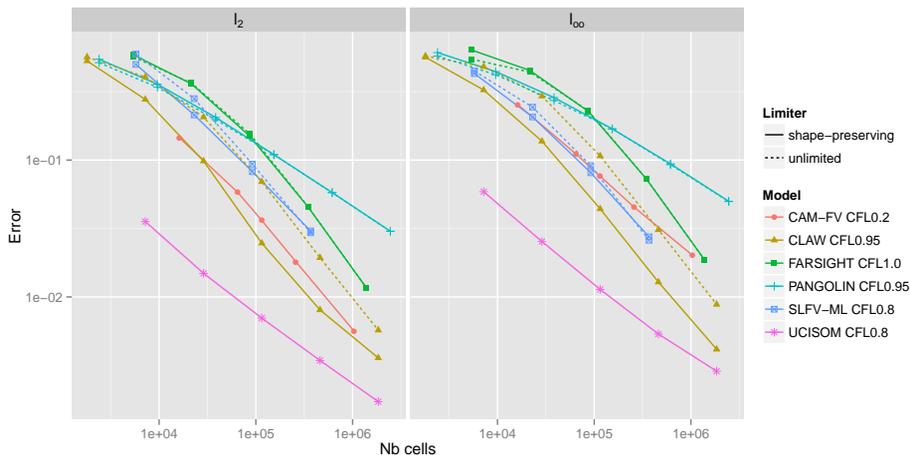


Figure 15. Numerical convergence rate for both error measures. There are computed using Gaussian hills after a full rotation. When available, the models are shown with and without the shape-preserving limiters.

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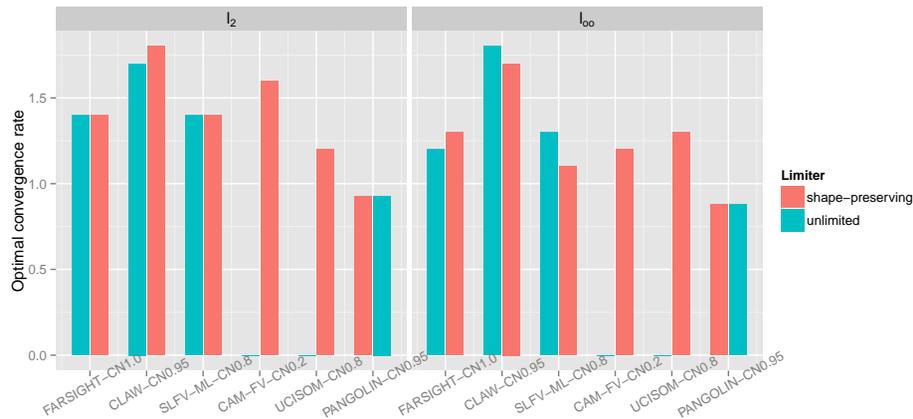


Figure 16. Optimal convergence rate computed by a least-square regression on data from Fig. 15. Some models did not offer data without shape-preserving limiters (CAM-FV, UCISOM).

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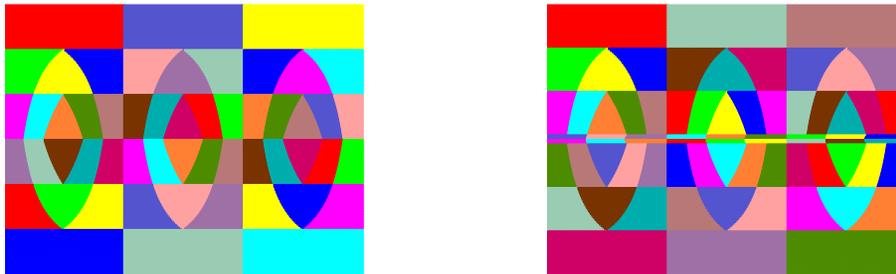


Figure 17. Analytical mesh partitioning for an optimal case (54 domains, left) and sub-optimal case (74 partitions, left). Each color corresponds to a subdomain (the same color can be used for different subdomains). The grid contains 8100 cells and is shown in latitude-longitude coordinates.

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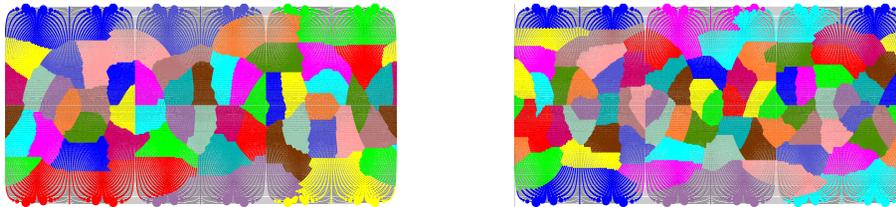


Figure 18. Mesh partitioning computed by the general purpose mesh partitioner Scotch for 54 domains (optimal case for Pangolin, left) and 72 domains (sub-optimal case for Pangolin, right). Each color corresponds to a subdomain (the same color can be used for different partitions). The grid contains 8100 cells and is shown in latitude-longitude coordinates.

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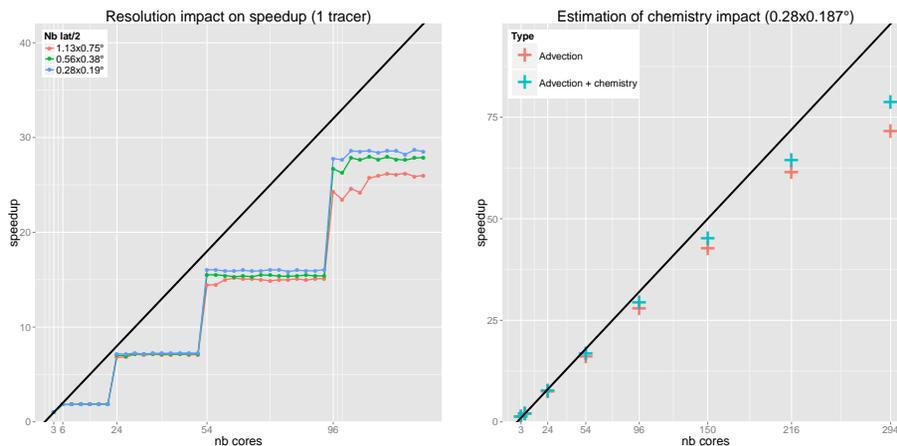


Figure 19. Speedup up to 126 cores (left) and 294 cores (right). The left plot shows the impact of grid resolution for smaller configurations. The right plot shows both the advection performances and an estimation of the chemistry impact on scalability. Resolutions used are: $1.125^\circ \times 0.75^\circ$, $0.56^\circ \times 0.376^\circ$, $0.28^\circ \times 0.188^\circ$. Both figures use non-divergent winds from Sect. 3 over a full period with a CFL of 0.96.