Model-data fusion across ecosystems: from multi-site optimizations to global simulations

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Abstract

This study uses a variational data assimilation framework to simultaneously constrain a global ecosystem model with eddy covariance measurements of daily net ecosystem exchange (NEE) and latent heat (LE) fluxes from a large number of sites grouped in seven plant functional types (PFTs). It is an attempt to bridge the gap between the numerous site-specific parameter optimization works found in the literature and the generic parameterization used by most land surface models within each PFT. The present multi-site approach allows deriving PFT-generic sets of optimised parameters enhancing the agreement between measured and simulated fluxes at most of the sites considered, with performances often comparable to those of the corresponding site-specific optimizations. Besides reducing the PFT-averaged model-data root-mean-square difference (RMSD) and the associated daily output uncertainty, the optimization improves the simulated CO₂ balance at tropical and temperate forests sites. The major site-level NEE adjustments at the seasonal scale are: reduced amplitude in C3 grasslands and boreal forests, increased seasonality in temperate evergreen forests, and better model-data phasing in temperate deciduous broadleaf forests. Conversely, the poorer performances in tropical evergreen broadleaf forests points to deficiencies regarding the modeling of phenology and soil water stress for this PFT. An evaluation with data-oriented estimates of photosynthesis (GPP) and ecosystem respiration (Reco) rates indicates distinctively improved simulations of both gross fluxes. The multi-site parameter sets are then
tested against CO$_2$ concentrations measured at 53 locations around the globe, showing significant adjustments of the modelled seasonality of atmospheric CO$_2$ concentration, whose relevance seems PFT-dependent, along with an improved interannual variability. Lastly, a global scale evaluation with remote sensing NDVI measurements indicates an improvement of the simulated seasonal variations of the foliar cover for all considered PFTs.

1. **Introduction**

Land surface models (LSMs) have been tools of growing importance in the continuous effort to develop comprehensive Earth system models which help to understand the effects of changes in land surface processes and land-use practices upon biogeochemical (carbon, water, nutrients) and energy cycles, and more generally upon the Earth’s climate (Cramer et al., 2001; Friedlingstein et al., 2006; Sitch et al., 2008). With the goal of improving accuracy and realism, the increasing amount and range of scale of the processes included in mechanistic LSMs result in a growing number of parameters associated with the corresponding model equations (Pitman, 2003). Some parameters are easily identified with a given physical process (and can sometimes be measured); others are purely empirical and account for a variety of processes embodied in a few equations, yet to be refined. In both cases, obvious computational and complexity limits have traditionally led model developers to use broad classes of soil and vegetation types, for which typical, generic parameter values are assigned (e.g., (Sellers et al., 1996)).

One difficulty is in scaling up the leaf- and plant-level measurements of physical parameters for ecosystem-scale simulations (Jarvis, 1995; Bonan et al., 2012). Besides, the variety of species within each of the 10 to 20 plant functional types (PFTs) typically used by most models makes the choice of a representative parameter value critical, thus adding significant uncertainty to the model outputs. In this context, parameter optimization methods have been increasingly used to calibrate model parameters and reduce the associated uncertainty. The criterion is to minimize the misfit between simulation outputs and observed data (Raupach et al., 2005). As for ecosystem models, eddy covariance measurements provide direct, near-continuous, in situ observations of carbon dioxide, water and energy exchanges between the canopy and the atmosphere (Baldocchi et al., 2001; Baldocchi, 2008). This measurement method has been applied across an extensive global network (560 sites as of October 2013), spanning a wide range of ecosystems and climates (http://fluxnet.ornl.gov/).

Over the last decade, numerous studies with various LSMs have used this available information to derive sets of parameters that significantly improve the model-data fit, with optimization approaches ranging from simple parameter adjustments to rigorous data assimilation frameworks (e.g., (Wang et al., 2001, 2007; Reichstein et al., 2003; Braswell et al., 2005; Knorr and Kattge,
However, most of these efforts have focused on model calibration at individual sites. It often results in model parameters overly tuned to the specifics of a particular site given the small spatial footprint of each flux tower (typically a few hectares). Only recently, some studies started to assess through optimization the generic nature of model parameters within PFTs. The benefit of a set of parameters derived at one site was evaluated for simulations at a similar site (Medvigy et al., 2009; Verbeeck et al., 2011) and over the surrounding region (Medvigy and Moorcroft, 2012), with encouraging results. In parallel, two independent efforts simultaneously used data constraints from several sites to assess the degree of improvement of the simulated fluxes depending on the “generic criterion” used for the optimised parameters (Groenendijk et al., 2011; Kuppel et al., 2012). The study of (Groenendijk et al., 2011), conducted at over a hundred locations across several PFTs, found that the cross-site parameter variability after optimization explained the poorer performances of grouping sites by PFT, while no such discrepancy appeared in (Kuppel et al., 2012), a study however limited to temperate deciduous broadleaf forests.

Building on the optimization procedure developed by (Kuppel et al., 2012), the present work assesses the potential of the multi-site assimilation of carbon net ecosystem exchange (NEE) and latent heat (LE) flux measurements in a process-based terrestrial ecosystem model (ORCHIDEE). The objective is to improve site-scale simulations of carbon and water fluxes at a large number of flux towers sites, as well as global scale simulations of vegetation phenology and terrestrial carbon balance. Specifically, we address the following questions: 1) for each of the seven PFTs considered (out of 12 in ORCHIDEE, 5 being not covered by the measurements used here), can we find a generic set of optimised parameters that enhance the model-data fit at all sites? 2) how well does the multi-site approach compare to site-specific optimizations? 3) what are the main improvements introduced by the optimization procedure from seasonal to annual time scales: daily error, model-data bias, seasonal cycle amplitude and/or phase? 4) which processes remain poorly captured by the model after optimization? 5) have the eddy-covariance-constrained sets of multi-site parameters a notable impact on global scale simulations?

Section 2 presents the ecosystem model, the data assimilation system, and the eddy covariance measurements used in this study, as well the supplementary datasets and models. The results are presented and discussed in Sect. 3, successively dealing with the model-data fit at the site level (3.1), the comparison between multi- and single-site results (3.2), the uncertainties of modelled NEE and LE (3.3). Then are evaluated the impact of the derived multi-site parameterization upon the site-scale simulation of photosynthesis and ecosystem respiration rates (3.4), and at the global scale upon the simulated seasonality and interannual variability of atmospheric CO₂ concentration (3.5.1) and finally upon the seasonality of vegetation activity (3.5.2).
2. Materials & Methods

2.1 Vegetation model and optimised parameters

The biogeochemical vegetation model used in this study is ORCHIDEE (Organizing Carbon and Hydrology in Dynamic Ecosystems, Krinner et al., 2005). It calculates the water, energy and carbon fluxes between the land surface and the atmosphere at a half-hourly time step. The exchange of carbon and water during photosynthesis and the energy balance are treated every 30 minutes, while carbon allocation, autotrophic respiration, foliar onset and senescence, mortality and soil organic matter decomposition are computed on a daily time step. The soil hydrology follows a double-bucket scheme (Ducoudré et al., 1993) and its impact on stomatal conductance is described in (Krinner et al., 2005). The reader is referred to previous publications for the standard equations of ORCHIDEE (e.g., Kuppel et al., 2012). As in most biogeochemical models, the vegetation is grouped into several PFTs, 12 in the case of ORCHIDEE, excluding bare soil. Except for the modelled phenology (Botta et al., 2000), the equations governing the different processes are generic across PFTs, but with specific parameter values for each vegetation class. When used in “grid-point mode” at a given site, we force the model with the corresponding half-hourly gap-filled meteorological data measured at the flux towers. At the global scale, the global ERA-Interim meteorology (Dee et al., 2011) is used as forcing and the model outputs are calculated at a 0.72 x 0.72 deg² resolution. In this case the global PFT map is computed at the spatial resolution of the forcing fields, from an original vegetation map available at 5km, which is derived from a high-resolution IGBP AVHRR global land dataset (Eidenshink and Faundeen, 1994) and uses 94 ecosystem classes (Olson, 1994). Importantly, the modelled carbon pools are initially brought to equilibrium before both site- and global-scale simulations by cycling the available meteorological forcing over several centuries (spin up procedure), with the prior parameterization of the model. This procedure ensures a net carbon flux close to zero over annual-to-decadal timescales.

Table 1 presents the PFT-generic parameters used in this study. As our emphasis is on adjusting the carbon cycle, there are significantly more optimised parameters leveraging on photosynthesis and respiration processes than, for instance, on the energy balance. We also included two additional parameters to optimise the initial state of the model provided by the spin up procedure, which are 1) a common multiplier of the initial carbon pool content, by default equal to one, and 2) the initial leaf area index (LAI) of non-deciduous PFTs, by default taken from the spin up outputs. Both parameters are considered as site-specific, since the soil organic carbon content is closely related to the local land-use history, while the foliar cover of evergreen and herbaceous species directly relates to vegetation history at the site level. One consequence is that they cannot be spatially extrapolated,
thus the global simulations performed for evaluation (see sect. 2.4) use the default value of these
last two parameters, i.e., using the initial carbon pool content and foliar cover provided by the spin
up procedure.

2.2 Data assimilation system

The model parameters are optimised using the variational data assimilation method described in
(Kuppel et al., 2012). Assuming a Gaussian distribution for errors on the parameters, the model
outputs and the measured data, the optimised set of parameters corresponds to the minimization of
the following Bayesian cost function $J(x)$ (Tarantola, 2005):

$$
J(x) = \frac{1}{2} \left[ (y - H(x))^T R^{-1} (y - H(x)) + (x - x_b)^T P_b^{-1} (x - x_b) \right],
$$

which quantifies both the misfit between modelled and observed fluxes, and the misfit between a
priori and optimised parameters. $x$ is the vector of unknown parameters, $x_b$ the vector of background
(i.e., here, prior) parameter values, $H(x)$ the model output, $y$ the vector of observed fluxes, while $P_s$
and $R$ are the prior covariance matrices of parameter errors and observation errors, respectively.

The cost function is iteratively minimized with the gradient-based algorithm L-BFGS-B, which
allows prescribing boundaries for each variable to optimise (Byrd et al., 1995). At each iteration, the
gradient of the cost function $J(x)$ is computed with respect to all parameters, mostly using the
Tangent Linear (TL) model of ORCHIDEE generated with the automatic differentiator tool TAF
(Transformation of Algorithms in Fortran, see (Giering et al., 2005)). Exceptions concern two
phenological parameters, $K_{\text{pheno,crit}}$ and $c_{\text{Tsenes}}$ (see Table 1), where the threshold functions prevent the
use of a linear approximation. In these cases we use a finite-difference approach with prescribed
perturbation steps respectively equal to 4% and 2% of the allowed variation range. The recent work
of (Santaren et al., 2013) with the same ecosystem model highlighted the risk of converging
towards a local minimum within a site-specific variational optimization. In our case, preliminary
tests within three PFTs (tropical and temperate evergreen broadleaf forests, and temperate
deciduous broadleaf forests) allowed us to verify that the convergence of our multi-site approach
barely depends on the choice of the first-guess values assigned to the optimised parameters.
However, such robustness is not guaranteed with the site-specific approach, and potential
convergence issues are discussed in the results section.

Once the cost function reaches the minimum, the posterior parameter error variance/covariance
matrix $P_s$ is explicitly calculated from the prior error covariance matrices ($P_b$ and $R$) and the
Jacobian of the model $H$ at the minimum of the cost function ($H_x$), using the linearity assumption (Tarantola, 2005):

\[
P_a = \left[ H_x^\top R^{-1} H_x + P_b \right]^{-1}.
\]

(2)

The prior parameter error covariance matrix $P_b$ is diagonal as prior uncertainties are supposed to be uncorrelated between parameters. The prior standard deviation for each parameter is equal to 1/6 of the range between lower and higher boundaries. The latter have been carefully specified following the physical and empirical expertise of the ORCHIDEE modelers, based on literature reviews or databases (such as TRY, (Kattge et al., 2011)).

In the prior observation error covariance matrix $R$, we include both the random error on the measurements and the model error, the latter stemming from missing/inadequate process representation in the structural equations of the ecosystem model. Although the measurements error is known not to be constant (e.g. (Richardson et al., 2008)), a previous study using the ORCHIDEE model suggested that the model component dominates the observation error budget (Kuppel et al., 2013). The variances in $R$ are chosen constant at a given site for each type of data (NEE and LE), equal to the mean square difference between the prior model and the observations. We also choose for simplicity to keep $R$ diagonal, based on the rapid decline of the model error autocorrelation beyond the first lag day (Kuppel et al., 2013).

### 2.3 Assimilated eddy covariance flux data

We use the eddy covariance data provided by 78 flux towers of the FLUXNET global network (Baldocchi, 2008), representative of seven of the 12 vegetated PFTs defined in the ORCHIDEE model (supplementary Table S2). All the sites of a given dominant ecosystem are located in the same geographical hemisphere, which makes seasonal analyses easier. These observations derive from standard flux data processing methodologies (correction, gap-filling and partitioning) of the La Thuile dataset (Papale, 2006). From the large amount of available site-years in this dataset, our selection was driven by several requirements, the first of these being a minimum vegetation cover of 70% by the dominant PFT within each tower footprint, based on site-level information. Then were discarded the sites where measurements show a significant disagreement with the prior simulation outputs, as it suggests strong model structural deficiencies that make the parameter optimization pointless. Lastly, we selected at each site the longest data segment of consecutive years without gaps larger than a few weeks. Where measurements of the ground heat flux ($G$) were available, the monthly energy balance was closed with a correction factor then
half-hourly-interpolated and applied to the latent heat (LE) and sensible heat (usually called H) fluxes, according to the Bowen ratio technique (Twine et al., 2000). The half-hourly, gap-filled measured fluxes of net ecosystem exchange (NEE) and LE are then used to compute daily means. We chose to assimilate daily-averaged observations and not half hourly measurements so as to focus the optimization on time scales ranging from seasonal to annual variations, and to take advantage of the rapidly-decreasing autocorrelation of gap-filled half-hourly fluxes (Lasslop et al., 2008). In order not to give too much weight to data estimated from gap-filling as compared to measured data, each daily observation error is inflated by a factor $1+0.5k$, where $k$ is the daily fraction of half-hourly data estimated from gap-filling. We also checked that the gaps still remaining after the gap-filling were distributed evenly over the course of the day. The individual days with more than 20% of these “ultimate” gaps were not included in the assimilation.

The eddy covariance data are compared to the simulated fluxes in terms of RMSD and bias. In addition, for the six non-tropical PFTs we use a curve fitting procedure (composed of a polynome of degree 2 and four harmonics) to decompose the fluxes into their trends and mean seasonal cycles following (Thoning et al., 1989). The detrended smooth seasonal cycle is used to estimate the ratio between the average annual amplitude of the simulated and observed fluxes, as well as a model phase coefficient defined as

$$C_{phase} = 1 - \frac{|e_{sim} - e_{obs}| + |b_{sim} - b_{obs}|}{e_{obs} - b_{obs}}$$

Here, $b_i$ and $e_i$ are respectively defined as the days when the detrended smooth curve crosses the zero line. In tropical evergreen broadleaf forests, the phase and amplitude diagnostics presented above are not applied, due to the lack of a marked seasonal cycle. Instead, the predictive power of the simulations is evaluated using the Nash-Sutcliffe model efficiency coefficient (Nash and Sutcliffe, 1970):

$$NSE = 1 - \frac{\sum (F_{sim}^t - F_{obs}^t)^2}{\sum (F_{obs}^t - \bar{F}_{obs})^2},$$

where $F_{sim}^t$ is the value of the simulated or observed flux at the time step $t$, and $\bar{F}_{obs}$ the mean observed flux.

2.4 Evaluation tools
The model is evaluated at the sites using the two components of NEE: the gross primary productivity (GPP) and the ecosystem respiration rate (R\textsubscript{eco}), both estimated via the flux-partitioning method described in (Reichstein et al., 2005). This method extrapolates nighttime measurement of NEE, representing nighttime R\textsubscript{eco}, into daytime R\textsubscript{eco} using a short-term-calibrated temperature response function. GPP is then derived as the difference between R\textsubscript{eco} and NEE. We acknowledge that GPP and R\textsubscript{eco} are not fully independent data (with respect to the assimilated NEE) and are essentially model-derived estimates somewhat conditional on our underlying assumptions, and it will be kept in mind during the analysis.

Additionally, measurements of the Normalized Difference Vegetation Index (NDVI) made by the MODIS instrument are used to evaluate the simulated phenology at the global scale. From 2000 to 2010, the calculated reflectances (from measured irradiances) have been corrected for atmospheric absorption and scattering (Vermote et al., 2002) and directional effects (Vermote et al., 2009) in order to obtain a daily NDVI product with a 5-km spatial resolution. Observations contaminated with snow cover were removed from the analysis using MODIS' quality filter, and we discarded NDVI observations below 0.2 in order to minimize the impact of bare soil reflectance. Spatial averaging is used to match the ERA-Interim resolution (0.72° x 0.72°) used for the global scale simulations. Because it is directly derived from surface reflectances, we preferred NDVI to other satellite products such as FAPAR or LAI, the latter requiring intermediate processing steps usually involving radiative transfer models, and thus possibly adding uncertainty to the retrieved data (Garrigues et al., 2008). Following (Maignan et al., 2011), we then calculate the Pearson correlation factor between the times series of measured NDVI and the Fraction of Absorbed Photosynthetically Active Radiation (FAPAR) modelled by ORCHIDEE, at the weekly time scale during the period 2000-2010. FAPAR has been estimated from modelled LAI with a simple Beer’s law:

\[
FAPAR = 1 - \exp(-0.5 \times \text{LAI})
\]  

The link between simulations and measurements is made by spatially averaging the latter to reach the resolution of the vegetation model (i.e. that of the ERA-Interim forcing). For each of the seven PFTs considered, we restrict our correlation computation to the model boxes where the dominant PFT’s cover fraction exceeds 50% and where both NDVI and FAPAR time-series exhibit a visible seasonal cycle (i.e. with a standard deviation larger than 0.04).

Lastly, the simulated global NEE fluxes are output at the daily timescale and spatially averaged from the ERA-Interim grid (0.72°x0.72°) to a 2.5°x3.75° resolution (latitude, longitude). The LMDz atmospheric transport model (Hourdin et al., 2006) was used at this resolution to convert these terrestrial fluxes into monthly atmospheric CO\textsubscript{2} concentrations, during the period 1989 to
In order to complete the carbon balance at the planetary scale, we also transport the global oceanic and fossil net carbon fluxes respectively taken from a climatology (Takahashi et al., 2009) and from the EDGAR database (http://edgar.jrc.ec.europa.eu). The contribution of biomass burning is neglected, because re-growth of burnt vegetation is not accounted for in this version of ORCHIDEE, and so are the evasion of CO2 from aquatic bodies and emissions from harvested wood and agricultural products. The transported fluxes are evaluated using 53 smoothed record of atmospheric CO2 concentrations ($C_{\text{CO2}}$) over the globe (supplementary Table S3) (GLOBALVIEW-CO2, 2013). As the optimization of the initial soil carbon content cannot be spatially extrapolated for global simulations (see sect. 2.1), the modelled trend of $C_{\text{CO2}}$ is not evaluated. Rather, we focus on the seasonal analysis and use the curve-fitting procedures of (Thoning et al., 1989) to extract the detrended seasonal signal of $C_{\text{CO2}}$. In addition, we identify the contributions of 11 sub-continental regions to the simulated atmospheric CO2 concentration at each station by independently transporting the fluxes from each following area: boreal North America, temperate North America, tropical America, South America, Europe, northern Africa, southern Africa, boreal Asia, temperate Asia, tropical Asia, and Australia (e.g., Fig. 1 in (Gurney et al., 2003)). The simulated interannual variability of the $C_{\text{CO2}}$ is evaluated using the model-data RMSD of monthly anomaly, from the detrended smooth seasonal signal calculated above:

$$C_{\text{CO2,anom}} = C_{\text{CO2,month}} - \left\langle C_{\text{CO2,month}} \right\rangle_{\text{allyears}} ,$$

where $\left\langle C_{\text{CO2,month}} \right\rangle_{\text{allyears}}$ is the all-time average, for each month of the year.

### Results & discussion

#### 3.1 Site-level simulation of carbon and water fluxes

Figure 1 shows the average corrections brought by the optimization to the modelled NEE fluxes (with negative values meaning carbon uptake), grouped by dominant PFT (see acronyms in Table 1), in terms of RMSD and bias between simulations and measured data, also showing the PFT-averaged mean seasonal cycles. The largest reductions of model-data RMSD are found in temperate and boreal broadleaf forests (TempEBF, TempDBF and BorDBF), where the two optimization scenarios (single- and multi-site) decrease the misfit by more than 25% compared with the prior (unoptimized) model. In temperate needleleaf forests (TempENF) and C3 grasslands (C3grass), the RMSD reduction exceeds 30% for single-site optimizations, but the corresponding multi-site sets of parameters reduce this value to less than 20%. The improvements are less significant in tropical evergreen broadleaf forests (TropEBF) and boreal evergreen needleleaf forests (BorENF), where the reductions of misfit is between 9 and 15%. Figure 1B shows that the
NEE is on average overestimated by the prior model for all PFTs. This feature is even more striking in ecosystems which are marked sinks of carbon (according to the average measured carbon balance, not shown), here tropical and temperate forests. This positive bias is an artifact from the model initialization procedure, which brings each simulated site to a near equilibrium (see sect. 2.1). It is significantly corrected by the optimization, notably via the scaling of the initial carbon pool content at each site (parameter $K_{soilC}$ in Table 1), one consequence being a clear reduction of the respiration during the winter of temperate and boreal ecosystems and grasslands sites in agreement with the measured data (Fig. 1C).

Figure 2 shows that the simulation of the latent heat flux (LE) is overall less improved by the optimizations than that of the net carbon flux, keeping however in mind the problem of energy balance closure discussed in sect. 2.3. The reduction of RMSD is the highest on average at TempDBF sites with values 24% below the prior value, while decreases of 15 to 19% are found at TempEBF and BorENF sites. The effect of the optimization is the weakest on average at sites located in TempENF and C3grass ecosystems. These weaker performances regarding LE flux indicate that the energy and water cycles in the ORCHIDEE model involve other relevant parameters not optimised here, and possibly that the structural equations bear a significant error. Notably, we include in the optimization only one parameter that directly controls the soil evaporation ($Z_0\overheight$, see Table 1), and there is for example no constraint on the calculation of the surface temperature, a key component of the energy balance.

At the seasonal scale, Fig. 3A shows that large reductions (in relative value) of the simulated mean seasonal NEE amplitude are found in boreal evergreen needleleaf and deciduous broadleaf forests and C3 grasslands. The average correction is somewhat exaggerated in the two former cases and relatively accurate in the latter case. Conversely, the seasonal NEE variations are consistently amplified by the optimization in temperate evergreen needleleaf and broadleaf forests. However, the averaged model-data phasing is only weakly modified for the five aforementioned PFTs, with the exception of the site-specific improvements at TempENF and C3grass sites. Besides, considering the mild correction of the model-data biases in BorENF, BorDBF and C3grass (Fig. 1B), one can deduce that most of the reduction of RMSD discussed earlier is for these three PFTs due to an improvement of the simulated NEE amplitude after the optimization.

In temperate deciduous broadleaf forests, the simulated pattern of NEE is chiefly improved via a better phased seasonal cycle, as shown by the increased phase score, which was already close to one before optimization. An earlier study at a similar set of sites of the same PFT showed that the optimization scheme tends to correct the overall prior model overestimation of the growing season
length (Kuppel et al., 2012). On the other hand, the simulated seasonal amplitude of NEE is barely changed after optimization, as the corrected flux overestimations in winter and summer tend to cancel out, with a PFT-averaged seasonal amplitude remaining smaller than that of the observed data (Figs. 1C and 3).

Regarding the latent heat flux, Fig. 3B shows that the optimization has generally a weaker effect on the simulated LE average phase and amplitude than in the case of NEE. In most cases the correction brought by the optimization barely affects the modelled phase, but improves the seasonal amplitude. We notice that the LE seasonal cycle is most often flattened as compared to the prior model in agreement with the observations, except for the inconsistent amplification at TempEBF sites and the over-reduction after the site-specific optimization in C3 grasslands. The weak phase correction might be related to the soil evaporation component of the latent heat flux, on which the optimization has a limited leverage as mentioned earlier in this section, while the transpiration rate is tightly linked to GPP. It would also explain the generally lower phase coefficient in deciduous ecosystems (Fig. 3), where soil evaporation is a potentially significant component of LE during leaf onset and senescence.

Besides, applying the Nash-Sutcliffe model efficiency coefficient (NSE, see Eq. 4) to all sites shows that TropEBF is the only PFT studied here where the PFT-averaged value of this metric remains below zero after optimization for both fluxes, with $N_{\text{SE}_{\text{NEE}}}=[-2.77, -1.99, -1.83]$ and $N_{\text{SE}_{\text{LE}}}=[-0.64, -0.35, -0.52]$ in prior, multi-site and site-specific cases, respectively (other PFT values not shown). It means that after optimization the model-data mean square error is still larger than the variance of the observations, or, in other words, that the observed mean is on average a better predictor than the model outputs. Figure 1 shows that for TropEBF the prior model simulates an unobserved increase of NEE from sink to source around July, and the simultaneous decrease of LE (Fig. 2) points towards an unrealistic simulated drought stress during this period of the year, the driest at most sites of this PFT. The optimization barely corrects the NEE variations during the dry season, although a more realistic LE flux is simulated after the multi-site optimization. An earlier optimization study at a site of the same PFT highlighted the need for a much deeper soil water reservoir along with a more linear root profile than that parameterized in the prior model, in order to account for the ability of tropical evergreen forests to maintain high photosynthesis and transpiration during the dry season (Verbeeck et al., 2011). Our multi-site parameterization of the processes dealing with soil water availability goes in that direction, with values of soil water depth, root profile and water stress coefficient respectively adjusted from 2 to $2.38 \pm 0.065$ m, from 0.8 to $0.72 \pm 0.095$ m$^{-1}$ and from 6 to $6.5 \pm 1.06$ (Table 1). These corrections from the prior parameterization remain however insufficient, as shown by the poorly realistic optimised seasonal
cycle of NEE in Fig. 1. On the other hand, (Verbeeck et al., 2011) also pointed at the structural inconsistency in the standard ORCHIDEE model for tropical evergreen forests: the phenological scheme notably neglects the leaf renewal at the transition between wet and dry season (Chave et al., 2010) and the hydric stress calculation ignores the role of groundwater (Miguez-Macho and Fan, 2012), while these mechanisms possibly explain the high subsequent photosynthesis and transpiration rates often observed (Weirdt et al., 2012). Concerning the LE flux, the optimization brings somewhat limited, yet consistent changes, while the reduction of daily uncertainty is modest, indicating a poor level of constraint by the observations used. It suggests either significant errors in the model equations, or that relevant, poorly known parameters, have not been considered.

3.2 Single-site versus multi-site

It can be noticed in Figs. 1, 2 and 3 that there is a general consistency across PFTs between RMSD reductions introduced by multi-site and site-specific optimizations, with some exceptions in TempENF and most notably C3grass where the average site-specific RMSD reduction is twice as large for NEE, while there is almost no average multi-site RMSD decrease for LE. Although the large number of sites selected for this last PFT and the associated inter-site variability calls for prudence when considering average seasonal flux variations, it is worth noting that C3 grasslands are here the only PFT generically spanning such a diversity of climates. The reported discrepancy might thus indicate a need for additional classes of C3 grasslands in the model, at least with a climatic regionalization and ideally taking also into account pedologic conditions and management practices.

More generally, one would expect better efficiency from a site-specific scheme than with a multi-site approach, given that grouping sites with different characteristics introduces conflicting constraints on the model equations, along with the fact that the RMSD is the criterion used in the optimization procedure (as the prior covariance matrix in the cost function of Eq. (1) is chosen diagonal, see sect. 2.2). It is true most of the time, except notably for NEE in boreal deciduous broadleaf forests and LE at TropEBF, TempEBF and BorENF sites where the multi-site optimization results on average in larger RMSD decreases than the site-specific approach. In these cases, Figs. 1 and 2 show that it stems from unchanged local RMSD after the site-specific optimization at a few sites of these particular PFTs. As found by (Santaren et al., 2013), it may point to a failure of the single-site inversion algorithm to converge towards the global minimum of the cost function, possibly due to the presence of local minima. Our hypothesis is that the corresponding multi-site cost functions avoid this pitfall because they are made more regular by the larger amount of simultaneous constraints on the parameters, “smoothing out” some of the
problematic local minimums. Preliminary multi-site optimization tests, using a few tens of random starting points, support this hypothesis, and further investigations will be needed to evaluate if this behavior is valid for all PFTs. Indeed, we acknowledge some uncertainty regarding whether or not the optimised sets of parameters correspond to the very minimum of the cost function, as the efficiency of the variational optimization approach employed is conditional on a reasonable compliance with the linearity hypothesis.

3.3 Site-scale uncertainty

In addition to improving the agreement between modelled and measured fluxes, the optimization procedure is also useful to reduce the total uncertainty associated with the modelled output variables at each site, defined as:

\[ \sigma_{\text{total}} = \sqrt{\sigma^2_{\text{observations}} + \sigma^2_{\text{parameters}}} \]  

(7)

\( \sigma_{\text{total}} \) represents the summed contribution of two errors arising in the observation space: the measurements error and the error of the equations of the model (see sect. 2.2). It is not directly altered through parameter optimization, although the model component may in principle vary with the parameter values. Following (Desroziers et al., 2005), \( \sigma_{\text{total}} \) is diagnosed at each site as the square root of the covariance between the time series of prior and posterior flux residuals (model minus observations). \( \sigma_{\text{parameters}} \) is the parameter error contribution to the simulated fluxes, calculated at each site, before optimization, as the average daily standard deviation of the projection in observation space of the prior error covariance matrix \( P_b \), using the model’s Jacobian matrix \( H \), based on the definitions of sect 2.2. The same is done after optimization, respectively using \( P_a \) and \( H_\infty \).

Figure 4 reports the average value of \( \sigma_{\text{total}} \) for simulated daily NEE and LE, showing individual sites values and the corresponding PFT means as in Figs. 1 and 2. The reduction of the total NEE uncertainty varies from one PFT to another, ranging from 6% in tropical evergreen broadleaf forests to 33% in boreal evergreen needleleaf forests. As \( \sigma_{\text{total}} \) is reduced by 65 to 95% (not shown), we deduce from Eq. (7) that the weak relative decrease of \( \sigma_{\text{total}} \) indicates a dominance of the observation error in the total uncertainty budget. This is for example consistent with the reported inaccuracies in the model structure for TropEBF ecosystems discussed in the previous section.

Regarding the LE flux, the mild changes from prior to posterior uncertainty means that we might face a potentially large observation error component (model + measurements) – the latter being insensitive to parameter optimization, see sect. 2.3 – and overall that little statistical information has been gained from the optimization of the selected water cycle parameters.
Besides, one can notice that the posterior uncertainties are always slightly lower for multi-site optimization than with the site-specific approach, which is consistent with the fact that the number of assimilated data is larger in the former case than in the latter. Finally, we also found that the optimization suppresses at each site much of the temporal correlation of the flux error, which are large in the prior ORCHIDEE model (see for instance the time correlogram in the Fig. 1 of (Kuppel et al., 2013)). It results in a large decrease of the total yearly uncertainty from the prior model for all PFTs, by 77 to 86% and 43 to 80% for simulated NEE and LE flux, respectively (not shown).

3.4 Simulated GPP and respiration

Figure 5 shows the mean seasonal cycle, averaged over each PFT, for the gross carbon fluxes: photosynthesis (GPP, Fig. 5A) and ecosystem respiration ($R_{eco}$, Fig. 5B). The “observed” values are estimates based on a partition of the measured NEE (see sect. 2.4). These gross carbon fluxes have not been used as constraints in the optimization procedure, but are useful as indicators of the model performance. One can first notice that the average increases of GPP at TropEBF and TempEBF sites are responsible for the NEE decrease observed in Fig. 1. It is worth noting that the results reported in Fig. 5 also confirm the inability of the model to simulate a sustained high photosynthesis rate during the dry season at TropEBF sites (see Sect. 3.1), while this feature appears in the observations estimates. At TempENF sites, the remarkable adjustment of the NEE cycle primarily derives from a reduced $R_{eco}$ at the peak of the growing season. Both GPP and $R_{eco}$ are consistently decreased in boreal forests and C3 grasslands sites, although the reduction is still lower than what would be needed to match the estimates. In addition, because the respiration rate is the sole reducing component in winter and because the photosynthesis rate is more largely decreased than $R_{eco}$ during the growing season, the net result is the reduction of the seasonal amplitude of NEE for these three PFTs. Finally there is a large, yet insufficient, decrease of $R_{eco}$ after the optimization in temperate deciduous broadleaf forests, notably related to the scaling of the initial carbon pool content (sect 3.1 and (Kuppel et al., 2012)), while GPP is less drastically reduced, in close agreement with the observations. This evaluation at each site with gross carbon fluxes shows that the optimization procedure is able to provide a set of parameters which improves the simulation of both assimilation and respiration processes in the ORCHIDEE model for six out of the seven PFTs considered here, suggesting a partial distinction of both gross contributions from the constraint provided by the net carbon flux.

3.5 Global-scale evaluation

One of the objectives of assimilating flux data from a large number of sites, spanning a wide range of ecosystems, is to identify generic sets of parameters that improve the simulation of carbon
and water balance at the regional-to-global scale. Indeed, there is no guarantee that a set of parameters improving the simulations at an ensemble of individual sites sharing broadly common biogeochemical and biophysical characteristics, but with a limited spatial footprint, will also be beneficial for simulations at much larger scales. In this context, global simulations allow evaluation of how the constraint of eddy covariance data is propagated from one spatial scale to another, and how transferable the optimised parameterization is from grouped in situ optimizations to gridded simulations.

3.5.1 Seasonality of atmospheric CO$_2$ concentrations

Regarding the simulated mean seasonal cycle of atmospheric C$_{CO2}$, the optimised set of parameters yields a median reduction of the model-data RMSD of 5.2%. Among the 53 samples locations used in this study, there is a significant improvement at 27 of them with a RMSD decrease larger than 5%, a notable degradation at 20 sites with a RMSD increase larger than 5%, and less than a 5% shift at the remaining 6 locations. In addition, a latitudinal clustering can be identified, as a large median improvement by 42.2% (RMSD-wise) is found at the 3 northernmost sites (Alert, Ny-Alesund, and Barrow) and by 33.5% at the 18 locations of the Southern Hemisphere, while there is a median degradation by 5.6% in the rest of the Northern Hemisphere.

Figure 6 shows the mean seasonal cycle of the simulated C$_{CO2}$, compared to the extended record at three locations, one in each of the latitudinal areas defined above: Alert, South Pole, and Mauna Loa, respectively. We note that using the optimised parameters sets tends to reduce the seasonal amplitude of C$_{CO2}$, with in the Northern Hemisphere an earlier phasing for the “breathing of the biosphere”. At station Alert, there is a significant adjustment of the simulated seasonal cycle, when changing from the default to the multi-site parameterization of the ORCHIDEE model. This correction chiefly benefits the seasonal amplitude, which is decreased and becomes remarkably close to that observed. The analysis of the contribution of the 11 sub-continental regions in the simulated atmospheric signal (see sect. 2.4), grouped in Fig. 6D in larger regions, indicates that the major terrestrial contribution to this result are changes in C$_{CO2}$ due to the boreal Northern Hemisphere fluxes. It is consistent with the decrease of the NEE seasonal amplitude produced by the multi-site optimization at sites in boreal evergreen needleleaf forests, boreal deciduous broadleaf forests and C3 grasslands (Figs 1C and 3A), dominant in this region. Separate global simulations using optimised parameterization for one PFT at a time show that the degraded phasing at Alert produced by the multi-site approach in Fig. 6A mainly stems from the contributions of BorENF and C3 grasslands ecosystems (not shown). While a mild multi-site phase deterioration from the prior parameterization is found at the site level in BorENF (Fig. 3A), it is not the case for
C3 grassland and it may thus question the representativeness of the flux measurements sites used, with respect to high-latitudes ecosystems in general.

At station South Pole, the model-data fit is also mostly enhanced after the optimization by a significant decrease of the seasonal amplitude of \(C_{\text{CO}_2}\), which is more than twice as large in the prior simulation as in the measured data. Besides, the “regionalized” analysis indicates that the corrections are primarily due to the reduced seasonal amplitude of \(C_{\text{CO}_2}\) components from temperate South America and southern Africa, and contributions from the boreal Northern Hemisphere are also noticeable (not shown). We therefore deduce that the optimization of C3 grasslands parameters is the most influential factor explaining the improved simulation of \(C_{\text{CO}_2}\) at this station, but also that the influence of boreal needleleaf evergreen forests cannot be neglected here.

The reduction of the simulated cycle amplitude is too strong at station Mauna Loa, which, combined with earlier seasonality, leads to a poorer model-data fit after optimization. The remote location of Mauna Loa (north Pacific) makes it sensitive to influences from most of the Northern Hemisphere. We find that the main drivers of the simulated correction are flattened, earlier \(C_{\text{CO}_2}\) variations in temperate and boreal regions of North America and Asia, and Europe (not shown). These results thus reflect part of the reduction of the seasonal amplitude of NEE in boreal ecosystems and C3 grasslands noticed at Alert and South Pole stations. The degraded model-data fit between optimised \(C_{\text{CO}_2}\) and data from Mauna Loa also suggests that the boreal correction of NEE amplitude is too strong or insufficiently compensated at large scale by the amplification of the seasonal cycle at temperate latitudes visible at TempENF and TempDBF sites (Figs. 1C and 3A).

Finally, using the multi-site-optimised model overall brings a small improvement of the modelled interannual variability of \(C_{\text{CO}_2}\), with a median reduction of 3.9% for the RMSD between modelled and measured monthly anomaly (not shown). Forty-five locations, out of the 53 used in this study, display an improvement with RMSD decreases up to 27%, while at the remaining 8 sites the degradation of the simulated interannual variability remains small with RMSD increases always smaller than 1.5% (not shown). These results suggest that despite the relative shortness (one to three years) of most of the FluxNet datasets selected to optimise the ORCHIDEE model, the diversity of the covered weather situations gives a modest, yet consistent source of information to better reproduce interannual variations of carbon fluxes at the global scale.

### 3.5.2 Global scale phenology index

Figure 7 reports for each optimised PFT the correlation factor between weekly values of measured NDVI and modelled FAPAR during the period 2000-2010 (see sect. 2.4), for both the
prior and optimised model. There is no result for BorDBF whose vegetation fraction never exceeds 40% in our case. All remaining six PFTs exhibit a higher median correlation factor when using the multi-site parameterization, which means that the modelled leaf seasonal cycle better matches the global scale observations. This median improvement seems to accurately reflect the overall trend for TempDBF-, BorENF- and C3grass-dominated pixels, while a larger inter-pixel variability is introduced in the case of temperate evergreen forests. The improved modelled seasonality is related to the more accurately simulated GPP at FluxNet sites after multi-site optimization, the latter being in turn partly driven by the improvement of the seasonal variations of simulated LAI. The dominant feature seems to be a shorter growing season length for TempDBF, which is consistent with the site-level simulations of GPP seasonality for this PFT (Fig. 5A), and an earlier beginning of the growing season for C3 grasses (not shown). Note that this improvement also explains most of the increased correlation factors in temperate and boreal evergreen forests, since these PFTs do not present a climate-driven leaf phenology in the current formulation of the ORCHIDEE model. Consequently, deciduous and herbaceous PFTs are the only significant contributors to the seasonal cycle at such a coarse resolution, even when these ecosystems are secondary and/or the understory within an evergreen-dominated forest. Lastly, the score for TropEBF remains poor because the model wrongly simulates the leaf renewal and the hydric stress during the dry season, as discussed in Sects. 3.1 and 3.4.

3.6 Limitations of the current approach: summary and discussion

The limitations to our model-data fusion method highlighted throughout the results section are of three kinds, somewhat interlocked: 1) within the limits of the model structure, 2) how adequate the chosen set of optimised parameters was and 3) how close to the optimal values the optimization algorithm tuned these parameters.

Taking these items in reverse order, we first acknowledge that using a variational optimization algorithm with a model with non-linearities might expose to miss the global minimum of the cost function, and indeed a few obvious convergence failures cases have been found for some single-site optimizations in TropEBF, TempENF, and boreal forests. Some functions of the ORCHIDEE model could potentially be linearized to generate a more accurate tangent linear model—and to advantageously avoid to use finite-differences for some phenological parameters (see Sect. 2.1)—, while remaining coherent with the model's philosophy. It might imply a demanding effort of model recoding, but it has already been done for another LSM (Knorr et al., 2010). Alternatively, stochastic optimization approaches could yield better convergence, as they can circumvent the linearity constraint. While a single-site model-data fusion study with the same LSM showed
advantageous results for a genetic Monte-Carlo-based technique over its variational counterpart (Santaren et al., 2013), no major difference was found by (Ziehn et al., 2012) between Monte-Carlo and gradient-based approaches when optimizing a simpler LSM with atmospheric CO$_2$ observations. In the case of a multi-site optimization efforts, we suggest that the cost function “smoothing” discussed in Sect. 3.2 could make the convergence efficiency less sensitive to the choice of the minimization approach, while keeping in mind the much lower computational time required in the variational case.

Second, the number of optimised parameters remains somewhat modest as compared to the diversity of processes modelled in the ORCHIDEE model. Our choice was partly driven by a model sensitivity criterion, while the actual leverage of an optimised parameter on model outputs also depends on the uncertainty associated to this very parameter (Dietze et al., 2014). It can result in selecting some parameters that are already reasonably well known but that have medium-to-high model sensitivity and thus with low overall leverage, while poorly known parameters with mild-to-low model sensitivity could have a comparatively higher value for the optimization. In addition, as our focus was on the carbon cycle, only a few water-and-energy-related parameters were considered. Notably, the correction of LE partly benefited from that of NEE via transpiration, but the soil evaporation optimization was neglected despite being a significant -and debated- player of the terrestrial water cycle (Schlesinger and Jasechko, 2014).

The third hindering factor to simulating carbon and water fluxes close to their true value is the “observation error”, i.e. the uncertainty arising from the simplification needed to make ecosystem functioning fit within explicit equations plus the error made associated to the measurements, fluxes and meteorological forcing included. Although this error is rarely quantified in model-data fusion efforts, model-data fit analyses and uncertainty budgets showed in this study that the relative importance of this observation error greatly varies from one PFT to another –and is potentially dominated by the model error component in the case simulations at flux towers sites (Kuppel et al., 2013). It is the highest in tropical evergreen broadleaf forests, where parameter optimization will likely be of limited help until a more realistic phenological scheme is implemented. Regarding the simulations of LE in general, the small amount of related parameters optimised makes it difficult to assess to which extent the nearly-unchanged flux uncertainty comes from the parameter scarcity or structural inaccuracies in the model, stressing again the need for a better consideration of water and energy cycles together with that of carbon in future model-data fusion efforts.

4 Conclusions
Generalizing the results of (Kuppel et al., 2012) across ecosystems, this study has shown that a significant degree of improvement is introduced to the simulation of carbon and water fluxes, through a generic optimization approach with in situ measurements of NEE and LE fluxes, relying on the traditional PFT classification used in many land surface models. At the global scale, this optimization method allows first a better simulation of the seasonal foliar cover. Second, the multi-site parameter set has a significant leverage upon the simulated seasonality of atmospheric $C_{CO2}$, with performances somewhat spatially heterogeneous and depending on the PFT considered, while a small, yet encouraging improvement of the simulated interannuality of $C_{CO2}$ is found. The remaining discrepancies in $C_{CO2}$ indicate that combining atmospheric CO2 concentration and a larger number of flux towers observations, in a Carbon Cycle multi-Data Assimilation Systems (CCDASs, e.g., (Kaminski et al., 2013)), would be beneficial. Using more site-years of flux data will also allow a systematic in situ evaluation of the multi-site parameters across time periods, regions and climate regimes by separating training sites from evaluation sites. Such procedure was not applied in this study due to the small number of sites for some PFTs, but remains essential to test a LSM used for climate projections. More generally, we suggest that the assimilation of FluxNet data should be considered as a baseline for the development of multi-data assimilation systems where more complementary data streams are combined. In particular, daytime and nighttime NEE could replace the daily values used here, and adding measurements of leaf area index, soil respiration fluxes (e.g. chamber measurements), biomass and litter/soil carbon pools, would help better separating the processes and constraining environmental drivers, as would a simultaneous parameter optimization of both over- and understory PFT fractions. The FluxNet multi-site approach can also be used to characterize the structural, parametric and total uncertainties associated with the simulated annual biospheric carbon balance at regional-to-global scales, and to compare it with 1) the discrepancies of results between global ecosystem models (Sitch et al., 2008), and 2) the error carried by the terrestrial carbon fluxes estimated via inverse modeling with atmospheric transport models (e.g., (Chevallier et al., 2010)). The underlying problem is thus to evaluate what would be gained from simultaneously assimilating various data streams covering different spatial and temporal scales into a terrestrial ecosystem model, and how the PFT classification should be refined to maximize this improvement. In parallel, by using a diagonal prior covariance matrix for parameter error, within a same PFT and across PFTs, we implicitly assumed that all parameters could in principle be efficiently corrected as independent random distributions. It ignores the fact that a covariance structure interlinking the optimised parameterization would be necessary to translate the interconnectedness of ecophysiological processes within a given PFT. For instance, the allocation of carbon within the plant reservoirs depends on specific allometric relations and on photosynthesis rate; these relations would need to be embedded in the prior parameter error.
covariance matrix. Additionally, the influence of nearby individuals of other PFTs (e.g., the 
understory) should be accounted for when correcting parameters of a given PFT. Together with a 
simultaneous optimization of several PFTs, building standard spatialized parameter covariance 
tables from databases of plant traits and soil characteristics (e.g., (Kattge et al., 2011)) and 
'preliminary' posterior multi-site parameter error covariance matrices (e.g., supplementary material 
of (Kuppel et al., 2012)) might soon become necessary to consistently apply model-data fusion to 
more sophisticated mechanistic ecosystem models.

5 Code availability

The source code of the data assimilation system is available at 
https://pypi.python.org/pypi/ORCHISM. Regarding the ORCHIDEE vegetation model, the source 
files of the Tag version 1.9.5.2 used for this study can be obtained upon request (see 
http://labex.ipsl.fr/orchidee/index.php/contact), while the associated documentation can be found at 
https://forge.ipsl.jussieu.fr/orchidee/wiki/Documentation. Note that the tangent linear version of the 
ORCHIDEE model has been generated using a commercial software (TAF, see sect. 2.2). For this 
reason, only the ‘forward’ version of the ORCHIDEE model is available for sharing, to which only 
the finite differences method is employed for parameter optimization. Finally, the source code of the 
LMDz atmospheric transport model can be found at http://web.lmd.jussieu.fr/trac.

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Gianelle, A. Raschi, H. Kondo, A.J. Dolman, T. Johansson, M. Nilsson, A. Lindroth, A. Grelle, J. 
Hollinger, R. Matamala, W.C. Oechel, J. Hadley, B. Law, L. Gu, A. Noormets, P. Blanken, G. 
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References


Giering, R., Kaminski, T. and Slawig, T.: Generating efficient derivative code with TAF: adjoint and


Table 1. Parameters of ORCHIDEE optimised in this study. The prior values are given for each PFT, and multi-site posterior values are in bold font. A hyphen means that the parameter is not optimised, spinup that the spinup value is taken, and site that the posterior value is site-specific.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
<th>Plant functional type&lt;sup&gt;a&lt;/sup&gt;</th>
<th>Trop</th>
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<th>Temp</th>
<th>Temp</th>
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<th>Bor</th>
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<td>EBF</td>
<td>DBF</td>
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<td>DBF</td>
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<td>45</td>
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<td>Ball-Berry slope</td>
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<td>9</td>
<td>9</td>
<td>9</td>
<td>9</td>
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<tr>
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<td>8.841</td>
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<td>7.714</td>
<td>9.970</td>
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<td>Minimum fraction of LAI$_{\text{MAX}}$ to stop carbohydrate use</td>
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<td>5.000</td>
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<td>Multiplicative factor for growing season start threshold</td>
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<td>L$_{\text{agecrit}}$</td>
<td>Critical age for leaves (days)</td>
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<td>$LAI_{\text{init}}$</td>
<td>Initial LAI (m$^2$.m$^{-2}$)</td>
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<td>5</td>
<td>4.5</td>
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<tr>
<td>$f_{\text{stressh}}$</td>
<td>Parameter reducing the hydric limitation of photosynthesis</td>
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<td>$Dpu_{\text{cste}}$</td>
<td>Total depth of the soil water reservoir (m)</td>
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<td>6.507</td>
<td>7.146</td>
<td>7.135</td>
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<td>4.881</td>
<td>5.505</td>
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<td></td>
<td></td>
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<td></td>
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<td></td>
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<tr>
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<td>Slope of the temperature dependence</td>
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<td>0.16</td>
<td>0.16</td>
<td>0.16</td>
<td>0.16</td>
<td>0.16</td>
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<td>0.094</td>
<td>0.185</td>
<td>0.178</td>
<td>0.174</td>
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<sup>a</sup> PFT = Plant functional type.
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<th>Parameter</th>
<th>Description</th>
<th>Values</th>
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<td>GR_{frac}</td>
<td>Fraction of biomass available for growth</td>
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<tr>
<td>respiration</td>
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<tr>
<td><strong>Maintenance respiration</strong></td>
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<td><strong>Heterotrophic respiration</strong></td>
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<tr>
<td>GR_{frac}</td>
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<tr>
<td>respiration</td>
<td></td>
<td></td>
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<tr>
<td>K_{soilC}</td>
<td>Scaling factor for all initial soil carbon stocks after spinup</td>
<td>site</td>
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<td>Q_{10}</td>
<td>Factor of the temperature control function</td>
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<td><strong>Decomposition</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>h_{crit,litter}</td>
<td>Total litter height (m)</td>
<td>0.08</td>
</tr>
<tr>
<td>Z_{decomp}</td>
<td>Factor of the exponential profile of soil temperature and moisture</td>
<td>0.2</td>
</tr>
<tr>
<td><strong>Energy balance</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>K_{albedo,veg}</td>
<td>Multiplicative factor of surface albedo</td>
<td>1</td>
</tr>
<tr>
<td>Z_{0,overheight}</td>
<td>Reference roughness length (m)</td>
<td>0.0625</td>
</tr>
</tbody>
</table>

* TropEBF = tropical evergreen broadleaf forest; TempENF = temperate evergreen needleleaf forest; TempEBF = temperate evergreen broadleaf forest; TempDBF = temperate deciduous broadleaf forest; BorENF = boreal evergreen needleleaf forest; BorDBF = boreal deciduous broadleaf forest; C3grass = C3 grassland.
Figure 1. Model-data (A) RMSD and (B) bias for the daily NEE time series at each site (filled circles), grouped and averaged by PFT (horizontal bars), in three cases: prior model (green), multi-site optimization (blue) and single-site optimization (orange). (C) PFT-averaged mean seasonal cycle of NEE, for the training observations (black) and the three aforementioned cases, smoothed with a 15-day-moving-average window.
Figure 2. Model-data (A) RMSD and (B) bias for the daily LE time series at each site (filled circles), grouped and averaged by PFT (horizontal bars), in three cases: prior model (green), multi-site optimization (blue) and single-site optimization (orange). (C) PFT-averaged mean seasonal cycle of LE, for the training observations (black) and the three aforementioned cases, smoothed with a 15-day-moving-average window.
Figure 3. PFT-averaged model phase coefficient versus model-to-data amplitude ratio, for the detrended smooth seasonal cycles of (A) NEE and (B) LE fluxes. Simulations using prior parameters (green) are compared to multi-site (blue) and single-site (orange) optimizations, with the measured reference indicated by the intersection of the dashed lines.

Figure 4. Uncertainty of simulated daily (A) NEE and (B) LE fluxes. For each PFT, the horizontal lines give the average of the individual site values (filled circles), in three cases: prior model (green), multi-site optimization (blue) and single-site optimization (orange).
Figure 5. PFT-averaged mean seasonal cycles of (A) the photosynthetic carbon flux and (B) the respiration flux, smoothed with a 15-day-moving-average window. The simulations using prior (green), single-site (orange) and multi-site (blue) parameterizations are compared to the evaluative observation-derived flux estimates (black).
Figure 6. Detrended mean seasonal cycle of the atmospheric CO$_2$ concentrations at (A) Alert, (B) South Pole and (C) Mauna Loa locations during the 1989-2009 period: the optimization-independent concentrations records (black) are compared to simulations where the biospheric contribution is calculated using the ORCHIDEE model with default (green) and multi-site (blue) parameterization, with the model-data RMSD given between brackets. (D) Regional contributions to the mean seasonal cycle simulated at Alert.
Figure 7. Correlation factor between weekly time series of modelled FAPAR and independent measurements of NDVI, for the 2000-2010 period. The results are grouped using the dominant PFT at each pixel, for global simulations with default (green) and multi-site parameterization (blue). The central horizontal bar indicates the median value, the top and bottom of the boxes correspond to the first and last quartile, and the 5- and 95-percentile are given by the 'error bars'.

1 TropEBF (n=785) 2 TempENF (n=291) 3 TempEBF (n=39) 4 TempDBF (n=206) 5 BorENF (n=1360) 6 C3grass (n=5745)