Dear reviewer,

thank you for reviewing our paper and your comments.

**Minor corrections**

- Page 1, line 3: There is already “often” in the sentence. “some climate models often use” makes no sense.

- Page 1, line 6: Done.

- Page 1, line 10: It is not clear what you want us to change here. That is just some words repeated from the sentence.

- Page 1, line 11: What do you mean by “more or duplicating”? What do you want us to change here?

- Page 1, line 13: Done.

- Page 1, line 15–16: What do you mean by “bit consuming”? What do you want us to change here?

- Page 1, line 20: “of ATLAS” is correct. ATLAS contains other modules than the chemistry module.

- Page 1, line 25: Done.

- Page 2, line 15: Done.

- Page 2, line 23–26: I don’t see how to put that message into two sentences.

- Page 2, line 31: Done.

- Page 3, Table 1: Done.

- Page 5, line 3: Changed citation to the discussion paper.

- Page 5, line 17: Done.

- Page 7, line 10: Has been published as discussion paper in the meantime (see above).

- Page 8, line 15: What do you mean by “more important”? It is necessary to use these quantities in both hemispheres in the model formulation.

- Figure 17–18: Increased font size.
Dear reviewer,
thank you for reviewing our paper and your helpful comments.

Comments

- Abstract: As the author and maintainer of ATLAS, I prefer to give ATLAS just as a name and not as an acronym. SWIFT originally meant “Semi-empirical Weighted Iterative Fit Technique”, but just this fitting approach has been discarded in the current version. Therefore, I would suggest to use SWIFT just as a name here and not to use the outdated acronym.

- P1, L3: We think it is justifiable to stay at the current formulation. Looking e.g. at Eyring et al., 2013, only 9 out of 46 CMIP5 models have an interactive ozone scheme, of which several are CCMs and don’t use a fast parameterization like Cariolle. The current formulation does not want to imply that there are no GCMs with fast ozone chemistry.

- P2, L1: We have extended the discussion in the introduction and mentioned that there is a growing number of models incorporating stratospheric ozone chemistry. We have also added a reference for CCMVal and a reference for an overview paper of the ozone schemes in the CMIP5 models (Eyring et al., 2010, 2013).

- P2, L30: In fact, there exists an independent Extrapolar SWIFT model. Unfortunately, this was not mentioned in the manuscript. This omission was caused by a delay of the submission of this paper by about 2 years and not checking for this again. While the extrapolar model was not ready for use 2 years ago, we are in the process of publishing a paper on the Extrapolar SWIFT model in the moment. We have now changed the name of the model from “SWIFT” to “Polar SWIFT” in the manuscript, and added a reference to the Extrapolar SWIFT model in the introduction. Added “(in combination with the Extrapolar SWIFT model)” to the sentence at P2, L30.

- P5, L5: The cited paper and this manuscript were submitted as companion papers at the same time. Hence, we were not able to give a reference at the time of submission. We have now added the reference to the discussion paper in Atmos. Chem. Phys.

- P5, L20: We have rounded the values in the text now, but kept the exact values in the Table 3. We give all information in the paper that is needed to implement the SWIFT model, which includes the exact pressure values.

- P7: We agree that it does not hurt to give the full equation with the covariance here. It is however not really relevant for the discussion in the paper, in particular since it cannot be applied to the more complex equations 8/10/11/12. We checked in all cases where it is mentioned in the text how well \( \langle X_1 X_2 \rangle \) and \( \langle X_1 \rangle \langle X_2 \rangle \) agree, but did not use a formal
criterion for the allowed magnitude of the “intensity of segregation”. In all cases, the values for $\langle X_1 X_2 \rangle$ and $\langle X_1 \rangle \langle X_2 \rangle$ were either almost identical or largely different, so that the decision was clear without a formal criterion. As discussed in the text, we then judged the quality of the approximation by looking at the goodness of the fit of the parameterized term to the term obtained from ATLAS.

- P7, L26: Changed.
- P11, L11: Changed to “the spatial distributions of ClO and NO are very different”.
- P29, L4: Rephrased to “Both the magnitude and the interannual variability of the MLS measurements are reproduced well by the SWIFT model runs in the northern hemisphere. The interannual variability is larger and reproduced better in the northern hemisphere than in the southern hemisphere.”
Update of the **Polar** SWIFT model for polar stratospheric ozone loss (**Polar** SWIFT version 2)

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¹Alfred Wegener Institute for Polar and Marine Research, Potsdam, Germany

*Correspondence to:* I. Wohltmann (ingo.wohltmann@awi.de)

**Abstract.** The **Polar** SWIFT model is a fast scheme for calculating the chemistry of stratospheric ozone depletion in polar winter. It is intended for use in Global Climate Models (GCMs) and Earth System Models (ESMs) to enable the simulation of interactions between the ozone layer and climate. So far, climate models often use prescribed ozone fields, since a full stratospheric chemistry scheme is computationally very expensive. **Polar** SWIFT is based on a set of coupled differential equations, which simulate the polar vortex averaged mixing ratios of the key species involved in polar ozone depletion on a given vertical level. These species are $\text{O}_3$, chemically active chlorine ($\text{ClO}_x$), $\text{HCl}$, $\text{ClONO}_2$ and $\text{HNO}_3$. The only external input parameters that drive the model are the fraction of the polar vortex in sunlight and the fraction of the polar vortex below the temperatures necessary for the formation of polar stratospheric clouds. Here, we present an update of the **Polar** SWIFT model introducing several improvements over the original model formulation. In particular, the model is now trained on vortex averaged reaction rates of the ATLAS Chemistry and Transport Model, which enables a detailed look at single processes and an independent validation of the different parameterizations for the single processes contained in the differential equations. The training of the original **Polar** SWIFT model was based on fitting complete model runs to satellite observations and did not allow this. A revised formulation of the system of differential equations is developed, which closely fits vortex averaged reaction rates from ATLAS that represent the main chemical processes influencing ozone. In addition, a parameterization for the $\text{HNO}_3$ change by denitrification is included. The rates of change of the concentrations of the chemical species of the **Polar** SWIFT model are purely chemical rates of change in the new version, while the rates of change in the original **Polar** SWIFT version included a transport effect caused by the original training on satellite data. Hence, the new version allows for an implementation into climate models in combination with an existing stratospheric transport scheme. Finally, the model is now formulated on several vertical levels encompassing the vertical range in which polar ozone depletion is observed. The results of the **Polar** SWIFT model are validated with independent MLS satellite observations and the results of the original detailed chemistry model of ATLAS.

1 **Introduction**

The importance of interactions between climate change and the ozone layer has long been recognized (e.g. Thompson and Solomon, 2002; Rex et al., 2006; Nowack et al., 2015). Hence, it is desirable to account for these interactions in climate models. Usually, this is accomplished by coupling a full stratospheric chemistry module to a Global Climate Model (GCM)
in models referred to as Chemistry Climate Models (CCMs) (e.g. Eyring et al., 2010). Since this approach is computationally very expensive, ozone is usually prescribed in the type of climate models that are used in the Intergovernmental Panel on Climate Change (IPCC) reports (IPCC, 2013), where long-term runs and multiple scenario runs are required. There is however a growing number of models incorporating interactive ozone chemistry (e.g. Eyring et al., 2013), either by using simplified fast schemes like the Cariolle scheme (Cariolle and Déqué, 1986; Cariolle and Teyssèdre, 2007) or Linoz scheme (McLinden et al., 2000; Hsu and Prather, 2009) or by using CCMs. The fast stratospheric chemistry scheme Polar SWIFT was developed to enable interactions between climate and the polar ozone layer in this type of climate model-time-critical applications of climate models and to improve quality and performance compared to existing schemes. The original version of the Polar SWIFT model was presented in Rex et al. (2014). Here, we present an update of the Polar SWIFT model. The Polar SWIFT model is complemented by an independent model for calculating extrapolar stratospheric ozone chemistry (Extrapolar SWIFT), which is presented in a separate publication (Kreyling et al., 2017, see also Kreyling, 2016).

Polar SWIFT simulates the evolution of the polar vortex averaged mixing ratios of six key species that are involved in polar ozone depletion by solving a set of coupled differential equations for these species on a given vertical level (Rex et al., 2014). The model includes four prognostic variables (ClONO₂, HCl, total HNO₃, and O₃) and two diagnostic variables (ClOₓ = ClO + 2 Cl₂O₂ and HNO₃ in the gas phase). The differential equations contain several free fit parameters, which were fitted to match satellite observations in the old model version (see Rex et al., 2014) and which are fitted to vortex averaged reaction rates from the ATLAS Chemistry and Transport Model in the new version.

Polar SWIFT is driven by time series of two external input parameters. The first is the fraction of the polar vortex area that is cold enough to allow the formation of polar stratospheric clouds (Fractional Area of PSCs, abbreviated FAP) and the second is the 24 h average of the fraction of the polar vortex that is exposed to sunlight (Fractional Area of Sunlight, abbreviated FAS). A system of four differential equations is formulated that describes the chemical rate of change of the prognostic variables as a function of only FAP, FAS and the mixing ratios of the species only (the term for HNO₃ also includes the rate of change caused by denitrification). The equations comprise terms for the most important chemical processes involved in polar ozone depletion, e.g. the effect of the catalytic ClO dimer cycle.

Since only a single value per vertical level and species is used in Polar SWIFT, which is constant over the polar vortex, and since the model is able to use a large time step of typically one day and a simple integration scheme, it is possible to calculate the ozone evolution of a complete winter in a few seconds.

The original system of equations is shown in Table 1 and Table 2, together with the new model formulation, which is presented in more detail in Section 3. Table 3 contains the fitted coefficients.

In contrast to other fast ozone schemes for climate models like the Cariolle scheme (Cariolle and Déqué, 1986; Cariolle and Teyssèdre, 2007) or Linoz (McLinden et al., 2000; Hsu and Prather, 2009), which were originally designed to model only extrapolar ozone, the Polar SWIFT model is not based on a single linear differential equation based on a Taylor series expansion, but on a set of coupled non-linear differential equations representing the main processes changing polar ozone. This has the advantage that the model is not required to be linear and can cope with the non-linearities occurring in polar ozone chemistry. Together with the fact that the model equations are closely based on the real atmospheric processes, we
Table 1. List of equations used in the original and new Polar SWIFT version. Terms A to L are specified in Table 2. \( \langle \ldots \rangle \) is the vortex mean, \( z \) is a free fit parameter. FAP and FAPs are fractions of the polar vortex below different threshold temperatures for the formation of PSCs (see Section 2.5).

<table>
<thead>
<tr>
<th>Prognostic equations (original)</th>
<th>Prognostic equations (new)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \frac{d \langle [O_3] \rangle}{dt} = -D )</td>
<td>( \frac{d \langle [O_3] \rangle}{dt} = -D ) unchanged</td>
</tr>
<tr>
<td>( \frac{d \langle [ClONO_2] \rangle}{dt} = B - A - G - H )</td>
<td>( \frac{d \langle [ClONO_2] \rangle}{dt} = B - A - H )</td>
</tr>
<tr>
<td>( \frac{d \langle [HCl] \rangle}{dt} = C + F - A )</td>
<td>( \frac{d \langle [HCl] \rangle}{dt} = C_1 + C_2 + F - A - L - K )</td>
</tr>
<tr>
<td>( \frac{d \langle [HNO_3] \rangle}{dt} = -E )</td>
<td>( \frac{d \langle [HNO_3] \rangle}{dt} = -E ) unchanged</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Diagnostic equations (original)</th>
<th>Diagnostic equations (new)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \langle [ClO_x] \rangle = \langle [Cl_y] \rangle - \langle [HCl] \rangle - \langle [ClONO_2] \rangle )</td>
<td>( \langle [ClO_x] \rangle = \langle [Cl_y] \rangle - \langle [HCl] \rangle - \langle [ClONO_2] \rangle ) unchanged</td>
</tr>
<tr>
<td>( \langle [HNO_3]_g \rangle = \langle [HNO_3] \rangle \cdot (1 - \text{FAP}) ) + ( z \cdot \langle [HNO_3] \rangle \cdot \text{FAP} )</td>
<td>( \langle [HNO_3]_g \rangle = \langle [HNO_3] \rangle \cdot (1 - \text{FAP}_s) ) + ( z \cdot \langle [HNO_3] \rangle \cdot \text{FAP}_s )</td>
</tr>
</tbody>
</table>

expect our model to behave more realistically than a Taylor series based approach, especially in conditions far away from the current atmospheric mean state. The Polar SWIFT model is therefore able to represent ozone-climate interactions during climate change (in combination with the Extrapolar SWIFT model).

The newest version of the Cariolle scheme (Cariolle and Teyssèdre, 2007) also includes a parameterization for heterogeneous polar chemistry, but is based on a quite different approach using a temperature tracer. The newest version of the Linoz scheme (Hsu and Prather, 2009) uses a very simple parameterization based on an earlier version of the Cariolle scheme (Cariolle et al., 1990).

In Section 2, an overview of the new Polar SWIFT model is given and the fitting procedure is described in detail. In Section 3, we present the new differential equations for the four prognostic variables of the model (HCl, ClONO2, HNO3 and O3), and the fits to the modeled reaction rates. In Section 4, the Polar SWIFT model is validated by comparison to MLS satellite data and the original detailed chemistry model of ATLAS. Section 5 contains the conclusions.

2 Overview of the changes in the new Polar SWIFT version

2.1 Revision of the system of differential equations based on ATLAS results

The original formulation of the system of differential equations is revised based on results of the Lagrangian Chemistry and Transport Model ATLAS. A detailed description of the model can be found in Wohltmann and Rex (2009) and Wohltmann...
Table 2. List of the terms used in the differential equations in the original and new Polar SWIFT version. \((\ldots)\) is the vortex mean. \(a\) to \(l\) and \(y\) are free fit parameters. FAP and \(\text{FAP}_s\) are fractions of the polar vortex below different threshold temperatures for the formation of PSCs (see Section 2.5). FAS is the fraction of the vortex exposed to sunlight (see Section 2.5).

<table>
<thead>
<tr>
<th>Expression (original)</th>
<th>Expression (new)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Term A: Heterogeneous reaction (\text{HCl} + \text{ClONO}_2)</strong></td>
<td></td>
</tr>
<tr>
<td>(a \cdot \langle [\text{ClONO}_2] \rangle \cdot \langle [\text{HNO}_3] \rangle \cdot \text{FAP} ) (\langle [\text{HCl}] \rangle &gt; 27, \text{ppt})</td>
<td>(a \cdot \langle [\text{ClONO}_2] \rangle \cdot \langle [\text{HNO}_3] \rangle^{2/3} \cdot \text{FAP} ) (\langle [\text{HCl}] \rangle &gt; 1, \text{ppt})</td>
</tr>
<tr>
<td>(a \cdot \langle [\text{HCl}] \rangle \cdot \langle [\text{ClONO}_2] \rangle \cdot \langle [\text{HNO}_3] \rangle \cdot \text{FAP} ) (\langle [\text{HCl}] \rangle &lt; 27, \text{ppt})</td>
<td>(a \cdot \langle [\text{HCl}] \rangle \cdot \langle [\text{ClONO}_2] \rangle \cdot \langle [\text{HNO}_3] \rangle^{2/3} \cdot \text{FAP} ) (\langle [\text{HCl}] \rangle &lt; 1, \text{ppt})</td>
</tr>
<tr>
<td><strong>Term B (and G in the original model): Net change by (\text{ClONO}_2) gas phase reactions</strong></td>
<td></td>
</tr>
<tr>
<td>(b \cdot \langle [\text{HNO}_3]_g \rangle \cdot \text{FAS} ) (\langle [\text{ClO}_x] \rangle &gt; 135, \text{ppt})</td>
<td>(b \cdot \langle [\text{ClO}_x] \rangle \cdot \langle [\text{HNO}_3]_g \rangle \cdot \text{FAS} ) (B) and (G) replaced by (B)</td>
</tr>
<tr>
<td>(b \cdot \langle [\text{ClO}_x] \rangle \cdot \langle [\text{HNO}_3]_g \rangle \cdot \text{FAS} ) (\langle [\text{ClO}_x] \rangle &lt; 135, \text{ppt})</td>
<td></td>
</tr>
<tr>
<td><strong>Term C: Reaction (\text{Cl} + \text{CH}_4)</strong></td>
<td></td>
</tr>
<tr>
<td>(c \cdot \langle [\text{ClO}_x] \rangle / \langle [\text{O}_3] \rangle \cdot \text{FAS} )</td>
<td>(c_1 \cdot \langle [\text{ClO}_x] \rangle / \langle [\text{O}_3] \rangle \cdot \text{FAS}^2 + )</td>
</tr>
<tr>
<td>(c_2 \cdot \langle [\text{ClONO}_2] \rangle / \langle [\text{O}_3] \rangle \cdot \text{FAS}^3 )</td>
<td></td>
</tr>
<tr>
<td><strong>Term D: Ozone depletion by (\text{ClO}) dimer and (\text{ClO–BrO}) cycle</strong></td>
<td></td>
</tr>
<tr>
<td>(d \cdot \langle [\text{ClO}_x] \rangle \cdot \text{FAS} )</td>
<td>(d \cdot \langle [\text{ClO}_x] \rangle \cdot \text{FAS} ) unchanged</td>
</tr>
<tr>
<td><strong>Term E: Denitrification</strong></td>
<td></td>
</tr>
<tr>
<td>(e \cdot \langle [\text{HNO}_3] \rangle \cdot \text{max}((\text{FAP} - y), 0) )</td>
<td>(e \cdot \langle [\text{HNO}_3] \rangle \cdot \text{FAP}_s )</td>
</tr>
<tr>
<td><strong>Term F: Reaction (\text{ClO} + \text{OH})</strong></td>
<td></td>
</tr>
<tr>
<td>(f \cdot \langle [\text{ClO}_x] \rangle \cdot \text{FAS}^2 ) Arctic</td>
<td>(f \cdot \langle [\text{ClO}_x] \rangle \cdot \text{FAS}^2 )</td>
</tr>
<tr>
<td>(0.25f \cdot \langle [\text{ClO}_x] \rangle \cdot \text{FAS}^2 ) Antarctic</td>
<td></td>
</tr>
<tr>
<td><strong>Term H: Heterogeneous reaction (\text{ClONO}_2 + \text{H}_2\text{O})</strong></td>
<td></td>
</tr>
<tr>
<td>(h \cdot \langle [\text{ClONO}_2] \rangle \cdot \text{max}((\text{FAP} - y), 0) )</td>
<td>(h \cdot \langle [\text{ClONO}_2] \rangle \cdot \langle [\text{HNO}_3] \rangle^{2/3} \cdot \text{FAP} )</td>
</tr>
<tr>
<td><strong>Term K: Reaction (\text{HCl} + \text{OH})</strong></td>
<td></td>
</tr>
<tr>
<td>(k \cdot \langle [\text{HCl}] \rangle \cdot \text{FAS}^2 )</td>
<td></td>
</tr>
<tr>
<td><strong>Term L: Heterogeneous reaction (\text{HOCl} + \text{HCl})</strong></td>
<td></td>
</tr>
<tr>
<td>(l \cdot \langle [\text{HOCl}] \rangle \cdot \langle [\text{HCl}] \rangle \cdot \langle [\text{HNO}_3] \rangle^{2/3} \cdot \text{FAP} )</td>
<td>(\langle [\text{HOCl}] \rangle = \langle [\text{ClO}_x] \rangle \cdot \text{FAS} )</td>
</tr>
</tbody>
</table>
et al. (2010). The model includes a gas phase stratospheric chemistry module, heterogeneous chemistry on polar stratospheric clouds and a particle-based Lagrangian denitrification module. The chemistry module comprises 47 active species and more than 180 reactions. Absorption cross sections and rate coefficients are taken from recent JPL recommendations (Sander et al., 2011).

Vortex averaged mixing ratios of all model species and vortex averaged reaction rates of all modeled reactions are used to identify the important processes involved in polar ozone depletion, and to identify the relevant reactions, their relative importance and their time evolution. Results are based on two model runs for the southern hemispheric winters 2006 and 2011 (1 May to 30 November) and two model runs for the northern hemispheric winters 2004/2005 (15 November to 31 March) and 2009/2010 (1 December to 31 March). The identification of the most important processes and reactions is discussed in a companion paper (Wohltmann et al., 2017). The present paper will concentrate on the technical aspects, like the fitting procedure and finding appropriate parameterizations for the processes.

Details of the model setup are described in Wohltmann et al. (2017) and we will only repeat the most important facts here. Model runs are driven by meteorological data from the ECMWF ERA Interim reanalysis (Dee et al., 2011). Chemical species are mainly initialized by MLS satellite data (Waters et al., 2006). The initial horizontal model resolution is 150 km. The runs use a potential temperature coordinate and vertical motion is driven by total diabatic heating rates from ERA Interim. In addition to the binary background aerosol, the model simulates three types of Polar Stratospheric Clouds, that is supercooled ternary HNO$_3$/H$_2$SO$_4$/H$_2$O solutions (STS), solid clouds composed of nitric acid trihydrate (NAT), and solid ice clouds. The number density of NAT particles in the runs is set to 0.1 cm$^{-3}$, the number density of ice particles is set to 0.01 cm$^{-3}$ and the number density of the ternary solution droplets to 10 cm$^{-3}$. A supersaturation of HNO$_3$ over NAT of 10 (corresponding to about 3 K supercooling) is assumed to be necessary for the formation of the NAT particles. For ice particles, a supersaturation of 0.35 is assumed. The settings for the polar stratospheric clouds largely favor the formation of liquid clouds (binary liquids and STS clouds) over the formation of NAT clouds and activation of chlorine predominantly occurs in liquid clouds in the model runs.

2.2 Vertical levels

Fitted parameters for the differential equations from Table 1 and Table 2 are obtained for 5 pressure levels, which roughly encompass the vertical range in which ozone depletion is observed. The choice of the pressure levels is guided by the pressure levels of the EMAC (ECHAM/MESSy Atmospheric Chemistry) model (39 level version) in this altitude range (Jöckel et al., 2006; Roeckner et al., 2006), which is the first model in which Polar SWIFT is implemented. The levels used are 69.6611 hPa, 54.0364 hPa, 41.5987 hPa, 31.7739 hPa and 24.0747 hPa (see Table 3 for exact values). Results at intermediate levels can either be obtained by vertical interpolation of the fitted parameters or by running the Polar SWIFT model at the two enclosing levels and averaging the results. In the following, we will only show results from the 54 hPa level in the figures for clarity.
2.3 Fit of the free parameters to ATLAS reaction rates

The fitting procedure for the original model version was based on fitting the time series of species mixing ratios of a complete Polar SWIFT model run to satellite observations at a given vertical level. This approach has several disadvantages:

- The fit is non-linear, since the solution of the differential equations depends non-linearly on the fit parameters. This requires a non-linear fitting algorithm, which may only find a local and not a global minimum for the residuum of the fit.

- In addition, the fitting procedure is iterative and is computationally more expensive than a linear fit. Every iteration of the fitting procedure requires a complete run of the Polar SWIFT model.

- Transport effects are implicitly included. The rate of change of the satellite data at a given level is the sum of the chemical rate of change and the rate of change by transport. Hence, the fit parameters include a transport effect. This effect is most pronounced for O₃, where the rates of chemical change and of change by subsidence in the polar vortex are comparable.

- Satellite data of the species that are fitted have to be available. For species like ClONO₂, the availability of measurements is limited.

Here, we employ a new method which avoids these disadvantages. We take advantage of the fact that all of the equations of the system of differential equations from Table 1 and Table 2 on a given vertical level are of the form

\[
\frac{d\langle X_n \rangle(t_i)}{dt} = c_{p_{n1}}f_{p_{n1}}(\langle X_1 \rangle(t_i), \ldots, \langle X_N \rangle(t_i), t_i) + \ldots + c_{p_{nM(n)}}f_{p_{nM(n)}}(\langle X_1 \rangle(t_i), \ldots, \langle X_N \rangle(t_i), t_i)
\] (1)

where \(\langle \ldots \rangle\) is the vortex average, \(\langle X_n \rangle\) is the vortex averaged mixing ratio of species \(n\) and \(N\) is the number of species \((n = 1, \ldots, N)\). The \(f_p(\ldots)\) are functions of the mixing ratios (and of fixed parameters like FAS and FAP) which represent the parameterizations for the different processes \(p = 1, \ldots, P\) introduced in Rex et al. (2014). The processes \(f_p\) are the terms \(A, B\) etc. in Table 1 and 2. The \(c_p\) are the associated fitted coefficients for each parameterization \((a, b\) etc. in Table 2). The \(p_{nm}\) assign a parameterization to a specific species \(n\) and the additive term \(m\) of that species. \(M(n)\) is the number of additive terms for species \(n\). Different \(p_{nm}\) are allowed to contain the same number (i.e. the same parameterization can be used for different species). The net chemical rate of change \(d\langle X_n \rangle(t_i)/dt\) for every species and all \(f_p(\ldots)\) terms can be obtained as fixed values from the ATLAS runs for a number of model time steps \(t_i\) \((i = 1, \ldots, T)\), since both the vortex averaged mixing ratios and the vortex averaged reaction rates are available from the ATLAS model. This gives a system of \(T \cdot N\) equations which can be solved for the \(c_p\). The system consists of simple linear equations for the \(c_p\), which can be solved by a least squares fit (since the number of equations \(T \cdot N\) is much larger than the number of coefficients \(P\), the system is overdetermined). Equations with different time steps \(t_i\) but the same species \(n\) are coupled since they contain the same \(c_p\). Additionally, equations with different species may also contain the same \(c_p\).
To simplify the fit further, we split the left-hand side into a sum of the rates of change that are caused by single chemical reactions

\[
\frac{d \langle X_n \rangle}{dt}(t_i) = \frac{d \langle X_n \rangle}{dt} \Big|_1(t_i) + \ldots + \frac{d \langle X_n \rangle}{dt} \Big|_{K(n)}(t_i)
\]  

(2)

where \( \frac{d \langle X_n \rangle}{dt} \Big|_k \) is the rate of change caused by the \( k \)th reaction changing species \( n \) in ATLAS, with \( K(n) \) the number of reactions changing species \( n \) \((k = 1, \ldots, K(n))\). In many cases, it is feasible to assign a single reaction (or a sum of a very few reactions) to one of the parameterizations \( f_p(\ldots) \) on the right hand side. This way, the system of differential equations decouples into many independent linear equations, which can simply be solved by fitting the \( c_p \) as a factor that scales the parameterization \( f_p(\ldots) \) to the rate of change of the corresponding chemical reaction:

\[
\frac{d \langle X_n \rangle}{dt} \Big|_k(t_i) = c_p f_p(\langle X_1 \rangle(t_i), \ldots, \langle X_N \rangle(t_i), t_i)
\]  

(3)

The time series of the northern hemispheric runs and of the southern hemispheric runs are concatenated and fitted at the same time to obtain one set of fit parameters valid for both hemispheres. This is done because the physical and chemical foundations are the same in both hemispheres and the same parameterizations can be used. Since the conditions in the northern and southern hemisphere cover a wide range of temperatures, this approach ensures that the model does respond correctly to changes in temperature, e.g. temperature trends caused by climate change.

### 2.4 Vortex averages

The vortex averaged mixing ratios of the species \( \langle X_n \rangle \) in the northern hemisphere are obtained by assuming that the vortex edge is situated at the 36 PVU contour of modified potential vorticity (PV) at all altitudes. Modified PV is calculated according to Lait (1994), with \( \theta_0 = 475 \) K. In the southern hemisphere, the vortex edge is assumed to be situated at the \(-36 \) PVU contour. Note that the vortex tracer criterion described in Wohltmann et al. (2017) is not applied here.

The air parcels of ATLAS that are inside the vortex are vertically binned into bins centered at the 5 pressure levels of Polar SWIFT to obtain the mixing ratios \( \langle X_n \rangle \) for these levels by averaging. The edges of the bins are in the middle between the Polar SWIFT levels (in the logarithm of pressure). ATLAS model output is available at 00 h UTC and 12 h UTC. Vortex means from 00 h UTC and 12 h UTC on a given day are averaged to obtain daily means. Vortex averaged reaction rates are calculated as 24 h averages over the diurnal cycle by the method described in Wohltmann et al. (2017).

Usually, it is easy to find a parameterization for the rate of a specified reaction or the mixing ratios of a chemical equilibrium if only looking at a given location inside the vortex (i.e. a reaction \( A + B \rightarrow C \) leads to the equation \( \frac{d[C]}{dt} = k[A][B] \) with [A] the mixing ratio of A and \( k \) the rate coefficient). However, problems arise if vortex averages are used. If we assume that either the mixing ratios of the species are sufficiently constant over the area of the vortex, or that the differential equations do only contain terms linear in the mixing ratios, we can use vortex averages. Care has to be taken if products of mixing ratios appear in the equations. If \( X_1 \) and \( X_2 \) are the mixing ratios of two species, the vortex average of the product is not necessarily the same as the product of the vortex averages (if their covariance is not zero)

\[
\langle X_1 X_2 \rangle \neq \langle X_1 \rangle \langle X_2 \rangle + \text{cov}(X_1, X_2)
\]  

(4)
There are several possibilities to cope with this problem. If at least one of the species is long-lived and constant over the vortex, approximate equality can be assumed. If both species are short-lived, the vortex can be divided into a sunlit part and a dark part, and two separate constant mixing ratios can have to be assumed in the sunlit and dark part.

However, we will see in the following that it is not possible in all cases to transform the original expression for the chemical reaction at a single location to an equivalent expression that only uses vortex averages. We use expressions that are empirically derived in these cases. Here, the quality of the approximation is assessed by the goodness of fit for the wide range of climate conditions observed in the training data set.

2.5 The external parameters FAP and FAS

The 24 h averaged fraction of the polar vortex in sunlight (FAS) and the fraction of the polar vortex below the formation temperature of polar stratospheric clouds (FAP) are calculated from the same ERA Interim data that is used for running the ATLAS model for consistency.

Two different FAP parameters are used in the new version of the Polar SWIFT model, which are called FAP and FAP_s. Evidence from modeling studies and observations suggests that a considerable part of chlorine activation occurs on clouds composed of liquid binary and supercooled ternary solutions (STS) and that nitric acid trihydrate (NAT) clouds only form when large supersaturations of more than 10 are reached (for a detailed discussion and references, see Wohltmann et al., 2013). By chance, the required supercooling of 3 K also corresponds roughly to the temperature at which binary liquid aerosols begin to take up HNO_3 in significant quantities and are transformed into ternary solutions, which increases the reaction rates on liquid aerosols significantly. Hence, we calculate the area of the polar vortex above a supersaturation of HNO_3 over NAT of 10 according to the equations of Hanson and Mauersberger (1988) and divide the values by the vortex area. This quantity is called FAP_s in the following. However, chlorine activation already sets in at higher temperatures than the NAT threshold temperature minus 3 K on the liquid aerosols, albeit with smaller rates. Hence, we also calculate a quantity called FAP by assuming no supersaturation. The decision to use FAP or FAP_s is based empirically on the quality of the fit for the single equations. A special case is the denitrification, which is based on sedimenting NAT particles in the ATLAS model and is parameterized with FAP_s.

For FAS, the area below a solar zenith angle of 90° inside the vortex is calculated and divided by the vortex area. To obtain a 24 h average, the polar vortex obtained from ERA Interim is assumed to be fixed for a virtual 24 h period. Then, the solar zenith angles are calculated for many intermediate time steps in this 24 hour period. The area below 90° solar zenith angle is calculated for each intermediate step. Finally, the results are averaged over the intermediate time steps.

3 The parameterizations

In the next sections, we present the new differential equations for the four prognostic variables of the model (HCl, ClONO_2, HNO_3 and O_3), and the fits to the modeled reaction rates. The terms f_p are indicated by upper case letters A, B, C, … in the
following, to comply with the notation in Rex et al. (2014). Mixing ratios of species are denoted by putting the name of the species into brackets, e.g. \([\text{HCl}]\) for the mixing ratio of HCl. \(\langle \ldots \rangle\) is the vortex mean again.

### 3.1 HCl

#### 3.1.1 Overview

The equation for HCl is changed from

\[
\frac{d}{dt} \langle [\text{HCl}] \rangle = C + F - A \tag{5}
\]

in the original model to

\[
\frac{d}{dt} \langle [\text{HCl}] \rangle = C_1 + C_2 + F - A - L - K \tag{6}
\]

in the new model. Term \(C\) of the original model and terms \(C_1\) and \(C_2\) of the new model represent the effect of the reaction

\[
\text{Cl} + \text{CH}_4 \rightarrow \text{HCl} + \text{CH}_3 \tag{R1}
\]

which is responsible for deactivation of Cl into HCl under ozone hole conditions in the southern hemisphere and is the main HCl production reaction in both hemispheres. In the new parameterization, we split term \(C\) into two terms \(C_1\) and \(C_2\) to account for two different Cl sources (\(\text{Cl}_2\text{O}_2\) photolysis and the \(\text{ClO} + \text{NO}\) reaction). The less important reaction

\[
\text{Cl} + \text{CH}_2\text{O} + \text{O}_2 \rightarrow \text{HCl} + \text{CO} + \text{HO}_2 \tag{R2}
\]

which also depends on Cl, is subsumed into term \(C\) in the new model. Term \(F\) represents the effect of the reaction of ClO with OH

\[
\text{ClO} + \text{OH} \rightarrow \text{HCl} + \text{O}_2 \tag{R3}
\]

which helps HCl reformation in both hemispheres. Term \(A\) accounts for the effect of the most important heterogeneous reaction activating chlorine

\[
\text{HCl} + \text{ClONO}_2 \rightarrow \text{Cl}_2 + \text{HNO}_3 \tag{R4}
\]

We introduce a new Term \(L\) for the heterogenous reaction

\[
\text{HOCl} + \text{HCl} \rightarrow \text{Cl}_2 + \text{H}_2\text{O} \tag{R5}
\]

which is responsible for a considerable part of the activation in the southern hemisphere and for a non-negligible part in the northern hemisphere. Another reaction that consumes HCl not included in the original model that turned out to be significant in late winter and spring is

\[
\text{HCl} + \text{OH} \rightarrow \text{H}_2\text{O} + \text{Cl} \tag{R6}
\]

which is considered by a new Term \(K\).
3.1.2 Term $C$

Term $C$ represents the effect of

$$\text{Cl} + \text{CH}_4 \rightarrow \text{HCl} + \text{CH}_3 \quad (R1)$$

This reaction is responsible for chlorine deactivation under ozone hole conditions and is the main production reaction of HCl in both hemispheres (Wohltmann et al., 2017). If we assume that CH$_4$ is sufficiently constant, the rate of production of HCl by this reaction is only proportional to Cl:

$$\left\langle \frac{d[HCl]}{dt} \right|_{R1} \sim \langle [\text{Cl}] \rangle \quad (7)$$

Term $C$ of the original model is split into two additive terms $C = C_1 + C_2$ in the new model. These two terms account for two different sources of Cl. Under sunlit conditions, Cl is mainly determined by two source reactions that produce Cl:

$$\text{Cl}_2\text{O}_2 + h\nu \rightarrow 2\text{Cl} + \text{O}_2 \quad (R7)$$

$$\text{ClO} + \text{NO} \rightarrow \text{Cl} + \text{NO}_2 \quad (R8)$$

and a reaction that removes Cl:

$$\text{Cl} + \text{O}_3 \rightarrow \text{ClO} + \text{O}_2 \quad (R9)$$

Reaction R7 is coupled to the catalytic ClO dimer cycle. It can be shown by using the equilibrium condition $d[\text{Cl}]/dt = 0$ that the mixing ratio of Cl under sunlit conditions is roughly approximated by

$$\langle [\text{Cl}] \rangle_{\text{day}} = \left( \frac{2k_{R7}[\text{Cl}_2\text{O}_2]}{k_{R9}[\text{O}_3]} \right)_{\text{day}} + \left( \frac{k_{R8}[\text{ClO}][\text{NO}]}{k_{R9}[\text{O}_3]} \right)_{\text{day}} \quad (8)$$

where $\langle \ldots \rangle_{\text{day}}$ is the average over the sunlit part of the vortex and the $k_R$ are the rate coefficients. The first term on the right side corresponds to Term $C$ for the Cl$_2$O$_2$ photolysis in the original model and to Term $C_1$ in the new model. The second term corresponds to the new Term $C_2$ for the ClO + NO reaction. Vortex averaged mixing ratios can be obtained by an area weighted average:

$$\langle [\text{Cl}] \rangle \approx \text{FAS} \cdot \langle [\text{Cl}] \rangle_{\text{day}} + (1 - \text{FAS}) \cdot \langle [\text{Cl}] \rangle_{\text{night}}$$

$$\approx \text{FAS} \cdot \langle [\text{Cl}] \rangle_{\text{day}} \quad (9)$$

under the assumption that there is no Cl at night.
Vortex averaged mixing ratio of Cl₂O₂ for the Arctic winter 2004/2005, the Antarctic winter 2006, the Arctic winter 2009/2010 and the Antarctic winter 2011 at 54 hPa (from left to right). Vortex average (solid blue) and parameterization for the mixing ratio by ⟨[ClOₓ]⟩(1 – FAS) (dashed blue) and average over sunlit part of vortex (solid magenta) and parameterization for the mixing ratio by ⟨[ClOₓ]⟩ (dashed magenta). Tick marks on the horizontal axis show start of months.

**Term C₁**

The vortex average of the photolysis coefficient $k_{R7}$ is assumed to be proportional to FAS. Figure 1 shows that $⟨[Cl₂O₂]⟩_{\text{day}}$ is proportional to $⟨[ClOₓ]⟩$ in good approximation, since a relatively constant fraction of ClOₓ is in the form of Cl₂O₂ during day in the covered time period. We assume that ozone is sufficiently constant over the vortex, so that $⟨[O₃]⟩_{\text{day}} = ⟨[O₃]⟩$ and that the division and the vortex mean can be interchanged. Hence, Term $C₁$ is parameterized similarly as the original term $C$:

$$C₁ = c₁ \cdot \frac{⟨[ClOₓ]⟩}{⟨[O₃]⟩} \cdot FAS^2$$

(10)

This is the original term multiplied by FAS. The two different FAS factors in the new model have their origin in the area weighted average and in the photolysis coefficient, respectively. The term $1/⟨[O₃]⟩$ makes sure that if ozone concentrations become low, reaction R9 of the ClO dimer cycle becomes less efficient and the ratio of Cl over ClO increases.

**Term C₂**

Term $C₂$ accounts for reaction R8 which produces Cl in large quantities in spring (Wohltmann et al., 2017) and was not considered in the original model. Looking at equation 8, it is tempting to model Term $C₂$ by assuming that:

$$\frac{⟨[ClO][NO]\rangle}{⟨[O₃]\rangle}$$

(11)

is equal to

$$\frac{⟨[ClO]⟩_{\text{day}}}{⟨[O₃]⟩_{\text{day}} \cdot ⟨[NO]⟩_{\text{day}}}$$

(12)
and then finding parameterizations for $\langle [\text{ClO}] \rangle_{\text{day}}, \langle [\text{NO}] \rangle_{\text{day}}$ and $\langle [\text{O}_3] \rangle_{\text{day}}$. Unfortunately, it turns out that this approximation is not valid, since the spatial distributions of ClO and NO are not equally distributed very different and

$$\langle [\text{ClO}][\text{NO}] \rangle_{\text{day}} \neq \langle [\text{ClO}] \rangle_{\text{day}} \langle [\text{NO}] \rangle_{\text{day}} \quad (13)$$

The reason is that there is an equilibrium between ClONO$_2$ on the one side and ClO and NO$_2$ on the other side, which limits the amount of ClO and NO$_2$ (and in turn NO) that can exist at the same location. ClONO$_2$ is to a good approximation in an equilibrium between

$$\text{ClONO}_2 + h\nu \rightarrow \text{Cl} + \text{NO}_3 \quad (R10)$$

$$\rightarrow \text{ClO} + \text{NO}_2 \quad (R11)$$

and

$$\text{ClO} + \text{NO}_2 + \text{M} \rightarrow \text{ClONO}_2 + \text{M} \quad (R12)$$

and the partitioning of NO$_x$ is governed, to a good approximation, by the equilibrium between

$$\text{O}_3 + \text{NO} \rightarrow \text{NO}_2 + \text{O}_2 \quad (R13)$$

$$\text{ClO} + \text{NO} \rightarrow \text{Cl} + \text{NO}_2 \quad (R8)$$

$$\text{NO}_2 + h\nu \rightarrow \text{NO} + \text{O} \quad (R14)$$

By using the equilibrium conditions $d[\text{NO}]/dt = 0$ and $d[\text{ClONO}_2]/dt = 0$, the product of ClO and NO can be expressed by

$$[\text{ClO}][\text{NO}] = \frac{(k_{R10} + k_{R11})k_{R14}[\text{ClONO}_2]}{k_{R12}(k_{R13}[\text{O}_3] + k_{R8}[\text{ClO}])} \quad (14)$$

Unfortunately, the vortex mean of this function can again not be replaced by this function formulated in terms of the vortex means $\langle [\text{ClONO}_2] \rangle$, $\langle [\text{O}_3] \rangle$ and $\langle [\text{ClO}_x] \rangle$.

That is, a formulation of Term $C_2$ which is quantitatively correct and only depends on the vortex means of the variables is not possible. It is only possible to find a parameterization that results in a good fit and takes into account some important properties of the above equations.

A very good fit for Term $C_2$ can be achieved by the parameterization

$$C_2 = c_2 \cdot \langle [\text{ClONO}_2] \rangle / \langle [\text{O}_3] \rangle \cdot \text{FAS}^3 \quad (15)$$

The three FAS factors take the involved photolysis reactions R10/R11 and R14 and the area weighted average into account. The dependence on ClONO$_2$ in Equation 14 is considered by multiplying by $\langle [\text{ClONO}_2] \rangle$. The shift of the equilibrium towards high Cl values for low O$_3$ values by the Cl + O$_3$ and NO + O$_3$ reactions is parameterized by dividing by $\langle [\text{O}_3] \rangle$. 

12
Figure 2. Fit of Term C for the Arctic winter 2004/2005, the Antarctic winter 2006, the Arctic winter 2009/2010 and the Antarctic winter 2011 at 54 hPa. Sum of the vortex averaged reaction rates modeled by ATLAS for the reactions Cl + CH\textsubscript{4} and Cl + CH\textsubscript{2}O\textsubscript{2} (blue), the fitted terms C\textsubscript{1} (orange) and C\textsubscript{2} (brown) and the sum C\textsubscript{1} + C\textsubscript{2} (red). Tick marks on the horizontal axis show start of months.

Table 3. Fit coefficients

<table>
<thead>
<tr>
<th>p [hPa]</th>
<th>69.66111</th>
<th>54.03643</th>
<th>41.59872</th>
<th>31.77399</th>
<th>24.07468</th>
<th>Scaling factor</th>
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<tr>
<td>a</td>
<td>7.986612</td>
<td>4.085210</td>
<td>2.846390</td>
<td>2.479554</td>
<td>1.963608</td>
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</tr>
<tr>
<td>b</td>
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<td>3.031378</td>
<td>2.740275</td>
<td>2.715443</td>
<td>3.770580</td>
<td>-10^7</td>
</tr>
<tr>
<td>c\textsubscript{1}</td>
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<td>0.836649</td>
<td>0.706846</td>
<td>0.716972</td>
<td>1.108429</td>
<td>-10^-6</td>
</tr>
<tr>
<td>c\textsubscript{2}</td>
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<td>6.386807</td>
<td>6.274739</td>
<td>5.244277</td>
<td>4.904797</td>
<td>-10^-7</td>
</tr>
<tr>
<td>d</td>
<td>8.884890</td>
<td>8.325397</td>
<td>7.646982</td>
<td>6.904189</td>
<td>6.515611</td>
<td>-10^1</td>
</tr>
<tr>
<td>e</td>
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<td>4.124637</td>
<td>4.285359</td>
<td>4.443291</td>
<td>3.918175</td>
<td>-10^-2</td>
</tr>
<tr>
<td>f</td>
<td>1.863004</td>
<td>1.817837</td>
<td>1.804207</td>
<td>1.940491</td>
<td>3.163943</td>
<td>-10^-1</td>
</tr>
<tr>
<td>h</td>
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<td>0.592115</td>
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<tr>
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<td>7.179308</td>
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</table>

The sum C\textsubscript{1} + C\textsubscript{2} is fitted to the sum of the modeled rates of the two reactions R1 and R2. R2 is a less important reaction that also depends on Cl. Figure 2 shows the sum of the reaction rates modeled by ATLAS (blue), the fitted term C = C\textsubscript{1} + C\textsubscript{2} (red) and the two components C\textsubscript{1} (orange) and C\textsubscript{2} (brown) at the second fitted pressure level (54 hPa). The fitted coefficients can be found in Table 3.
3.1.3 Term $F$

Term $F$ represents the effect of the reaction of ClO with OH

\[ \text{ClO} + \text{OH} \rightarrow \text{HCl} + \text{O}_2 \quad \text{(R3)} \]

which helps HCl formation in both hemispheres. The reaction starts to become important only in late winter, when sunlight comes back and OH and ClO are produced in photolytic reaction cycles. Since ClO$_x$ levels decrease in spring, it is only important for a relatively short period (February to March in the northern hemisphere, September to October in the southern hemisphere, Wohltmann et al., 2017). The rate of change of HCl by this reaction is given by the area weighted rate of change under sunlit conditions, since there is no OH and very little ClO at night

\[
\left\langle \frac{d[HCl]}{dt} \right\rangle_{\text{R3}} \approx \text{FAS} \cdot \left\langle \frac{d[HCl]}{dt} \right\rangle_{\text{day}}
\]

The rate of change during day can be expressed by

\[
\left\langle \frac{d[HCl]}{dt} \right\rangle_{\text{R3}}_{\text{day}} = \langle k_{R3}[\text{ClO}][\text{OH}] \rangle_{\text{day}}
\]

Contrary to the situation in the last section, the vortex average and the multiplication can be interchanged, to a good approximation, for ClO and OH

\[
\langle [\text{ClO}][\text{OH}] \rangle_{\text{day}} \approx \langle [\text{ClO}] \rangle_{\text{day}} \langle [\text{OH}] \rangle_{\text{day}}
\]

Hence, Term $F$ is parameterized by

\[
F = f \cdot \langle [\text{ClO}] \rangle_{\text{day}} \cdot \langle [\text{OH}] \rangle_{\text{day}} \cdot \text{FAS}
\]

with the FAS factor from the area weighting. The mixing ratio $\langle [\text{ClO}] \rangle_{\text{day}}$ is modeled by assuming proportionality to ClO$_x$

\[
\langle [\text{ClO}] \rangle_{\text{day}} \sim \langle [\text{ClO}_x] \rangle
\]

since a relatively constant fraction of ClO$_x$ is present as ClO during day. Figure 3 shows that this assumption works well. The mixing ratio $\langle [\text{OH}] \rangle_{\text{day}}$ is modeled by assuming

\[
\langle [\text{OH}] \rangle_{\text{day}} \sim \text{FAS}
\]

Figure 4 shows that this is a sufficiently good assumption, partly due to the fact that the mixing ratios of OH are relatively similar in the northern and southern hemisphere. In conditions not disturbed by heterogenous chemistry on PSCs, it can be shown that the stratospheric OH abundance is in relatively good approximation a linear function of the solar zenith angle, mostly independent from the concentrations of other species (Hanisco et al., 2001). In addition, the average solar zenith angle in the vortex is in good approximation a linear function of FAS. However, this is not true anymore under conditions of
heterogeneous chemistry, and significant deviations from this behaviour occur, especially in the southern hemisphere (see Fig. 11 in Wohltmann et al., 2017, the effect is also visible in Figure 4).

Production and loss processes of HO$_x$ = OH + HO$_2$ are fairly complicated (Hanisco, 2003; Wohltmann et al., 2017). In particular, it is not possible to find a simple equation that relates the mixing ratios of the relevant source gases CH$_4$, HNO$_3$ and H$_2$O to the mixing ratio of HO$_x$. In addition, the partitioning inside HO$_x$ depends in a complicated way on O$_3$, ClO$_x$ and NO$_x$ and there are considerable differences in the partitioning of HO$_x$ between OH and HO$_2$ in the northern and southern hemisphere (see Wohltmann et al., 2017). Hence, only an empirical parameterization that is not a function of the source gases is given here. Note that this means that the Polar SWIFT model implicitly uses the water vapour and methane levels of the ATLAS model runs and that it is not possible to model responses to changes in these source gases with Polar SWIFT.

Term $F$ is fitted to the modeled rate of reaction R3. Figure 5 shows the modeled reaction rate and the fitted Term $F$.

### 3.1.4 Term $A$

Term $A$ accounts for the effect of the most important heterogeneous reaction activating chlorine

\[
\text{HCl} + \text{ClONO}_2 \rightarrow \text{Cl}_2 + \text{HNO}_3
\]  

(R4)

The parameterization of Term $A$ remains similar to the parameterization in the original model. For high HCl, it is given by

\[
A = a \cdot \langle [\text{ClONO}_2] \rangle \cdot \langle [\text{HNO}_3] \rangle^{2/3} \cdot \text{FAP}
\]  

(22)

and for low HCl it is given by

\[
A = a \cdot \langle [\text{HCl}] \rangle \cdot \langle [\text{ClONO}_2] \rangle \cdot \langle [\text{HNO}_3] \rangle^{2/3} \cdot \text{FAP}
\]  

(23)
**Figure 4.** Vortex averaged mixing ratio of OH for the Arctic winter 2004/2005, the Antarctic winter 2006, the Arctic winter 2009/2010 and the Antarctic winter 2011 at 54 hPa. Vortex average (solid blue) and parameterization for the mixing ratio by FAS$^2$ (dashed blue) and average over sunlit part of vortex (solid magenta) and parameterization for the mixing ratio by FAS (dashed magenta). Tick marks on the horizontal axis show start of months.

**Figure 5.** Fit of Term $F$ for the Arctic winter 2004/2005, the Antarctic winter 2006, the Arctic winter 2009/2010 and the Antarctic winter 2011 at 54 hPa. Vortex averaged reaction rate modeled by ATLAS for the reaction ClO + OH (blue) and the fitted Term $F$ (red). Tick marks on the horizontal axis show start of months.
Figure 6. Normalized pseudo first-order rate coefficients as a function of HCl mixing ratio for the heterogeneous reactions ClONO$_2$ + HCl (blue) and HOCl + HCl (cyan) on liquid STS surfaces. Reaction rates were calculated for $T = 190$ K, $p = 50$ hPa, 10 ppb HNO$_3$, 0.15 ppb H$_2$SO$_4$, 4 ppm H$_2$O and 1 ppb ClONO$_2$.

The threshold for HCl is set to 1 ppt. Reaction rates for heterogeneous reactions are proportional to the surface area density of the liquid or solid particles in the ATLAS model. The surface area density is modeled by $\langle [\text{HNO}_3] \rangle^{2/3} \cdot \text{FAP}$. Here, we assume that cloud particles are mainly composed of HNO$_3$, that all HNO$_3$ is in liquid or solid form in the area below the threshold temperature used for FAP, and that all HNO$_3$ outside this area is in the gas phase. In the original model, the parameterization $\langle [\text{HNO}_3] \rangle \cdot \text{FAP}$ was used. In the new model, $\langle [\text{HNO}_3] \rangle$ is raised to the power of 2/3 to account for the difference between particle volume density (proportional to the mixing ratio of liquid or solid HNO$_3$ per volume of air) and particle surface area density (surface is proportional to volume raised to the power of 2/3).

For heterogeneous reactions on NAT, reaction rates are not proportional to HCl, i.e. the change of HCl is given by

$$\frac{d[HCl]}{dt} \bigg|_{R4} = -k_{R4}[\text{ClONO}_2]$$

where $k_{R4}$ is a pseudo first-order rate coefficient, which is not a function of HCl. This is not the case for reactions on liquid STS surfaces, where the rate depends on the concentration of HCl (Figure 6). Activation mainly occurs on liquid surfaces in the model runs. The sensitivity of the reaction rate on the HCl concentration is non-linear, with a rapid increase between 0 and 0.3 ppb. The reaction rate becomes relatively independent of HCl above 0.3 ppb. Hence, a parameterization that does not depend on HCl is a good approximation and gives a better fit than a parameterization that depends linearly on HCl.

Term $A$ is fitted to the modeled rate of the heterogeneous reaction R4. Figure 7 shows the modeled rate of this reaction (blue) and the fitted term $A$ (red).
Figure 7. Fit of Term A for the Arctic winter 2004/2005, the Antarctic winter 2006, the Arctic winter 2009/2010 and the Antarctic winter 2011 at 54 hPa. Vortex averaged reaction rate modeled by ATLAS for the reaction HCl + ClONO₂ (blue) and the fitted Term A (red). Tick marks on the horizontal axis show start of months.

3.1.5 Term L

The new Term L accounts for the effect of the heterogeneous reaction

\[ \text{HOCl} + \text{HCl} \rightarrow \text{Cl}_2 + \text{H}_2\text{O} \] \hspace{1cm} (R5)

which can activate a significant part of chlorine in the southern hemisphere and a non-negligible part in the northern hemisphere.

In the original model, this contribution was implicitly subsumed into Term A. However, since we use Term A both in the HCl equation and in the ClONO₂ equation with the same fit parameter \( a \), we introduce an additional term here to represent the HCl loss by HOCl + HCl. Similar to the approach for Term A, Term L is parameterized by

\[ L = l \cdot \langle [\text{HOCl}] \rangle \cdot \langle [\text{HCl}] \rangle \cdot \langle [\text{HNO}_3] \rangle^{2/3} \cdot \text{FAP} \] \hspace{1cm} (25)

HOCl is parameterized by

\[ \langle [\text{HOCl}] \rangle \sim \langle [\text{ClO}] \rangle_{\text{day}} \cdot \text{FAS} \] \hspace{1cm} (26)

HOCl is in a fast equilibrium between

\[ \text{ClO} + \text{HO}_2 \rightarrow \text{HOCl} + \text{O}_2 \] \hspace{1cm} (R15)

and

\[ \text{HOCl} + h\nu \rightarrow \text{Cl} + \text{OH} \] \hspace{1cm} (R16)
under sunlit conditions. Using the equilibrium condition, we obtain

\[
\langle [\text{HOCl}] \rangle_{\text{day}} = \left( \frac{k_{R15}}{k_{R16}} [\text{ClO}] [\text{HO}_2] \right)_{\text{day}}
\]  

(27)

Now, we assume that the ratio of \([\text{HO}_2]\) and \(k_{R16}\) is nearly constant, since both terms depend on the amount of sunlight, which gives

\[
\langle [\text{HOCl}] \rangle_{\text{day}} \sim \langle [\text{ClO}] \rangle_{\text{day}}
\]  

(28)

\(\langle [\text{ClO}] \rangle_{\text{day}}\) is parameterized by \(\langle [\text{ClO}_x] \rangle\) (see discussion of Term \(F\) and Figure 3). If we assume that there is no HOCl during night, we obtain

\[
\langle [\text{HOCl}] \rangle = \langle [\text{HOCl}] \rangle_{\text{day}} \cdot \text{FAS}
\]  

(29)

This assumption is not straightforward. If the heterogenous reaction HOCl + HCl did not take place, night-time mixing ratios of HOCl would remain at mixing ratios similar to the daytime values, since the reactions R15 and R16 do not proceed during night. However, the parameterization for Term \(L\) is only different from zero when heterogenous reactions can proceed (due to the FAP term) and when enough chlorine is activated (due to the \(\langle [\text{ClO}_x] \rangle\) term). Under these conditions, HOCl is depleted by the HOCl + HCl reaction during night.

HOCl + HCl is a heterogeneous reaction whose reaction rate will be proportional to FAP. The rate of the HOCl + HCl reaction shows a more linear dependency on HCl mixing ratios than the ClONO\(_2\) + HCl reaction (Figure 6). Hence, we include the HCl mixing ratio as a linear factor in Term \(L\), which improves the fit compared to a parameterization that does not depend on HCl. Still, Term \(L\) shows one of the poorer fits compared to the other parameterizations.

Term \(L\) is fitted to the modeled reaction rate of the heterogeneous reaction R5. Figure 8 shows the modeled reaction rate and the fitted Term \(L\).

3.1.6 Term \(K\)

A reaction not included in the original model that affects the redistribution of HCl and ClONO\(_2\) in late winter and spring is

\[
\text{HCl} + \text{OH} \rightarrow \text{H}_2\text{O} + \text{Cl}
\]  

(R6)

as shown in Wohltmann et al. (2017). In spring, this reaction consumes much of the HCl that is produced by Cl + CH\(_4\). The reaction is represented by a new Term \(K\), which is parameterized by

\[
K = k \cdot \langle [\text{HCl}] \rangle \cdot \langle [\text{OH}] \rangle_{\text{day}} \cdot \text{FAS}
\]  

(30)

The equation is derived analogously to the equation for Term \(F\). We multiply by FAS again to take the average over the sunlit area into account. Term \(K\) is fitted to the modeled rate of reaction R6. Figure 9 shows the modeled reaction rate and the fitted Term \(K\).
Figure 8. Fit of Term $L$ for the Arctic winter 2004/2005, the Antarctic winter 2006, the Arctic winter 2009/2010 and the Antarctic winter 2011 at 54 hPa. Vortex averaged reaction rate modeled by ATLAS for the reaction $\text{HOCl + HCl}\rightarrow \text{Cl}_2 + \text{H}_2\text{O}$ (blue) and the fitted Term $L$ (red). Tick marks on the horizontal axis show start of months.

Figure 9. Fit of Term $K$ for the Arctic winter 2004/2005, the Antarctic winter 2006, the Arctic winter 2009/2010 and the Antarctic winter 2011 at 54 hPa. Vortex averaged reaction rate modeled by ATLAS for the reaction $\text{HCl + OH}\rightarrow \text{H}_2\text{O} + \text{Cl}$ (blue) and the fitted Term $K$ (red). Tick marks on the horizontal axis show start of months.
3.2 ClONO$_2$

3.2.1 Overview

The equation for ClONO$_2$ is changed from

$$\frac{d\langle[\text{ClONO}_2]\rangle}{dt} = B - A - G - H$$ (31)

in the original model to

$$\frac{d\langle[\text{ClONO}_2]\rangle}{dt} = B - A - H$$ (32)

in the new model. ClONO$_2$ is in a near equilibrium between

$$\text{ClONO}_2 + h\nu \rightarrow \text{Cl} + \text{NO}_3$$ (R10)

$$\rightarrow \text{ClO} + \text{NO}_2$$ (R11)

and

$$\text{ClO} + \text{NO}_2 + M \rightarrow \text{ClONO}_2 + M$$ (R12)

In the new model version, the net effect of these reactions (and of some additional ClONO$_2$ loss reactions) is described by Term $B$, while in the original model, there were two different additive terms $B$ and $G$. The net change of ClONO$_2$ by the above reactions is responsible for deactivation of active chlorine in the northern hemisphere. Term $A$ accounts again for the effect of the heterogeneous reaction

$$\text{HCl} + \text{ClONO}_2 \rightarrow \text{Cl}_2 + \text{HNO}_3$$ (R4)

which both activates HCl and ClONO$_2$, while Term $H$ accounts for the effect of the less important heterogeneous reaction

$$\text{ClONO}_2 + \text{H}_2\text{O} \rightarrow \text{HOCl} + \text{HNO}_3$$ (R17)

which only activates ClONO$_2$.

3.2.2 Term $B$

Term $B$ represents the net effect of the reactions R10/R11 and R12. ClONO$_2$ is in an equilibrium between R10/R11 and R12 (Wohltmann et al., 2017). Changes in ClONO$_2$ by a shift in this equilibrium are mainly induced by the production of NO$_x$ (NO$_x = \text{NO} + \text{NO}_2 + \text{NO}_3 + 2\text{N}_2\text{O}_5$). Since NO$_x$ is mainly produced by the comparably slow reactions

$$\text{HNO}_3 + h\nu \rightarrow \text{NO}_2 + \text{OH}$$ (R18)
HNO₃ + OH → H₂O + NO₃

(R19)

these reactions determine the net production of ClONO₂. The equilibrium condition for ClONO₂ can be written as

[ClONO₂] ∼ [ClO][NO₂]

(33)

Production of NOₓ will increase NO₂. In turn, ClONO₂ will increase almost instantly at the expense of NO₂ to match the equilibrium condition again. In this sense, ClONO₂ can be considered a part of NOₓ, which is mainly partitioned into NO, NO₂ and ClONO₂. Term B is parameterized by

\[ B = b \cdot \langle [\text{ClO}_x] \rangle \cdot \langle [\text{HNO}_3]_g \rangle \cdot \text{FAS} \]

(34)

where [HNO₃]_g denotes HNO₃ in the gas phase. This parameterization is obtained empirically, since it is again difficult to derive an expression from the chemical equations, and qualitatively takes into account the properties of the ClONO₂ equilibrium. The change of NOₓ is parameterized empirically as \( \langle [\text{HNO}_3]_g \rangle \cdot \text{FAS} \) taking into account that NOₓ is produced from HNO₃ under sunlit conditions. Term B is fitted to the sum of the modeled rates of the following reactions

ClO + NO₂ + M → ClONO₂ + M

(R12)

ClONO₂ + hν → Cl + NO₃

(R10)

ClONO₂ + hν → ClO + NO₂

(R11)

ClONO₂ + Cl → Cl₂ + NO₃

(R20)

ClONO₂ + OH → HOCl + NO₃

(R21)

ClONO₂ + O → ClO + NO₃

(R22)

The main channel of the photolysis reaction is into Cl+NO₃ (R10), but the minor channel R11 into ClO+NO₂ is also included in the fit. In addition, we include several reactions of the form ClONO₂ + X in the fit, where X is one of Cl, OH, O. Figure 10 shows the sum of the modeled reaction rates for these reactions and the fitted Term B.

3.2.3 Term A

See explanation in section 3.1.4.
Figure 10. Fit of Term B for the Arctic winter 2004/2005, the Antarctic winter 2006, the Arctic winter 2009/2010 and the Antarctic winter 2011 at 54 hPa. Sum of the vortex averaged reaction rates modeled by ATLAS for the reactions ClONO₂ + hν (both channels), ClO + NO₂, ClONO₂ + Cl, ClONO₂ + OH and ClONO₂ + O (blue) and the fitted Term B (red). Tick marks on the horizontal axis show start of months.

3.2.4 Term H

Term H accounts for the effect of the heterogeneous reaction

\[
\text{ClONO}_2 + \text{H}_2\text{O} \rightarrow \text{HOCl} + \text{HNO}_3
\]  

(R17)

Term H is parameterized by

\[
H = h \cdot \langle [\text{ClONO}_2] \rangle \cdot \langle [\text{HNO}_3] \rangle^{2/3} \cdot \text{FAP}
\]  

(35)

in the new model. The parameterization for Term H remains similar to the original model. The term \( \max(\text{FAP} - y, 0) \) of the original model (with \( y \) a fitted parameter) is exchanged by \( \langle [\text{HNO}_3] \rangle^{2/3} \cdot \text{FAP} \).

\( h \) is fitted to the modeled rate of reaction R17. The fit has a rather large residuum both with the original and the new parameterization. This is relativized by the fact that the ClONO₂ + H₂O reaction is only of minor importance for chlorine activation and ClONO₂ removal. One of the reasons for the disagreement may be the complicated dependence of the \( \gamma \) value of the reaction on H₂O (see Figure 11). Figure 12 shows the modeled reaction rate and the fitted Term H.

3.3 HNO₃

The change in the total amount of HNO₃ (i.e. the sum of the gas phase and the condensed phase) is given by

\[
\frac{d\langle [\text{HNO}_3] \rangle}{dt} = -E
\]  

(36)
Figure 11. Normalized pseudo first-order rate coefficient of ClONO$_2$ loss as a function of H$_2$O mixing ratio for the heterogeneous reaction ClONO$_2$ + H$_2$O on liquid STS surfaces. Reaction rates were calculated for $T = 190$ K, $p = 50$ hPa, 10 ppb HNO$_3$, 0.15 ppb H$_2$SO$_4$, 2 ppb HCl and 1 ppb ClONO$_2$.

Figure 12. Fit of Term $H$ for the Arctic winter 2004/2005, the Antarctic winter 2006, the Arctic winter 2009/2010 and the Antarctic winter 2011 at 54 hPa. Vortex averaged reaction rate modeled by ATLAS for the reaction ClONO$_2$ + H$_2$O (blue) and the fitted Term $H$ (red). Tick marks on the horizontal axis show start of months.
Figure 13. Fit of Term $E$ for the Arctic winter 2004/2005, the Antarctic winter 2006, the Arctic winter 2009/2010 and the Antarctic winter 2011 at 54 hPa. Vortex averaged rate of change of HNO$_3$ by denitrification modeled by ATLAS plus the rate of change of HNO$_3$ by chemical reactions modeled by ATLAS (blue) and the fitted Term $E$ (red). Tick marks on the horizontal axis show start of months.

Both in the original and in the new model. Changes in HNO$_3$ are dominated by changes due to denitrification, i.e. the irreversible removal of HNO$_3$ by sedimenting cloud particles. Term $E$ is parameterized by

$$E = e \cdot \langle [\text{HNO}_3] \rangle \cdot FAP_s$$

(37)

The term max(FAP − y, 0) of the original model is replaced by FAP$_s$ in the new model. The rate of change by sedimenting particles is assumed to be proportional to the volume of HNO$_3$ condensed in the cloud particles. For this, it is assumed that the amount of HNO$_3$ that is in the cloud particles is proportional to the total amount of HNO$_3$ inside the area indicated by FAP$_s$ and that the HNO$_3$ mixing ratio is proportional to the particle volume. Additionally, it is assumed that there are no cloud particles outside the area indicated by FAP$_s$. FAP$_s$ is chosen because denitrification is modeled by sedimenting large NAT particles which form above a given supersaturation.

$e$ is fitted to the modeled change by sedimenting particles plus the modeled sum of all reactions changing HNO$_3$ (which is small). Figure 13 shows the modeled rate of change of HNO$_3$ and the fitted Term $E$.

The partitioning between HNO$_3$ in the gas phase and in the liquid and solid phase is calculated by

$$\langle [\text{HNO}_3]_g \rangle = (1 - FAP_s) \cdot \langle [\text{HNO}_3] \rangle + z \cdot FAP_s \cdot \langle [\text{HNO}_3] \rangle$$

(38)

in the new version. In the original version, FAP was used for FAP$_s$. $z$ is obtained by a simple linear fit from Equation 38 and the model results for FAP$_s$, [HNO$_3$] and [HNO$_3$]$_g$. 
The rate of change of ozone is given by

\[
\frac{d\langle[O_3]\rangle}{dt} = -D
\]

where Term \( D \) is parameterized by

\[
D = d \cdot \langle[\text{ClO}_x]\rangle \cdot \text{FAS}
\]

Term \( D \) remains unchanged compared to the original model. The parameterization is based on the fact that the combined effect of the most important catalytic ozone destruction cycles (the ClO dimer cycle and ClO–BrO cycle) is a nearly linear dependence of ozone destruction on \( \text{ClO}_x \) (Rex et al., 2014). In addition, the rate of change of ozone depends on the amount of available sunlight due to the ClO dimer photolysis reaction.

The ClO dimer cycle alone would lead to a quadratic dependence on ClO in the sunlit part of the vortex, since the reaction

\[
\text{ClO} + \text{ClO} + \text{M} \rightarrow \text{Cl}_2\text{O}_2 + \text{M}
\]  

(R23)

is the rate-limiting step in the cycle. That would lead to the parameterization \( \langle[\text{ClO}_x]\rangle^2 \cdot \text{FAS} \), since \( \langle[\text{ClO}\rangle_{\text{day}} \sim \langle[\text{ClO}_x]\rangle \) (see Figure 3) and ClO is only present in the sunlit part of the vortex. The nearly linear dependence of the rate of change of ozone on \( \text{ClO}_x \) for the sum of the effect of both cycles has several reasons: The dependence of the rate of change of ozone on \( \text{ClO}_x \) caused by the ClO–BrO cycle, the dependence of the rate of change of ozone on \( \text{ClO}_x \) caused by the ClO dimer cycle, and the repartitioning of ClO and BrO.

The fact that most of the \( \text{ClO}_x \) that is set free from the heterogeneous reactions is in the form of Cl\(_2\) in early winter and needs to be photolysed into Cl can be ignored for the purpose of our model, since this happens before substantial ozone depletion is observed.

The amount of Br\(_y\) is not explicitly parameterized in the Polar SWIFT model. The effect of Br\(_y\) is implicitly included since the magnitude of the rate of change of ozone depends on the ClO–BrO cycle. The ATLAS runs that are used for the fits are initialized with a maximum Br\(_y\) of 19.9 ppt. Note that this means that the Polar SWIFT model implicitly uses the bromine levels that are given in the ATLAS model runs and that it is not possible to model responses to changes in bromine with Polar SWIFT.

Term \( D \) is fitted to the sum of the modeled reaction rates of all reactions changing ozone. Figure 14 shows the modeled reaction rates and the fitted Term \( D \). The figure shows that the parameterization works very well for ozone.

### 4 Validation

The species mixing ratios simulated by the Polar SWIFT model are compared to corresponding measurements of the Microwave Limb Sounder (MLS) satellite instrument and to simulations by the full stratospheric scheme of the ATLAS model.
Figure 14. Fit of Term $D$ for the Arctic winter 2004/2005, the Antarctic winter 2006, the Arctic winter 2009/2010 and the Antarctic winter 2011 at 54 hPa. Vortex averaged rate of change of O$_3$ by all reactions modeled by ATLAS (blue) and the fitted Term $D$ (red). Tick marks on the horizontal axis show start of months.

For validation, Polar SWIFT is implemented into the ATLAS model for the validation runs and uses the transport and mixing scheme of the ATLAS model, while the detailed stratospheric chemistry scheme of the ATLAS model is replaced by the simplified Polar SWIFT model. Runs are driven by ECMWF ERA Interim reanalysis data. This approach is needed to obtain results from Polar SWIFT that can be compared to measured data.

Polar SWIFT is implemented in ATLAS by adding the rate of change of ozone calculated by Polar SWIFT for a given layer to the ozone value of every air parcel inside the vortex and inside this layer. Note that this means that the ozone field does still vary across the vortex. The same is done for the other species HCl, ClONO$_2$ and HNO$_3$. The vortex means of these species, which are needed as input at the start of every time step, are obtained by averaging over all air parcels inside the vortex in the layer. Outside of the polar vortex, O$_3$, Cl$_y$, HCl, HNO$_3$ and ClONO$_2$ are reinitialized every day with seasonal climatologies.

For O$_3$ and HNO$_3$, a seasonal climatology based on all available MLS data is used (i.e. which is a function of the month of year, with data from all years averaged). Cl$_y$, ClONO$_2$ and HCl are taken from a seasonal climatology derived from ATLAS runs with the full chemistry model. While HCl is available from MLS data, it is not used here so that the sum of HCl and ClONO$_2$ is consistent with Cl$_y$.

Simulations of the Arctic winters 1979/1980–2013/2014 and the Antarctic winters 1980–2014 are conducted. The simulated interannual variability of ozone is compared to the observed interannual variability derived from MLS satellite data for the years from 2005 to 2014.

For every winter and hemisphere, a new run is started which is initialized with species mixing ratios from the same MLS and ATLAS climatologies that are used for the reinitialization described above (i.e. the same starting conditions in every year). Runs start on 1 November and end on 31 March in the northern hemisphere and start on 1 May and end on 30 November in the southern hemisphere. The long-term change in the chlorine loading of the stratosphere is considered by multiplying the Cl$_y$, 

27
**Figure 15.** Interannual variability of vortex averaged ozone mixing ratios in Arctic winter at 46 hPa for Polar SWIFT (blue) and MLS (red), on the last day before vortex breakup. The date differs for different years due to different dates of vortex breakup, see Table 4.

**Figure 16.** Interannual variability of vortex averaged ozone mixing ratios in Antarctic spring at 46 hPa on 1 October for Polar SWIFT (blue) and MLS (red).

HCl and ClONO$_2$ values by a number obtained by dividing the Equivalent Effective Stratospheric Chlorine (EESC, Newman et al., 2007) of the given year by the EESC of the year 2000.

Figure 15 shows the vortex averaged mixing ratios at 46 hPa simulated by Polar SWIFT in the northern hemisphere at the end of the winter compared to the mixing ratios obtained from MLS ozone data. Note that the date used in the plot differs for every year, since the date of the breakup of the polar vortex is different in every year. The dates are given in Table 4. Figure 16 shows the same for the southern hemisphere and on 1 October. Both the magnitude and the interannual variability of the MLS measurements are reproduced well by the Polar SWIFT model runs in the northern hemisphere. The interannual variability is larger and reproduced better in the northern hemisphere than in the southern hemisphere.
Table 4. Dates of vortex breakup for Figure 15

<table>
<thead>
<tr>
<th>Date</th>
<th>Years</th>
</tr>
</thead>
<tbody>
<tr>
<td>10 February</td>
<td>2009</td>
</tr>
<tr>
<td>15 February</td>
<td>2010</td>
</tr>
<tr>
<td>1 March</td>
<td>1984, 1989</td>
</tr>
<tr>
<td>10 March</td>
<td>1980, 2005</td>
</tr>
<tr>
<td>24 March</td>
<td>2011</td>
</tr>
<tr>
<td>No stable vortex</td>
<td>1985, 1999</td>
</tr>
</tbody>
</table>

Figure 17. Time evolution of vortex means of O₃ and HCl in the northern hemispheric winter 2004/2005 for Polar SWIFT driven by the ATLAS transport model (left), for the full chemistry model of ATLAS driven by the ATLAS transport model (middle) and for MLS satellite measurements (right). The black line marks the approximate breakup date of the vortex.
Figure 18. Same as Figure 17 for the southern hemispheric winter 2006.

Figure 17 shows the time evolution of vortex averages of $O_3$ and HCl for the winter 2004/2005 in the northern hemisphere. The first column shows the results of the Polar SWIFT model run driven by ATLAS and ERA Interim, the second column the results of the full chemistry model run of ATLAS and the third column the corresponding measurements of MLS. Figure 18 shows the same for the year 2006 and the southern hemisphere. The time evolution of ozone is reproduced well in both hemispheres. Since the long-term ozone climatology used for the initialization of Polar SWIFT is different from the actual measured values, some differences show up in early winter. The evolution of HCl shows some differences, which are partly caused by the fact that the full ATLAS model has a parameterization that partitions a significant part of HCl into the liquid phase to overcome a discrepancy between modeled and measured HCl values (for a detailed discussion, see Wohltmann et al., 2017). Polar SWIFT is always fitted to the total HCl mixing ratios of ATLAS and has no parameterization for HCl in the liquid phase. MLS measures HCl in the gas phase, and consequently, the figures for the full chemistry model and MLS show HCl in the gas phase. Hence, some differences between the total HCl values of Polar SWIFT and the gas phase values of MLS are observed. This is however of secondary importance, since the only variable of Polar SWIFT that is used outside of Polar SWIFT in a GCM is ozone.

5 Conclusions

This study presents an update of the Polar SWIFT model for fast calculation of stratospheric ozone depletion in polar winter. The update includes a revised formulation of the system of differential equations, a new training method based on model results of the ATLAS Chemistry and Transport Model and an extension from a single level to the vertical range in which polar ozone depletion is observed.
The model is validated by comparison to MLS satellite data and the full stratospheric chemistry scheme of the ATLAS model. It is shown that Polar SWIFT is able to successfully simulate the interannual variability and the seasonal change of ozone mixing ratios in the northern and southern hemisphere (Figure 15 to 18).

Polar SWIFT was specifically developed to enable interactions between climate and the ozone layer in climate models. So far, climate models often use prescribed ozone fields, since a detailed calculation of ozone chemistry is computationally very expensive. The computational effort needed is significantly reduced when using the Polar SWIFT model. The computing time for a complete winter simulated by Polar SWIFT is on the order of a fraction of a second on a single processor core, while the computational effort for the detailed chemistry model of ATLAS is on the order of several days per winter on 50 cores on current machines.

Polar SWIFT models the response of ozone to temperature changes and changes in the chlorine loading well, since care has been taken to represent the underlying chemical and physical processes in the model equations. This is also shown in Figure 15 to 18. As far as possible, the equations are derived by mathematical derivation, but note that some model equations are derived by empirically finding parameterizations that closely fit the training data set, since no closed equation can be derived for them. Bromine, methane, water vapour and some effects of HNO₃ are not variable in the model equations, which limits the ability of the model to respond to changes in these species and should be kept in mind.

Polar SWIFT has already been implemented successfully into the EMAC model and into ECHAM 6.3 and the first validation runs have been performed and show promising results. Results will be published in separate studies.

6 Code availability

The source code is available on the AWIForge repository (https://swrepo1.awi.de/). Access to the repository is granted on request under the given correspondence address. If required, the authors will give support for the implementation of SWIFT.

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References


