Dear referee #1,

Thank you for positive review and helpful comments. We addressed each of them and separately responded in the following list:

1. “Sometimes more explanations would be very helpful, in particular concerning the pollination module.”

   We followed the suggestion of the reviewer and extended the explanations of the newly implemented processes.

2. “In the introduction and discussion a lot of weight is put on migration processes and the inability of large-scale models to deal with it. In this context it seems at least a bit strange that the authors restrict their simulation to one plot of at maximum 200m*200m. It would be more convincing to make clear that you started with a detailed small scale model which later could maybe inform larger scale models and in particular can enhance understanding of gene flow in forests.“

   We extended the introduction with a statement about the intention of the model building as suggested.

3. “The question remains: how can this approach be adopted by models running on a larger scale? Can, for example, the detailed simulation of individual seeds and trees be upscaled? Does it make sense to use approaches as discussed in (Snell, 2014, Using dynamic vegetation models)? Please discuss.”

   We extended the potential model applications paragraph with suggestions for further development and upscaling approaches with this model.

4. “As already pointed out using only a small area of 4 ha for studying migration processes seems weird. Also the circular boundary conditions might confound results of spatial processes because spatial gradients disappear. (Maybe I got that wrong, but then it indicates that a better explanation is needed!)”

   We used only a small area for the verification of the implemented processes: for the newly implemented sensitivity analyses we used 100 x 1,000 m transects with plots tied together on the meridional borders securing a south-to-north migration.

5. “It also seems to me that ignoring the size or age of father trees, and by that the relative amount they contribute to the pollen cloud, can affect the results.”

   We did not explicitly include any allometric relationships of pollen production and tree performance in this version of the model because of sparse reference data, but it would be a further development. It is partly covered through the tree top height in the calculation of the pollination probability. See also our comment to RC1#24. We added an explanation in the discussion.

6. “A lot would be clarified by more detailed captions of the figures.”

   We added more descriptions to the figure captions.
Dear referee #1,

We address the specific comments and clarify formulations:

7. “Throughout the text: avoid the term “pollination of seeds”. Biologically the ovules are pollinated, and this yields the seeds. Or at least clarify that you mean the ovules in this context.”

   We clarified here and throughout the manuscript, the process of pollination of ovules rather than seeds as suggested.

8. “L36: There are forest models for all scales, not only for stands. Omit “stand”.”

   We adapted the sentence as suggested.

9. “L37: Between forest stand models and DGVMs, there are forest landscape models, which incorporate seed (whereas not pollen) dispersal (c.f., Snell et al, 2014, Using dynamic vegetation models; Shifley et al., 2017) and have been applied also to the arctic (e.g. TreeMig, Epstein et al, 2007).”

   We included this model type in the enumeration.

10. “L50: what do you mean by “at the molecular level”? The genes? The coded proteins? Or the resulting traits?”

    We mean the traits of individuals, on which selection can act, and adapted the sentence for clarification.


    We edited the sentence to clarify the consequences of high gene flow for local populations.

12. “L51: I do not understand how local adaptation prevents negative consequences (which ones?) due to founder effects. Clarify”

    We clarified the consequences, see response RC1#11 for details.

13. “L63: commonly -> sometimes. E.g. concerning DGVMs, to my knowledge up to now Rebecca Snell’s LPJ-GUESS version is the only one with something a bit similar to dispersal. Forest Landscape models of course contain dispersal, but believe it or not, it is very often switched off!”

    We exchanged the statement as suggested by the reviewer.


    Yes, we changed it.

15. “L108: It would biologically be more logical to start with pollination and describe seed dispersal afterwards”

    We exchanged the process implementation as suggested.

16. “L111: the formula is hard to read, one has to guess: (1/2)*distanceratio*(rand)**1.5 ???”

    We inserted an additional multiplicator sign for clear reading of the equation.

17. “L116: height of the tree top?”
We clarified the tree height by changing the expression to “tree top” as suggested.

18. “L120: Unclear: Probably you mean: wind speed and direction, which were randomly selected from a set of observations”

We changed the sentence structure as suggested by the reviewer.

19. “L121: Start with a general conceptual description of the pollination and refer to fig. 1.”

We moved parts of the implemented pollination from the introduction to here and refer to the conceptual sketch in figure 1.

20. “L122: Is the pollination simulated really for each individual ovule? Idea for an upscaling: Would it be possible to do that more in a "share" approach per tree (assuming that all ovules are of the same genotype): Of N seeds of the tree, the share p1 are pollinated with pollen from father 1, p2 from father 2,...”

Our description of the determination of pollen donors was not clearly stated: it was implemented in a “share” approach per tree as the reviewer suggests. We extended the description for clarification.

21. “L124: now you confuse me: tree or seed?”

We clarified the statement.

22. “L131: make the reference to fig. 1 more prominent, I overread it several times, and found fig. 1 just by chance.”

Following the suggestion of the reviewer, we added a reference to the beginning of the paragraph.

23. “L138: “pollen distribution”, isn’t it rather the overall pollination probability of a seed?”

We changed according to the suggestion the introduction of the equation.

24. “L140: Please make explicit if and how the pollen amount comes into play and how it depends on tree size or age or weather. How is a father tree defined by the variables above? How does its distance to the mother tree come into play? I see it in fig. 1, but not in the formulae”

For simplification, we have not yet included further allometric relationships into the functions for pollination calculation, but this can easily be achieved. See further details in RC1#5. The distance between mother and father tree is used in the functions, variable r.

25. “L160: runaway line”

We deleted the line.

26. “L187: What is the difference between the two parallelisations A and B?”

We added a description of the two different ways of parralellisation of a STL-list-container.

27. “L189-205: I’m confused. What is the difference between the implemented dispersal function and the full model? Isn’t the dispersal function implemented into the full model? So, where can differences come from? Why do you need this verification? Please clarify.”

We developed the functions in R and implemented them subsequent in C++. We intended to verify the implementation and correct computation of these and give a general overview about the resulting dispersal with our verification.
28. “L239: Why do you undergo the effort to calculate the wind-direction-dependent pollen transport, to then take father trees randomly from any direction? Why not using the father trees in the different directions? Or did I misunderstand that? Do you really sample the father trees with uniform probability?”

We edited the text to solve the potential misunderstanding of the calculation of the pollination process here and in the method section.

29. “L260: Why do you mention the times? Because the RAM adds up over time, or because the numbers of trees and seeds increase over time?”

The list-container require RAM depending on the actual tree and seed elements stored in them.

30. “L284: and forest landscape models, in particular individual based ones like Iland (Seidl et al, 2012)”

We added the additional model type of landscape models and the suggested citation.

31. “L312: Unclear. What would slow down the recent potential migration rate? And how?”

We edited this and the preceding sentence for clarification.

32. “L358: This would require simulations on very large areas or long transects, for which the current approach is (still) too slow. Some simplification/upscaling would be required.”

We are currently working on a simplified model, which is informed by simulations with LAVESI-WIND but especially designed for millennial-scale continental simulations. According to the suggestion of the reviewer, we extended the sentence.

33. “L365-370: This is the real step forward, I would even emphasize it more!”

We re-ordered the potential model application paragraph and placed this possible application at the end.

34. “Fig. 3: Please extend the caption, explaining in much more detail what was recorded. In particular the directions need to be explained. I guess, for wind and seeds, the direction means in which direction they go, in contrast for pollination the direction refers to where the father trees are?”

We give more details in the caption for a better understanding. See also RC2#78.
Dear referee #2,

Thank you for positive review and helpful comments. We addressed each of them and separately responded in the following list:

1. “New contributions are the insertion of wind speed and distance in the already existing seed dispersal kernel and the new pollination probability function. Beside this, however, it is only shown that the implementation of the functions work as intended and that two unspecified parallelisations lead to a computation time reduction. Else, the authors mainly write what potentially could be done with the model, but unfortunately miss to give sufficient instructions for how this could be done, nor do they show example simulations for the potential applications.”

We moved the verification to the supplement and included sensitivity analyses for both processes. In this new analyses, we used hypothetical transects and tracked for example the migration of the treeline border to evaluate the model's results to the change of the input parameters.

2. “I do not understand why the authors decided to put so much emphasis on describing the verification with all its sophisticated applied statistics. In my opinion the verification does not contribute to a knowledge gain and could be dealt with a few sentences, referring the main share to the supplementary. However, I do believe that a transparent description of the parameterisation and applied sensitivity analyses could be of large value for the community.”

This step was included to technically verify the implementation of wind-dependent seed dispersal and pollination. Following the recommendation of the reviewer we moved the verification to the supplement and included a sensitivity analyses for both newly implemented functions.

3. “I recommend a thorough revision of the manuscript targeting that in the end only those applications are emphasised in the abstract, introduction and conclusion that are sufficiently prepared in the methods and results and appropriately discussed.”

We edited the manuscript in many parts to include the new results of the sensitivity analyses.
Responses to recommendation for the different sections:

4. “(1) Abstract: In my opinion the abstract does currently not fit to the content of the paper. Reading it, I developed different expectations not addressed in the manuscript, such as model applications (at least exemplary) dealing with the advocated passing of genetic information and/or diversity and/or identifying important drivers of migration dynamics. Also global vegetation models are mentioned twice prominently in the abstract, e.g. last sentence: ’... substantially help in unveiling the important drivers ...’, however, unfortunately, I did not get an idea from the manuscript how this could be done and how global vegetation models can be improved. I recommend rewriting the abstract more closely describing the manuscript.”

We extended the manuscript with sensitivity analyses for both processes and added the main results in the abstract. Our intention with this manuscript is to present the model improvements and to give in the abstract the key information about why we implemented the model extension.

5. “(2) Introduction: The authors refer to DGVMs and list processes not implemented in them. However, they do not mention why these processes are not included – e.g. issues of parameterisation (see e.g. Snell et al. 2014), particularly also due to the high variation in seed dispersal rates (and vectors) within the plant functional types currently used (see e.g. Huntley et al. 2010, Lee 2011, Snell et al. 2014, Svenning et al. 2014), issues of coarse spatial resolution and of computational complexity arising with inter-grid cell communication via seed dispersal or other spatially linked processes (e.g. Nabel 2015) – yet these issues that cause problems for larger scale models seem to even get visible in this manuscript describing a local single species model: when discussing the huge increase in computation cost and that the model is not properly parameterised for the suggested studies (indicated by sentences such as "Before applying this new model version, however, a proper parameterisation is necessary." “If this can be efficiently parameterised, the model could further be used to track genetic lineages in time.”). I recommend mentioning these prominent problems of seed dispersal implementation in the introduction and relate to them in the discussion.”

We refer to the parametrisation issue caused by the use of plant functional types in DGVMs as well as increased simulation complexity caused by inter-grid cell communication.

6. “(3) Methods: (a) According to 2.1 the presented simulations assume homogeneous forest stands with periodic boundary conditions. However, applications to study tree line dynamics, or migration in general, or the suggested "impact of migration processes on the genetics", require dispersal among inhomogeneous plots/gridcells and I would appreciate at least a small application showing how the model can be used for such conditions, showing e.g. what migration speed results from the model, which processes have largest influences etc.”

We decided to follow the suggestion to include a sensitivity analysis for such processes. For this we simulated hypothetical 100 x 1,000 m transects on which seed dispersal was allowed on the meridional borders but not the latitudinal limits and tracked the colonisation to calculate migration rates. A further application to parameterise the model’s functions and assess migration rates for north-central Siberia would be beyond the scope of this manuscript and was recently accepted for online discussion (https://doi.org/10.5194/bg-2018-267).
7. “(3) Methods: (b) "2.2.4 parameterisation to fit field data": even if the authors only visually compared the resulting number of trees, it might be helpful to have a table listing the number of trees for different parameter combinations (at least in the supplementary). What sensitivities were detected, which parameters were particularly important/ influential in tuning the number of trees? The authors state that the model parameters required a revision after implementing the extensions - what can we learn from this? It might be worth to discuss which parameters had to be revised and how, which are sensitive and influential - these things could be really helpful for the community.”

We tuned manually the parameters and the resulting changed parameter values can be found in Table 1. In the Table we changed estimated to tuned in cases of fine tuning done for this manuscript. The regarding sensitivities can be found in Kruse et al. (2016) and also in the newly incorporated sensitivity analyses.

8. “(3) Methods: (c) Most of the parameters in Table 1 are stated as "estimated" but there at least needs to be a starting point! If the study aims to help parameterising DGVMs it would be helpful to at least know on what the parameters are originally based, even if its from another species etc.”

We changed the status of parameters that were tuned here to “tuned”, details about first guesses can be found in Kruse et al. (2016).

9. “(3) Methods: (d) 2.3.2: I find this section difficult to read and understand. If I am not mistaken the dispersal function was once implemented inside and once implemented outside the model (which I think is not explicitly stated somewhere?). I would move most of this and the according results section to the supplementary and only retain that the model was successfully verified.”

We moved large parts of the verification as suggested, see RC2#2 for details.

10. “(3) Methods: (e) 2.3.3: The header of this section suggests an evaluation. The text of the section suggests that the simulation results will be quantitatively compared to observed values from literature. Yet I did not find such a comparison in the results section.”

We have now included sensitivity analyses for both processes and moved the verification to the supplement. The resulting sensitivity values are discussed in the discussion section and we give further suggestions and comparisons to findings in the literature.

11. “(4) Results: (a) As stated above, I would move most of 3.1 to the supplementary (all comparison to ‘directly’ estimated/calculated).”

We moved the verification of the implementation of the function to the supplement as the reviewer suggested.

12. “(4) Results: (b) I do not get the "fraction of significant differences" in Table 2”

We calculated the mean pollination distances based on the same set of mature individuals and compared the resulting distances to these calculations. In the Table we state the amount of significant different mean values for each of the directions.

13. “(4) Results: (c) The second parallelisation variant outruns the first when using four cores, however, there seems to be a saturation in that 8 cores are not doing better but even worse than 4, why is this? It would be interesting to see what happens with 16/more cores!”

We ran additional simulations as suggested. See comment RC2#65.
14. “(5) Discussion: (a) The authors start with stating that unlimited seedbeds cause high uncertainty in DGVM predictions. While I agree that the assumption of unlimited seedbeds contributes to the uncertainty in DGVM studies/projections I think that there are heaps of at least equally important uncertainty sources, like modelling of mortality, competition, canopy structures, etc. Furthermore, I do not see that the manuscript present a remedy for the uncertainty connected to seedbeds. In my opinion a min/max assumption with no and full dispersal currently gives a better uncertainty frame than difficult to parametrise dispersal kernels. If one of the main messages of the manuscript stays that LAVESI-WIND can be used to enhance DGVMs, e.g. by parameterising dispersal kernels, I strongly recommend to discuss the issue and difficulties of (PFT) parameterization (see e.g. Huntley et al. 2010, Lee 2011, Snell et al. 2014).”

We included further details to the suggested topics in the discussion and in the introduction. Corresponds with RC1#2.

15. “(5) Discussion: (b) LAVESI is a single species model parameterised for a certain Larix species. I wonder how not represented processes, such as competition with other species/understory, trait variability, or others, could influence migration processes, particularly in the currently tree-less tundra? Is this implicitly covered by the parameterisation? If it’s implicitly covered, how might this change with climate change?”

Larches form single-species dominant forests in the areas the model was developed for and further competition with understory species (shrubs, grasses, etc.) were included implicitly. Future development of the model should be tested for the influence of such on the migration rate. We added a reference in the potential model application section.

16. “(5) Discussion: (c) Large parts of the model are realised as stochastic processes. How many repetitions are required to get a sound result, e.g. how is a targeted output variable such as migration speed influenced by the stochasticity?”

Even with the high stochasticity caused by many processes in the model, the variance is small when gathering the results of ten simulations. We randomly sampled from the 30 simulation repeats with a 50%-increased seed production factor the target variable of peak recruitment position. It can be seen that even with ten simulation repeats, the confidence interval is small and decreases further when using more repeats. Accordingly, we recommend to run a minimum of ten or better 30 simulation repeats to get sound results.
Figure review 1. Position of the peak recruitment position calculated from 2 to 30 simulation repeats relative to the value from 30 simulation repeats.

17. “(5) Discussion: (d) The last sentence of 4.2. stating that the model is not yet parameterisation to field data sounds as if it would only be a small step, but I assume that this is rather difficult and would like to read a bit more about how this can be done and what problems are anticipated.”

We explained that reference data for the northernmost arctic treeline areas are missing and thus a complete parameterisation could not be achieved.

18. “(5) Discussion: (e) The increase in computation costs associated with seed dispersal and the like have been mentioned in several places (e.g. Snell et al. 2014, Svenning et al. 2014, Nabel 2015) and are one of the reasons why seed dispersal is usually not accounted for on larger simulation extents. I think it would be worth to mention that this is a common finding when dealing with seed dispersal. Furthermore, the authors mention hundreds of CPUs here but did only conduct simulations with 1, 4 and 8 CPUs (and with one of the parallelisation the avg sim time was worse with 8 than with 4 CPUs). In order to better support their statements and in order to assess the merit of the parallelisations another set of simulations with e.g. 16 or 32 CPUs would be helpful.”

We added accordingly the suggested citations in the text. Furthermore, we ran additional simulations to test whether the simulation time decreases further when using more CPUs. Furthermore, we found a wrong setting for the simulation of 8 cores and correcting this led to consistent results. See also comment RC2#65 for further details on this.
19. “(5) Discussion: (f) In my opinion section 4.4 is not well supported by the rest of the manuscript. I for example miss a link from simulations on the homogeneous 200 x 200 m plot with periodic boundaries to a study investigating migration rates. How are borders of simulation plots connected? How is the long distance dispersal dealt with and pollination which potentially reach over several plots? How does this increase the computational complexity, is such a simulation currently computationally feasible? Especially, when you a certain set of repetitions is required to account for the stochasticity?

For the simulations used in this manuscript, we stated the different model settings for boundary conditions in the methods section. The newly incorporated sensitivity analysis was run on a 100 wide and 1,000 m long hypothetical transect. The meridional borders are connected and seeds passing the borders are distributed further in the north or south depending on their dispersal direction. Pollen on the other hand is not distributed over the borders of simulated plots. Whereas long-distance seed dispersal does not significantly increase the simulation time, and the implementation of pollination over plot borders would be feasible, when traits are passed via pollen and seeds one must decide how the information is passed (e.g. sampling from all available trait space), which we partly included in the ‘pollen influx’ application.

Furthermore, how can pollen influx be studied when the amount of pollen is not simulated by the model?”

One simple approach we think about is to simulate forest stands similar to those around locations for which pollen influx rates are available from surface sediments or sediment cores and tune the pollination process (even by including an allocation factor) until the resulting rates match. Subsequently one can compare past influx rates to simulations with this parameterised model forced with climate data independent from the pollen record and evaluate the importance of other model parameters.
Dear referee #2,

We address the “small comments, questions and remarks” below:

20. “l.1 - title: Since LAVESI did already contain spatially explicit seed dispersal, maybe add wind driven "Implementing spatially explicit wind driven seed and pollen dispersal ...”

We extended the title to clarify the scope of this manuscript.

21. “l.23 - is the selected pollen donor still potential? maybe: "... select the pollen donor.""

We adapted the sentence as suggested.

22. “l.46 - "is mainly caused"”

We improved the sentence to be clearer with the causation of overestimations of DGVMs.

23. “l.47 - "using a time lagged response function"? Snell 2014 uses a dispersal function for dispersal deteelly grid cells and a logistic function to limit within grid cell dispersal”

The reviewer is right, we changed the sentence accordingly.

24. “l.53 - "this" refers to what? local adaptation?“

We extended the content of the sentence and clarified the references.

25. “l.59 - "this ensured the most realistic implementation" I would remove this part of the sentence or rephrase the paragraph, because of the previously mentioned dynamics at the treeline. I had to read the sentence several times before I realised that this refers to the homogeneous forest only.”

We removed the unclear statement. Among other tested dispersal functions, the Gaussian with a fat tail led to stand structures best fitting to observations.

26. “l.63 - "are not coupled" – There is a phd thesis integrating wind dispersal in the DGVM CLM, see https://globalchange.mit.edu/sites/default/files/Lee_PhD_2011.pdf”

We included the additional suggested reference, which is an important step.

27. “l.64 - ‘Among others, Student’s 2Dt...’ This sentence seems lost - delete it?”

We removed the sentence as suggested.

28. “l.69-77: move to methods or discussion”

We moved parts of the paragraph to the methods and also the discussion section.

29. “l.84: “Results of the validation" -> verification?“

The regarding sentence was deleted.

30. “l.83-86: I would delete these sentences, particularly the second part informing that there is a discussion and conclusion section.”

The sentence were restructured and now gives a better summary of the content of the manuscript.

31. “l.93: I would use past here (i.e. "which were parameterised"), since you describe the parameterisation it in Kruse et al. (2016) and, if I understood it correctly, reparametrized it for this study?”
We changed the use to past in the sentence.

32. “I.95: What exactly are "homogeneous forest plots of 100 x 100 m" - 1. does a simulation run on one plot or several plots? 2. Does homogeneous refer to the environmental conditions? What is the resolution and what is the extent of the simulation runs?”

Here, “homogeneous” refers to spatial homogeneity, which means the climate is the same across the whole plot. Wherever seeds are dispersed within the borders of the plot, trees can grow. The plot size is variable, depending on the available computer sources, and a subgrid with 20-cm tiles is used for competition and further sensing of the environment of each tree. We edited the sentence for clarification.

33. “I.95: "seed dispersed beyond the plot borders" - thus out of the 100 x 100m plot?”

Yes.

34. “I.99: "... lag the hypothetical warming ..." – maybe "... densification and northwards migration might lag the applied hypothetical warming ..."”

We extended the sentence following the suggestion of the reviewer.

35. “I.111: for better readability maybe insert a space or comma or other separator between distance ratio and rand”

We inserted an additional multiplicator sign for clear reading of the equation.

36. “I.113: Does this refer to (1) the sensitivity analysis in Kruse et al. 2016 or (2) a new analysis? If (1) maybe point again to the reference, if (2) can you show results of the sensitivity analysis in your supplementary?”

We based the estimates on our earlier sensitivity analysis documented in Kruse et al., 2016.

37. “I.116+117: do you have references for the 75%, for Vd and lambda? Is there any biological interpretation for lambda?”

The values of two-thirds of the tree top height was chosen here as a sophisticated estimate based on own observations and parameters Vd chosen for the species trait based on Matlack (1987). Lambda is a tuning parameter and here only used to bring the height from m to cm dimension. This parameter could further be used to set the dispersal distance differently for additional species.

38. “I.120: a reference to 2.2.5 would be helpful here”

We refer now to the wind observation data set description.

39. “I.124: "subsequently" to what?”

We deleted the misleading word.

40. “I.128: could you shortly write what C and m are? Why do you use m=1.25? Gregory (1961) seems to recommend different values for m for different conditions.”

The parameters C and m are function parameters not further defined by Gregory (1961). We selected these values as a start here and fine tuning of these is planned in further studies.
41. “l.133: the symbols for the angle between trees and the actual wind direction are very difficult to visibly distinguish, because the bar is hardly noticeable. Maybe make the bar more visible, lower, or use another symbol for the wind direction”

We changed the notation of theta for clarification.

42. “l.143: "monthly climate series" - reading that the model has an annual temporal resolution I had to went back to the LAVESI description. I think it might be helpful to very briefly state which CRU variables are used to derive which annual driving variables”

We refer now to the climate variables used and added a sentence to describe which driving variables are computed from these.

43. “l.147: in this sentence field work is mentioned but it is neither explained what field work this was, nor a reference given. In l.156 I can infer that the reference probably is Wieczorek et al. (2017) and from this and other places I infer that the field work took place from 2011-2013. Maybe it would be easier to swap 2.2.3 and 2.2.4 and shortly properly introduce the field work.”

We changed the order of the paragraphs as suggested and added a brief introduction to the conducted fieldwork.

44. “l.149: should probably be “-36°C”

Yes, we corrected the temperature statement.

45. “l.153: which field data? (see above). 100 x 100 areas -> is this the one 100x100m plot? How many repetitions did you simulate?”

We improved the paragraph by additional explanation of the fieldwork.

46. “l.155: I do not get which climate you use. Is this the climate described in 2.2.3 or not? If so: do not repeat, if not: why not?”

We deleted the additional reference to the field site and refer to the climate data, which is described in paragraph 2.2.4 below.

47. “l.156: even if the number pf trees was only visually compared it would be nice to see some combinations of number of trees and parameters in a table”

We responded to this issue in RC2#7.

48. “l.158: what is a good fit?”

We clarified that we compared the stand densities for parameter tuning.

49. “l.160: "Climate forcing data" – leftover?”

We deleted the extra line.

50. “l.171: do you refer with "plots" to the 50 repetitions of the one simulated plot?”

Yes, we changed the text accordingly and refer to one plot rather than multiple plots.

51. “l.182: from all pollen sources or from the selected donors?”

We recorded only pollination events, not all potential pollen sources.
52. “l.184: "implemented simulations" -> "conducted simulations"
   We changed the word implemented to conducted as suggested by the reviewer.

53. “l.184-: repetition with 225”
   For clarification, we merged the final sentence with some repetition into this.

54. “l.187: How do these two parallelisations differ?”
   We added a description of the two different ways of parallelisation of a STL-list-container.

55. “l.203: "north between 345° and 15°" - how does this compare to the directions in Table 2?”
   We changed the degree value of -15° that equates to 345° in Table 2 to the latter value to match the text.

56. “l.219: plural vs singular: "computation time increases"
   We corrected the misuse of the plural of time.

57. “l.220: readability: “produced seeds”
   We changed the order of words as suggested.

58. “l.225-: repetition with 184 (however without 2 CPUs)"
   We deleted the sentence and checked given statements of used numbers of CPUs in the manuscript.

59. “l.239: uniform ? -> 2.2.2: "based on the probability density"
   We deleted the misleading reference and clarified the selection of the father tree.

60. “l.242: "the higher values" - which?”
   We clarified the connection of this and the preceding sentence.

61. “l.242-: I do not get: "4-6% of test show significant differences ... no evidence that the differences are significant"?
   We added the reference to the appropriate table 2 (now in supplement) with the stated fraction of significant differences.

62. “l.257: Maybe output storage is not in the Table S1?”
   The output is written out on demand and not stored in the RAM to reduce the memory consumption especially for large simulated plots.

63. “l.269: maybe replace inferring by calculating/tracking”
   We exchanged the word “inferring” to “including” for clarification.

64. “l.270: maybe replace estimating by calculating”
   We exchanged the word as suggested.
65. “I.273: the second variant outruns the first when using four cores, however, there seems to be saturation in that 8 cores are not doing better than 4 but slightly worse, why is this?”

We set the parameters for the run with eight cores wrongly and used again only four. However, the computation time may increase due to overheads introduced due to idle cores when the tree list is split and handed over to a higher number of cores. This effect can be seen when comparing the two different parallelisation approaches, of which the second performs better with less cores but did not improve further when using more cores as we could see here for first variant.

66. “I.289-: I would delete these three last sentences”

We deleted these sentences as suggested.

67. “I.300: "~ 12 m metres"”

We meant the maximum amount of seeds reaching ~12 m.

68. “I.303: -> Duncan (1954)”

We added the missing bracket.

69. “I.312: how did the winds change, such that the potential migration rate slowed down and not e.g. increased?”

This is a general statement and for clarification we edited this and the following sentences.

70. “I.317: maybe add ‘pollination’ and ‘this’, i.e.: "overestimation of pollination distances, but this seems unlikely"”

We followed the advice of the reviewer and edited the sentence accordingly.

71. “I.323: LAVESI-WIND?”

We refer in the text now to the current model acronym as suggested.

72. “I.324: maybe "evaluate with field-based data"?”

We exchanged the word as suggested.

73. “I.336: from the perspective of a DGVM grid cell (typically > 0.5”) 5,000 x 5,000 m is still very small scale”

In this paper we present the implementation and first tests of wind-dependent seed dispersal and pollination in the individual-based spatially explicit model. A trial run needed 40 hours for 10,000 years of a dense forest plot simulation, showing the general applicability even for millennial simulations in time. This model did was not intended to be used for continuous continental scale simulations but more to use it as validation/parameterisation of interconnections and potential time lags between DGVM grids, however with further improvements and using large computer clusters this might be possible. We stated this in the end.

74. “I.337: LAVESI-WIND?”

We added the current model version acronym as suggested.
75. “LAVESI-WIND?”

The version acronym was added to the model’s name.

76. “LAVESI-WIND?”

for each adult tree (potential pollen source) and for each seed source.”

We corrected the references to correspond with the figure legend.

77. “LAVESI-WIND?”

the shaded areas ... pollination probability for the labelled source ...” ->

this is the probability for the one labelled source, or?”

We clarified the seed source reference in the caption.

78. “LAVESI-WIND?”

I am surprised that 150-200m does not occur for pollination. Is this due to the
perspective taken for the plot? I.e. when I understand it correctly the seeding is from the
perspective away from a centre and the pollination is from the perspective of the centre? A
short sentence on this would be great for a quick understanding. When looking solely at the
figure it would also be nice to have some more information in the caption on what the figure
shows, e.g. a short note if this is an average of 50 runs with the full LAVESI-WIND.

The maximum pollination distance in the simulation setup is 155.6 m from one corner of
the full 200 x 200 m plot to the most distant corner of the centre 20 x 20 m plot. We give
more details in the caption for a better understanding.

Table 1: For a discussion of the re-parameterisation it would be nice if the original values of
the parameters could be listed here, too. This would also help to identify the new parameters.

We decided to keep the table as it is and give here only the adapted values.

Table 2: The different notations -15 and 345 are a bit irritating.”

We improved the notation. See comment RC2#83.

Further comments in the supplementary material:

79. “LAVESI-WIND?”

the structure Evaluation contains for each year one element. Footnote 5 was accidentally
deleted.


We give the full expressions in the table headers.

81. “Table S3: comma for thousand misplaced”

We corrected the misplaced comma.

82. “Table S3: why do the distance percentiles differ as compared to Table S2?”

The distance percentiles differ because here they are calculated for each direction
separately and in the other table for both direction at the same time.

83. “Table S4: notation mixing initially confuses (-15 vs 345)”

We changed -15° to 345° for readability.
Implementing spatially explicit wind-driven seed and pollen dispersal in the individual-based larch simulation model: LAVESI-WIND 1.0

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Abstract. It is of major interest to estimate the feedback of arctic ecosystems to the global warming we expect in upcoming decades. The speed of this response is driven by the potential of species to migrate, tracking their climate optimum. For this, sessile plants have to produce and disperse seeds to newly available habitats, and pollination of ovules is needed for the seeds to be viable. These two processes are also the vectors that pass genetic information through a population. A restricted exchange among subpopulations might lead to a maladapted population due to diversity losses. Hence, a realistic implementation of these dispersal processes into a simulation model would allow an assessment of the importance of diversity for the migration of plant species in various environments worldwide. To date, dynamic global vegetation models have been optimised for a global application and overestimate the migration of biome shifts in currently warming temperatures. We hypothesise that this is caused by neglecting important fine-scale processes, which are necessary to estimate realistic vegetation trajectories. Recently, we built and parameterised a simulation model LAVESI for larches that dominate the latitudinal treelines in the northernmost areas of Siberia. In this study, we updated the vegetation model by including seed and pollen dispersal driven by wind speed and direction. The seed dispersal is modelled as a ballistic flight, and for the pollination of ovules of seeds produced, we implemented a wind-determined and distance-dependent probability distribution function using a von Mises distribution to select the potential pollen donor. A local sensitivity analyses of both processes supported the robustness of the model’s results to the paramterisation, although it highlighted the importance of recruitment and seed dispersal traits for migration rates. This individual-based and spatially explicit implementation of both dispersal processes makes it easily feasible to inherit plant traits and genetic information to assess the impact of migration processes on the genetics. Finally, we give implications suggest how Tt he final model can be applied to substantially help in unveiling the important drivers of migration dynamics and, with this, guide the improvement of recent global vegetation models.

1. Introduction
How fast vegetation communities can follow their shifting climate envelope in a changing environment is determined by their ability to migrate. This is exceptionally challenging under current global change and plants might strongly lag behind their moving climate envelope (Harsch et al., 2009; Loarie et al., 2009; Moran and Clark, 2012). Temperatures are increasing most strongly in the Arctic. Accordingly, forests in the tundra-taiga transition zone are expected to respond by migration into the tundra (Bader, 2014; Holtmeier and Broll, 2005; MacDonald et al., 2008). However, empirical studies show diverse responses to the warming, including treelines being stable, advancing or even retreating (Harsch et al., 2009). A taiga range expansion though, might positively feedback to a global temperature increase due to albedo reduction (Bonan, 2008; Piao et al., 2007; Shuman et al., 2011).

To predict forest stand responses to climate, computer models were designed with different scopes of complexity, between highly general to very specific (Grimm and Railsback, 2005; Thuiller et al., 2008). Among these, simulation studies with dynamic global vegetation models (DGVMs) tend to overestimate the turnover of treeless tundra into forests (Brazhnik and Shugart, 2015, 2016; Frost and Epstein, 2014; Kaplan and New, 2006; Roberts and Hamann, 2016; Sitch et al., 2008; Snell, 2014; Yu et al., 2009; Zhang et al., 2013). On the other hand, forest landscape models (e.g. Snell et al., 2014; Shifley et al., 2017; Epstein et al., 2007) and small-scale models (forest-gap or individual-based) provide sufficient detail to realistically represent the responses at a stand level, but need much effort for parameterisation and are typically not applied over large areas (Martínez et al., 2011; Pacala et al., 1996; Pacala and Deutschman, 1995; Zhang et al., 2011). Further problems arise from the use of plant functional types as they consist of species with a wide variety of traits (e.g. Huntley et al. 2010, Lee 2011, Snell et al. 2014, Svenning et al. 2014). Nonetheless, the ability to form a closed canopy forest depends mainly on species traits acting at a fine-scale level such as (1) time needed to mature (life-cycle, high generation time) and produce viable seeds, (2) dispersal distance and the chance for long-distance seed dispersal and (3) germination and establishment of new individuals (Svenning et al., 2014). One source of The overestimation of migration rates of DGVMs is mainly caused by unconstrained seed availability when climate variables allow a vegetation type to establish, which was recently pointed out by using a time laged response dispersal function between the grid points in simulations with a DGVM (Snell, 2014; Snell and Cowling, 2015). However, connecting grid cells to allow dispersal among them increases the computational complexity of such models (e.g. Nabel 2015), but would be necessary to simulate realistic large-scale vegetation responses. In addition, the structure of a tree stand, and its response to changes in external forcing, is determined by further local processes, such as spatially explicit competition among individuals of all ages and their interactions. Of special interest is the local adaptation of the traits of individuals of local populations at the molecular level, which are influenced by a high gene flow through seed or pollen distributions across populations. High exchange can lead to outcrossing that hinders local adaptation, but also prevents negative consequences from diversity losses caused from inbreeding within separated isolated populations due to founder effects in the process of colonisation over large distances (Austerlitz et al., 1997; Burczyk et al., 2004; Fayard et al., 2009; Nishimura and Setoguchi, 2011; Ray and Excoffier, 2010). These processes have not been implemented continuously over a large scale in such simulation models.
Treeline stands in the Siberian Arctic were densifying, but only rather slowly colonising the tundra during the past decades (Frost et al., 2014; Kharuk et al., 2006; Montesano et al., 2016), which could be attributed to seed limitation (Wieczorek et al., 2017). We developed the *Larix* vegetation simulator LAVESI to simulate tree stand dynamics at the Siberian treeline on the southern Taymyr Peninsula and use it as a framework to explore impacts of climate change on larch forests (Kruse et al., 2016). In the first version, the dispersal function randomly dispersed seeds by a probability density function describing a Gaussian term with a fat-tail. This ensured the most realistic implementation and could be parameterised to fit observed stand patterns. The model simulates tree stands on plots, representing a homogeneous forest, which can easily be enlarged to simulate wider areas. However, for simulations on larger transects passing from forests to treeless areas, wind direction and strength become more important for seed dispersal and needed to be included in the model. Seed dispersal processes are well studied (Nathan et al., 2011a; Nathan and Muller-Landau, 2000) and are commonly-sometimes implemented in vegetation models but are seldomly rarely coupled with wind speed and direction (e.g. Lee, 2011; Levin et al., 2003; e.g.--Snell, 2014). Among others, Student’s 2D$t$ dispersal kernel depicts best the leptokurtic behaviour of dispersal kernels (Clark et al., 1999; Clark, 1998; Nathan and Muller-Landau, 2000; Petrovskii and Morozov, 2009). Also wind patterns might change over time, such as the pressure levels vary in a changing climate (Trenberth, 1990), or are directed (Lisitzin, 2012) so that an implementation of wind-dependent dispersal would enable a more realistic simulation of migration (cf. Nathan et al., 2011b).

Pollen was not represented in the former LAVESI version, but is needed to independently track gene flow by seeds and pollen through time. Pollen dispersal functions are frequently used to reconstruct vegetation composition from palaeo archives, for example in the Landscape Reconstruction Algorithm by Sugita et al. (2010), whereas other models have been used to track pollen clouds in tree stands (review in Jackson and Lyford, 1999; Prentice, 1985). Calculating every pollen dispersal event for each tree and seed is computationally challenging, but it can be simplified following the assumptions of Kuparinen et al. (2007). Accordingly, an individually based pollination for each seed could be implemented using a wind-determined and distance-dependent probability distribution function for pollen dispersal (similar to Gregory, 1961). It would make use of the von Mises distribution, which is an angular equivalent to the Gaussian normal distribution, for the two-dimensional representation (Abramowitz and Stegun, 2012). Besides tracking the full genealogy of a simulated tree stand, this pollination function allows the inheritance of individually varying traits of each tree, rather than randomly drawing the actual trait value from the pool of available traits (cf. Scheiter et al., 2013). Additionally, the implementation of spatially explicit seed dispersal and pollination would enable us to align the model to detailed biogeographical knowledge gained from molecular methods (e.g. Navascués et al., 2010; Polezhaeva et al., 2010; Semerikov et al., 2007, 2013; Sjögren et al., 2017). We started with a very detailed small-scale model that can later be used to inform large-scale models especially about plot connectivity through seed dispersal and pollination and subsequent gene flow in landscapes.

We aim with this study to enable the simulation of spatially explicit and wind-dependent seed dispersal and pollination in the individual-based model LAVESI. After the coupling and verification of the seed dispersal kernel to prevailing winds and the incorporation of the pollination is described in Section 2, we test the model’s sensitivity to its parameterisation in local sensitivity analyses and the influence on stand development, migration rates, and pollination distances. Results of the validation of the
updated model by comparisons of simulation experiments to observed wind patterns are presented in Section 3, which are discussed in Section 4 and followed by conclusions in Section 5.

2. Methods

2.1. General model description of the Larix vegetation simulator LAVESI

LAVESI is an individual-based spatially explicit model that currently simulates the life cycle of larch species as completely as possible from seeds to mature trees (Kruse et al., 2016). It was set up to improve our understanding of past and future treeline displacements under changing climates, focusing on the open larch forest ecosystem in northern Siberia, which is underlain by permafrost. The relevant processes (growth, seed production and dispersal, establishment and mortality) are incorporated as submodules, which were parameterised on the basis of field evidence and complemented with data from literature. Simulation runs proceed in yearly time steps and are forced by monthly temperature and precipitation time series. The area simulated represents spatially homogeneous forest plots of variable size with the use of an environment grid (e.g. competition) with 20-cm tiles and where the handling of seeds dispersed beyond the plot borders are deleted can be set to deletion or reintroduction from the other side to simulate a forest patch. The model is programmed in C++ using standard template libraries. This and its modular structure allow a straightforward implementation of further extensions. The model was successfully applied to conduct temperature-forcing experiments, where simulations revealed that the responses of the larch tree stands in Siberia – densification and northwards migration – might lag the applied hypothetical warming by several decades, until the end of 21st century (Kruse et al., 2016; Wieczorek et al., 2017).

Here we present the implementation of wind-dependent seed dispersal as well as the newly introduced pollination. The absorbing boundary condition had to be revised to allow the simulation of larger areas. Hence, we introduce a new mode of periodic boundary conditions for seeds leaving the simulated area, so that the borders of a simulation plot are connected along all borders, which we used in all the simulations for this manuscript. This mimics a tree stand within a homogeneous forest, similar to forest gap models (e.g. Brazhnik and Shugart, 2016; Pacala et al., 1996; Pacala and Deutschman, 1995; Zhang et al., 2011).

2.2. Implementing dispersal processes coupled to wind speed and direction

2.2.1. Pollination probability

Pollen was not represented in the former LAVESI version, but is needed to independently track gene flow by seeds and pollen through time. Accordingly, Figure 1 illustrates how we implemented an individually based pollination for each seed’s ovule using a wind-determined and distance-dependent probability distribution function for pollen dispersal (similar to Gregory, 1961). It makes use of the von Mises distribution, which is an angular equivalent to the Gaussian normal distribution, for the two-dimensional representation (Abramowitz and Stegun, 2012).
A pollen dispersal function was newly implemented as a distance-dependent probability function for pollination of each individual seed’s ovule, rather than simulating the large amount of pollen released by each tree (Gregory, 1961; Kuparinen et al., 2007). For each seed-bearing tree, the probability of pollen donating trees is calculated and out of the list of potential fathers for each seed one tree is randomly determined. The pollination probability of each seed’s ovule on a tree is proportional to the amount of pollen in the air column around it, which is, for simplification in the current implementation, not additionally dependent on the performance of the tree so that every tree that bears cones is taken into account, but this aspect might be included in future versions. The following function is used here as the distance-dependent probability distribution of arriving pollen:

\[ p_r = \exp \left( \frac{-2p_e r^{1-0.5m}}{\sqrt{\pi C(1-0.5m)}} \right) \tag{3} \]

where \( p_r \) is the distance-dependent distribution, \( r \) is the distance in m, \( p_e \) is the ratio of pollen descending velocity estimated for Larix gmelinii (Eisenhut, 1961) and wind speed and parameters Gregory’s \( C \) and \( m \) are set to \( C = 0.6 \text{ cm}^{-1-0.5m} \) and \( m = 1.25 \) (Eq. page 167 in Gregory, 1961).

The distribution described in Eq. 3 is multiplied by the von Mises distribution (Eq. 4), a continuous probability distribution on the circle, to include pollen distribution over a certain area and couple the process to the wind direction (illustration in Fig. 1; Abramowitz and Stegun, 2012).

\[ p_v = \frac{\exp(k \cos (\theta - \overline{\theta}))}{2\pi \overline{I}_0(\kappa)} \tag{4} \]

where \( \kappa \) is the inverse of the von Mises distribution's variance, and \( I_0(\kappa) \) is the modified Bessel function of order 0 as a function of \( \kappa \), \( \theta \) is the angle between trees and \( \overline{\theta} \) the actual wind direction. The modified Bessel function in the von Mises distribution is programmed in its integral representation using the Simpson integration scheme (Abramowitz and Stegun, 2012).

Consequently, following Gregory (1961) the pollen probability of a seed’s ovule mathematical form is:

\[ p = p_r p_v = \exp \left( \frac{-2p_e r^{1-0.5m}}{\sqrt{\pi C(1-0.5m)}} \cdot \frac{\exp(k \cos (\theta - \overline{\theta}))}{2\pi \overline{I}_0(\kappa)} \right) \tag{5} \]

### 2.1.1.2.2. Seed dispersal

In the initial version of LAVESI, seeds are dispersed in random directions and at a distance \( r \) in m, estimated by a Gaussian and negative exponential (fat-tailed) dispersal function (Eq. 5, Kruse et al., 2016):

\[ r = \sqrt{2E_0^2(-\log(\text{rand}))+\frac{1}{2} \text{distanceratio} \cdot \text{rand}^{-1.5}} \tag{1} \]

where \( E_0 \), originally named *width*, is the Gaussian distribution’s standard deviation in m, \( \text{rand} \) stands for a random number \( \in [0,1] \) and \( \text{distanceratio} \) is a weighing factor for the fat tail in m². Parameter estimates were based on a sensitivity analysis in Kruse et al. (2016) and numerical experiments.
The wind-dependent distance estimation was implemented as a ballistic flight following the assumptions of Matlack (1987). Accordingly, seed dispersal distances depend on the height of the releasing tree $H_t$ in m, currently estimated as 75% of $H_t$, and are modified by wind speed $V_w$ in m s$^{-1}$ and a species-specific fall speed of propagules (seed plus wing) $V_d = 0.86$ m s$^{-1}$ for $L. gmelinii$ and tuned by the parameter $\lambda$ (set to 0.01):

$$E_0 = 0.75 \cdot \lambda \cdot H_t \cdot \frac{V_w}{V_d}$$  \hspace{1cm} (2)

Finally, the direction for the seed dispersal is determined by the randomly selected wind observation (speed and direction, which were randomly selected from a set of observations (see Section 2.2.5 for details).

### 2.1.2. Pollination probability

A pollen dispersal function was newly implemented as a distance-dependent probability function for pollination of each individual seed, rather than simulating the large amount of pollen released by each tree (Gregory, 1961; Kuparinen et al., 2007). The pollination probability of a tree is proportional to the amount of pollen in the air column around it; subsequently, the following function is used here as the distance-dependent probability distribution of arriving pollen:

$$p_r = \exp\left(\frac{-2p_x e^{-r/0.5m}}{\sqrt{\pi C(1-0.5m)}}\right)$$  \hspace{1cm} (3)

where $p_r$ is the distance-dependent distribution, $r$ is the distance in m, $p_x$ is the ratio of wind speed and pollen descending velocity estimated for $Larix gmelinii$ (Eisenhut, 1961) and parameters $C$ and $m$ are set to $C = 0.6$ cm and $m = 1.25$ (Gregory, 1961).

The distribution described in Eq. 3 is multiplied by the von Mises distribution (Eq. 4), a continuous probability distribution on the circle, to include pollen distribution over a certain area and couple the process to the wind direction (illustration in Fig. 1; Abramowitz and Stegun, 2012).

$$p_\phi = \frac{\exp(k \cos(\theta - \bar{\phi}))}{2\pi I_0(k)}$$  \hspace{1cm} (4)

where $k$ is the inverse of the von Mises distribution's variance, and $I_0(k)$ is the modified Bessel function of order 0 as a function of $k$, $\theta$ is the angle between trees and $\bar{\phi}$ the actual wind direction. The modified Bessel function in the von Mises distribution is programmed in its integral representation using the Simpson integration scheme (Abramowitz and Stegun, 2012).

Consequently, following Gregory (1961) the pollen distribution's mathematical form is:

$$p = p_r p_\phi = \exp\left(\frac{-2p_x e^{-r/0.5m}}{\sqrt{\pi C(1-0.5m)}}\right) \frac{\exp(k \cos(\theta - \bar{\phi}))}{2\pi I_0(k)}.$$  \hspace{1cm} (5)

For each seed produced in simulation runs, every tree that bears cones is taken into account as a potential pollen donor. From these, one tree is randomly chosen based on the probability density to become the father of the produced seed.
2.1.3. Temperature and precipitation

Simulations are forced with monthly climate series from the CRU TS 3.22 database (Harris et al. 2014). We selected a grid box intersecting a location with a known northern taiga tree stand (CH06 at 70.66° N; 97.71° E, site CF in Wieczorek et al., 2017) and a northern forest tundra stand (TY04, 72.41° N; 105.45° E, site FTe in Wieczorek et al., 2017). From the available data we excluded years before 1934, because of missing climate station data and hence unreliable extrapolations in the data set (Mitchell et al., 2004). Furthermore, the final year was set to 2013, which is the latest year of field work. The climate at these sites either allows strong tree growth with mean July temperatures of 13.50 °C, coldest temperatures during January of -33.24 °C and a precipitation sum of ~328 mm per year or only sparse stands to emerge with temperatures of 13.11 and 36.07 °C in July and January, respectively, and ~247 mm annual precipitation (cf. Kruse et al., 2016).

2.1.4. Parameterisation to fit field data

The model’s parameters had to be revised after implementing the model extensions to achieve simulated tree densities comparable to field data. Forest inventory data were recorded for each larch individual with explicit positions on plots of a minimum area of 20 x 20 m areas for several locations along a density gradient from single-tree stands in the north to dense forest tundra stands in the south visited on summer expeditions in the years 2011 and 2013 in north-central Siberia, Russia (Wieczorek et al., 2017). We conducted simulations on 100 x 100 m areas with closed boundaries initialised by introducing 1,000 seeds in the first 100 years of a stabilisation period of 1,000 years, with forcing climate data randomly sampled from the available data. For the final 80 years of each simulation we used the climate series from one of the corresponding field sites (TY04, see 2.2.4 for details, 72.41 °N and 105.45° E, site FTe in Wieczorek et al., 2017). We visually compared the number of trees at year 2011 from the central 20 x 20 m area to the field survey data, which was the first year of fieldwork. The parameters were manually tuned and we iteratively performed simulation runs to improve the simulation results until finally achieving a similar stand densities (numbers of trees) good fit to the observed pattern (data not shown; parameter values in Table 1).

Climate forcing data

2.2.4. Temperature and precipitation

Simulations are forced with monthly mean temperature and precipitation sum series from the CRU TS 3.22 database (Harris et al. 2014). These are used to estimate long-term responses and derive the auxiliary climate variables active air temperature (sum of temperatures above 10 °C, AAT_{10}) and vegetation length (number of days exceeding the freezing point, net degree days, NDD_{0}) to calculate tree growth (details in Kruse et al., 2016). We selected a grid box intersecting a location with a known northern taiga tree stand (CH06 at 70.66° N; 97.71° E, site CF in Wieczorek et al., 2017) and a northern forest tundra stand (TY04, 72.41° N; 105.45° E, site FTe in Wieczorek et al., 2017). From the available data we excluded years before 1934, because of missing climate station data and hence unreliable extrapolations in the data set (Mitchell et al., 2004). Furthermore, the final year was set to 2013, which is the latest year of fieldwork. The climate at these sites either allows strong tree growth with mean July temperatures of 13.50 °C, coldest temperatures during January of -33.24 °C and a precipitation sum of ~328
mm per year or only sparse stands to emerge with temperatures of 13.11 and -36.07 °C in July and January, respectively, and ~247 mm annual precipitation (cf. Kruse et al., 2016).

### 2.1.5.2.2.5. Wind speed and direction

The model is driven with pairs of wind speed in m s⁻¹ and wind direction in degrees [°]. The winds at 10 m above the surface for the years 1979–2012 at 6 hourly resolution were extracted from the ERA-Interim reanalysis data set (Fig. 3; Balsamo et al., 2015). Because of the coarse spatial resolution (80 x 80 km), we considered only the grid box over the climate station Khatanga, which is situated roughly in the centre of the treeline ecotone on the southern Taymyr Peninsula (71.9° N; 102.5° E; Wieczorek et al., 2017). During simulation runs, values are randomly drawn from the year’s vegetation period (May to August; Abaimov, 2010) for each seed dispersal event and for the determination of pollination. For simulated years in which climate data are available but no corresponding wind data, a year is randomly selected.

#### 2.2.2.3. Model eSensitivity analyses for dispersal processes evaluation protocol

##### 2.2.1. Overall simulation setup

The simulation experiments were conducted on 200 x 200 m plots using the model with the new processes. Populations were initiated on empty areas by randomly distributing a fixed number of seeds during the first 100 years of a 1,000 year-long stabilisation period. The simulation model randomly drew weather conditions for each year from the complete available period 1934–2013 during the stabilisation period. In the final 80 simulation years, the actual weather data were used.

First, we performed simulation experiments with constant wind conditions to verify the implemented dispersal processes. Wind forcing was from the north or from the south, both with a constant wind speed of 10 km h⁻¹. Simulations were repeated 50 times with an input of 250 seeds per year during initialisation.

Second, we evaluated the functionality of the seed dispersal function by forcing the model with wind data from the reanalysis data set ERA-Interim (Balsamo et al., 2015). Simulations were repeated 10 times and population growth initiated by introducing 100 seeds per year during initialisation.

The dispersal distance and direction as well as the release height of every 100th seed dispersal event were recorded during each year of the complete simulation run. Pollination was assessed by recording the distance and direction from the pollen sources to the seed positions prior to seed release of all tree individuals present at the final year of the simulation.

Finally, we parallelised the code of the model using the OMP library and implemented simulations using 1, 2, 4 and 8 CPUs. The performance of the model was evaluated by recording the computation time of each single simulation year for complete simulation runs (1,080 years). We conducted four different runs, one with only wind dispersal of seeds (SEED), one with seed and pollination (+POLL), and two different parallelised pollination computations (+POLL_PAR-A and B).

##### 2.2.2. Verification of wind-dependency

We verified the wind-dependent seed dispersal by comparing the simulation results with the simulated results from the implemented dispersal function and refer to these values as ‘expected’. Therefore, we estimated the dispersal distances with...
the implemented dispersal functions (seeds Eq.1 and pollen Eq.5) under the same conditions as used for driving the model, namely winds from north or south with a constant speed of 10 km h$^{-1}$. The observed mean log-transformed (to achieve normal distribution) dispersal distances were compared to each other with a Welch two-sample t-test. We compared simulated to expected dispersal distances in each wind direction in height classes of trees in 10% steps of the sorted values, excluding the minimum and maximum values where only few observations could be recorded. The simulated data values in the range of ±5% at the determined height classes were first tested for an interaction between the release height and the dispersal distance with a Spearman’s rank-based measure of association (rho) and a t-test. Then we compared the simulated distances for each height class to the expected distances, both log-transformed prior to analysis, with a t-test. Furthermore, we compared the dispersal in both directions to each other using the same procedure.

The simulated pollination distances were compared to estimates from the implemented function under the same conditions, namely the adult trees’ position and constant north or south winds with a speed of 10 km h$^{-1}$. The resulting three-dimensional pollination distribution probabilities at simulation year 2011 (first year of field work) were binned to cardinal directions in steps of 30°, starting with North between 345° and 15°. The simulated and directly estimated log-transformed pollination distances were tested for differences in each individual direction with a Welch two-sample t-test for cases with > 10 observations. We tested whether the mean of the p-values is significantly greater than 0.01 with a Student t-test. To test the influence of the parameterisation of the variables from the newly introduced functions on the model’s results, we ran local sensitivity analyses (Grimm & Railsback, 2005, Cariboni et al., 2007). The input parameters (Table 2) were changed by 5 and 50% and a sensitivity value calculated by comparing the results with the reference run:

$$S_{+/−} = \frac{V_{+/−}V_{REF}}{\left| P_{+/−}P_{REF} \right|}$$

where $V$ is the variable of interest derived from each simulation run and $P$ is the parameter of interest, both plus (+) and minus (-) 5% of the estimated parameter, or with the reference value (Kruse et al., 2016).

For the evaluation of migration rates we selected three target output variables for the area ahead of the 100 m initialization area: (1) stemcount is the total number of stems (trees with a height above 130 cm), (2) forested area is the area covered with >100 stems ha$^{-1}$, and (3) peak recruit position is the position of the maximum number of stems on the basis of a running mean with a 50 m window. Additionally, the variable stand density, which is the number of stems in the 20 x 20 m plot in the centre of the lowermost area, was selected to assess impacts on plot level. Furthermore, the pollination distance expressed as the mean distance between the pollen-donating and seed-producing trees was calculated for the evaluation of the pollination function. The resulting sensitivity values were tested for significant changes from the reference results (mean of 0) with a t-test with a confidence level of 95%.

The simulations were carried out on hypothetical transects with a width of 100 m and length of 1,000 m using the new model version. Populations were initiated on empty areas only in the lowermost 100 m wide area by randomly distributing 1,000
seeds during the first 10 years of a 1,000 year long stabilisation period. During this phase, seeds exceeding the lowermost 100 x 100 m area were removed from the simulation. In the following simulation period seeds could enter the area above 100 m and colonise this empty area. The simulation model randomly drew weather conditions for each year from the complete available period 1934–2013 during the stabilisation and simulation period. These simulations were repeated for 30 times and the positions of each tree-individual tree were recorded at the end of the simulation (500 years). To directly compare results from simulations with changed parameters to reference runs the simulation period was repeated for each parameter variation starting with an identical state of the simulation at the end of the stabilisation period and using the same climate series.

2.4. Model-performance experiments

2.2.3. Evaluation of dispersal processes

The seed dispersal and pollination distances were evaluated by calculating the mean dispersal distances for both processes in bins of 30° cardinal directions over the complete simulation run for years with available wind data (1979–2012). In addition, we selected two years with contrasting wind patterns, the year 1990 with predominant winds from the East, and 1998 from the West. The results were qualitatively compared to observed values from the literature.

During the simulations, we recorded only one pollination event per tree per year reaching the central area of 20 x 20 m of the plot and every 100th seed dispersal event.

2.2.4. Model performance experiments

The memory load was estimated by adding up the size of all data types within each handled structure simulating a plot of one hectare (Table S1). These were multiplied by the actual number of elements in each of the structures. We calculated mean values of the number of handled items of the final 80 years of the simulations for the evaluation of dispersal processes to estimate the total memory needed for the arrays of trees and seeds and the grid representing the environment (Kruse et al., 2016).

Finally, to reduce the computation time, we parallelised the code for estimating pollination probabilities, seed dispersal, and tree density computation of the model using the OMP-library and implemented conducted simulations using 1, 2, 4, 8, and 16 CPUs. The performance of the model was evaluated by recording the computation time of each single simulation year for complete simulation runs (1,080 years). We conducted four different runs, one with only wind dispersal of seeds (SEED), one with seed and pollination (+POLL), and two different parallelised pollination computations (+POLL_PAR-A and B). First, we tried to simply hand over equally sized parts of the complete list of tree individuals including trees that do not have not produced seeds to the according selected number of CPUs (+POLL_PAR-A). In a second variant (+POLL_PAR-B), we tested attempted to decrease the potential computational overheads of idle CPUs that had finished their job faster because of
less few individuals that needed to estimate pollination for produced seed’s ovules, by cutting the list to only trees that produce seeds.

The computation time increases with the actual number of trees and seeds present in simulations. In consequence, we analysed the dependency between the time needed for each simulated year and the number of trees and, additionally, the number of produced seeds produced by generalised nonparametric regression (using the “gam”-function in R-package “gam”; Hastie, 2017). The dependent variable time $t$ was log-transformed prior to analysis. The explanatory variables – number of trees $N_t$ and seeds $N_s$ – were non-parametrically fitted and tested for non-linearity by comparing the deviance of a model that fits the terms linearly with a chi-squared test. In the initial model formula, we also included the interaction between the explanatory variables and excluded non-significant terms from the linear model ($p>0.05$) until yielding the final best model.

The code for estimating pollination probabilities, seed dispersal and tree density computation was parallelised using the OMP-library for C++ and we compared the reduction in computation time of simulations with 1, 4 and 8 CPUs.

3. Results

3.1. Verification of wind-dependency

The simulated seeds were solely dispersed in a north or south direction in coherence to the forcing winds (Fig. 2, Table S2 and S3). The median seed dispersal distances were ~12.2 m with a north wind and ~12.0 m with a south wind with a majority of 95% falling within ~43 m of the seed tree, but with rare (~0.1%) dispersal events >1,000 m (Fig. 2). The distance is equally highly correlated with the release height for both wind directions ($\rho =0.63$, $p<0.0001$; Fig. 2).

All simulated values were highly correlated to the directly estimated distances ($p>0.05$, Table S2; Fig. 2). The mean log-transformed simulated distances in a north or south direction were not different when comparing releasing trees of the same height ($p>0.05$, Table S3).

The pollination events were mainly coming from the direction of the forcing winds: however, ~18% deviated from the forcing wind direction (Table S42). This variance is introduced by the formulae used for calculating the pollination probability for each seed’s ovules on a tree and is further increased by the random (uniform) selection of a father out of a subset of all possible mature trees based on the probability density function. The median distance along forcing winds of ~38 m is, in general, shorter by ~3-5 m than in other directions (Table S42).

In north-central Siberia, the main wind directions observed during the vegetation period are a combination of both west and east (Fig. 3, upper row). In some years, one of these directions predominates, and is also characterised by stronger wind events. Accordingly, simulated seeds are dispersed into the general direction of the forcing wind data (Fig. 3, middle row). Dispersal distances can reach up to a maximum of several thousand kilometres, yet the majority of seeds fall within a few hundreds of metres, and these are dispersed over distances depicting the wind speeds as well.
The median pollen flight distances are generally larger than the seed's, with a technically fixed maximum of about the distance from the central plot to the borders (Fig. 3, lower row). Similar to seed dispersal, pollination follows the wind directions and fathers are positioned in the upwind direction of the main occurring winds.

### 3.2. Sensitivity analyses for implemented dispersal processes

The sensitivity analyses for the implemented dispersal processes, distances, simulated and expected from direct calculation, are more similar for those pollination directions with more samples, and only 4-6% of tests show significant differences. The higher values may be based on the uniform sampling of fathers and the associated smaller sample sizes in these directions. In all comparisons, we find no evidence that the differences are significant (Table S4).

Evaluation of dispersal processes seed dispersal function was extended for further model parameters that have an influence on the migration rate. In general, the four target variables have the same response direction towards changes in the parameters (Table 3). The stronger the changes, the more apparent becomes the change in the result so that the significances increases strongly from only 25% to 79%. The sensitivity values were of the same order of magnitude with the extreme values of -1.89 and 3.26 for each percent change in the input parameter. Most sensitive is the position of the peak recruitment for the observed migration rate (mean absolute sensitivity of 1.09 and 0.92 for 5 and 50%), whereas the impact on the stand level is of minor importance with sensitivities of only 0.28 and 0.19.

——The sensitivity values for resulting pollination distances for varied parameters were an absolute mean of change of 0.11 for 5% and 0.02 for 50% with the extremes of -0.08 and 0.30 (Table 4). The stronger the change, the more apparent is a change in the result (40 to 70% significant values), although the direction of the changes was similar. However, the change is a magnitude smaller when changed by 50% but the directions were consistent with those expected. Increasing Gregory’s $m$ led to farther pollination distances and vice versa for pollen descending velocity $V_d$, pollen. The sensitivities increased from the -0.07 to 0.09 on the southernmost plot to about -0.11 to 0.14 for the northernmost plot where also a higher proportion of significant values could also be observed.

In north-central Siberia, the main wind directions observed during the vegetation period are a combination of both west and east (Fig. 3, upper row). In some years, one of these directions predominates, and is also characterised by stronger wind events. Accordingly, simulated seeds are dispersed into the general direction of the forcing wind data (Fig. 3, middle row). Dispersal distances can reach up to a maximum of several thousand kilometres, yet the majority of seeds fall within a few hundreds of metres, and these are dispersed over distances depicting the wind speeds as well.

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3.2.3.3. Model performance

3.2.1.3.3.1. Memory consumption

The dynamic arrays need 120 bytes for each tree and 98 bytes for each seed. A further 54 bytes are needed for each of the environmental map tiles and another 117 bytes for the storage of output variables for each simulated year (Table S1). The constant containers use 390 bytes for the weather list and the parameter structures contain 642 bytes. On the basis of a simulated typical dense forest with ~92,000 seeds and ~25,000 tree individuals stored in the structures for each hectare, a simulation will need roughly ~15 MB of RAM in a setup of a 1,000 year initialising phase and a subsequent 80 year simulation phase.

3.2.2.3.3.2. Computation time

The simulation time increased with the number of trees in the simulation and for the contrasting simulation setups – either only wind-dependent seed dispersal SEED or also with the calculation of pollination +POLL (Fig. 4). The generalised additive model, including the number of seeds and a combination of the number of trees and number of seeds, explained the increase in computation time best and had the lowest AIC value among all simulation types (Table S65). All incorporated variables, namely number of trees and number of seeds, significantly explained the computation time. The number of trees is the most important explanatory variable at ~79.03%, followed by an interaction term of the number of trees and seeds at ~14.46%, and number of seeds at ~4.45% and a residual of ~2.017% unexplained variation.

Without including the pollination events, the computation takes ~0.6 s to calculate a year of a simulated plot on which 30,000 to 40,000 tree individuals are present (Fig. 4). In contrast, this increases to ~12048 s yr\(^{-1}\) for a similar stand when calculating the pollen donor for each produced seed (+POLL). The first implemented parallelisation of the pollination process (+POLL\_PAR A) shortened the computation time by roughly half to ~60 65 s yr\(^{-1}\) when using eight cores. The second variant (+POLL\_PAR B) outruns the first when using four to eight cores, and reaches a similar computation time using only four cores. The increase to 16 CPUs led to a further decrease of computation time only for the first variant.

4. Discussion

The assumption of unlimited seedbeds – allowing species in models to grow as soon as climate space allows them – causes high uncertainty in future predictions with dynamic global vegetation models (e.g. Midgley et al., 2007; Neilson et al., 2005; Sato and Ise, 2012). Implementing time-lagged responses in such models highlighted the need for a proper understanding and implementation of processes that limit species’ migrations (Snell, 2014; Snell and Cowling, 2015). To reveal and understand the underlying processes that cause time lags, we designed the model LAVESI that represents all life-cycle stages of larches in high detail from seeds to mature trees, producing seeds themselves, which are then distributed in the environment (Kruse et al., 2016). We built this model to simulate responses the Siberian treeline ecotone, which is solely covered over vast areas by a single tree species of the genus Larix. With this, it bears great potential to evaluate whether the difficulties caused e.g. by the plant functional type grouping many species with a variety of traits together as used in DGVMs (e.g. Huntley et al. 2010,
Lee 2011, Snell et al. 2014) can be overcome. Here we describe the model enhancements to achieve, for the first time, a coupled implementation of wind-driven seed dispersal and pollination in the larch forest simulator LAVESI. It can therefore be used for a very detailed evaluation of intra-stand processes determining migration speeds and help to improve abstract
dynamic global vegetation models (e.g. Sato et al., 2007; Sitch et al., 2003), forest landscape models (e.g. Seidl et al., 2012),
or regional forest gap models (e.g. Brazhnik and Shugart, 2015, 2016). Such a detailed representation of forest stands, as in the model presented here, is unlikely to be able to simulate forest dynamics on a continental to global scale (cf. Neilson et al., 2005). Nonetheless, the model can be used to parameterise dispersal kernels constraining inter-grid cell migration in DGVMs (Snell, 2014; Snell and Cowling, 2015) to achieve a better representation of processes constraining or enhancing the spread of a plant species.

We first tested the newly implemented functions for seed dispersal (Section 4.1) and pollination (4.2) by forcing simulations with one directional wind of constant speed. Then, the model was rerun with wind velocity profiles from the ERA-Interim data set (Balsamo et al., 2015) to test its behaviour under quasi-real conditions. In addition, we evaluated the model performance with the new processes (Section 4.3).

4.1. Wind-dependent seed dispersal

The simulated seed dispersal strictly followed the wind forcing and seeds settled in a downwind direction as expected, and not, as in the original model, in a purely ballistic manner (Kruse et al., 2016). We tested in a local sensitivity analysis the influence of different parameters for their influence on the stand level and the migration process. Sensitivity values were generally low with mean values between ~0.3 to 1.1, respectively at the stand level and for the migration rate. They are smaller compared to other parameters found in the sensitivity analysis of the first version of LAVESI by Kruse et al. (2016). In accordance with these findings, the new model is more sensitive to changes in parameters at transient stages such that higher values were found for the peak recruit position. Furthermore, only strong changes by 50% led in many case to significant changes in the results, strengthening the robustness of the model to the parameterisation. Those parameters leading to more available seeds and higher proportions of recruits (seed production rate, germination) had the highest sensitivity values and if increased they led to a faster migration and a stand infilling. As expected, the parameters seed release height, wind speed, distance ratio, and falls speed of propagules became significant for the migration rate but not for the local stand development. Seed dispersal is dependent on the release height of the seed (Matlack, 1987), which is low in the focus region (Wieczorek et al., 2017) and thus leads to low dispersal distances, compared to other taxa (González-Martínez et al., 2002, Pinus, 2006; Picea, Piotti et al., 2009). When winds are constantly blowing at 2.78 m s\(^{-1}\) (10 km h\(^{-1}\)), simulated distances seldom reach more than ~43 m and only on very rare occasions are they observed with distances exceeding 1,000 m. The dispersal kernel can thus be described as a combination of a Gaussian distribution, with its maximum fraction reaching a centre ~12 m metres from the releasing tree, and a long tail, best described by an exponential function. This aligns well with the implemented function in the model LAVESI (see details in Kruse et al., 2016). The model results are similar when driven with quasi-real wind data from the reanalysis data set ERA-Interim. The short seed dispersal distances depict well the generally
observed values of other larch species. For example, Duncan (1954) found for *Larix laricina* in the northern USA that 94% of seeds fell within 18 m of the releasing trees. Furthermore, Pluess (2011) found in dense forests of *Larix decidua* in the Swiss Alps an effective seed dispersal distance of 2–48 m. Moreover, the directions are now more realistically represented and follow the predominant west and east winds as expected (Fig. 3).

The use of winds from only the vegetation period might have introduced a bias, but it is based on the observation that this is the time when seeds are primarily dispersed (Abaimov, 2010). However, secondary dispersal by winds, due to uplift in strong winds, or travel in winter on frozen surfaces over long distances (Nathan et al., 2011a; cf. Pluess, 2011), or due to wind-independent animal-mediated zoochory (Evstigneev et al., 2017), is currently not represented but could facilitate the migration into tundra further. Also the wind regimes could have shifted their main wind direction from the past to the current setting and might even change in the future (Lisitzin, 2012; Trenberth, 1990). A change, for example, from north–south directions to the currently east–west wind directions, this we could have further slowdown limited the recent potential migration rate. This could explain the slow response of the treeline in northern Siberia to global warming, in addition to the long life-cycle of larches, as well as prevailing seed limitation in the north (Kruse et al., 2016; Wieczorek et al., 2017).

### 4.2. Pollination coupled to prevailing wind conditions

Pollen dispersal functions are frequently used to reconstruct vegetation composition from palaeo archives, for example in the Landscape Reconstruction Algorithm by Sugita et al. (2010), whereas other models have been used to track pollen clouds in tree stands (review in Jackson and Lyford, 1999; Prentice, 1985). Calculating every pollen dispersal event for each tree and seed is computationally challenging, but it can be simplified following the assumptions of Kuparinen et al. (2007). Hence, we implemented a density-dependent probability function and found in the sensitivity analysis that the pollination process was less affected by changing the input parameters than by the seed dispersal process. Values reached only a mean of ~0.02 when changed by 50% and increased from south to north, which covers a density gradient. Pollen influx from farther distances is more apparent in the more open stands, which furthermore is supported by the findings in the sensitivity analysis of the original model (Kruse et al., 2016). The pollination distance increases linearly with Gregory’s $m$, which increases the probability for farther standing trees, and decreases as expected for higher pollen descending velocities $V_d$. The density-dependent probability function assigns pollen donors mostly in an upwind direction, but also has a small angular scattering, which was introduced by the use of the von Mises distribution to capture the stochasticity of this process (Gregory, 1961; Kuparinen et al., 2007). This uncertainty could lead to an overestimation of pollination distances, but this seems unlikely because simulated pollen are travelling distances of ~38 m, which is longer compared to seeds and which is in concordance with observations (e.g. Pluess, 2011). However, the pollen amount and thus the probability of a distant tree to reach a seed–producing tree is dependent on the available resources and could further influence the resulting pollination distances. This relationship was not explicitly included but is partly covered by the use of the tree top height and with from this, better performing trees have a higher pollination probability. The pollination distance often reaches the maximal possible distance between two trees in our
simulation setup, which was the diagonal of the simulated area. These hypothetical pollen grains could probably reach distances of several hundred metres to kilometres, which would be in the range of the general dispersal distance observed in larches (Dow and Ashley, 1996; Hall, 1986). However, the current version of LAVESI-WIND is not yet fully parameterised to field data because pollen productivity and pollination distances as well as seed dispersal distances are to date not yet available for forests of the northernmost treeline area, but the next important step would be to evaluate validate the modelled seed dispersal and pollination processes with field-based data, and finally, to apply this model to achieve realistic predictions of a future treeline.

4.3. Model performance

The individual-based approach of the model LAVESI-WIND, with the extension of wind-dependent seed dispersal and pollination, bears a high potential of knowledge gain, but this comes with some challenges: (1) repeated calculations for millions of individuals (seeds and trees) are computationally intense (e.g. Snell et al. 2014, Svenning et al. 2014, Nabel 2015), and (2) they require a certain amount of memory during the simulation runs. Whereas the memory during each simulation run could be minimised to the needs of the simulation setup, the computational power was historically the limiting factor (Grimm and Railsback, 2005). But with the development of recent computer clusters with hundreds of CPUs, it seems very likely that one can overcome this, allowing us to use detailed and spatially explicit models at a regional scale (e.g. Paik et al., 2006; Zhao et al., 2013).

4.3.1. Memory consumption

We estimated the requirements for a hectare of a dense simulated forest as 15 MB of RAM. This means, on typical computer servers, even broad-scale simulation runs are easily feasible for 5,000 x 5,000 m, which would need ~38 GB RAM and takes approximately 40 hours. The current LAVESI-WIND version was not fully optimised to lower the needs of memory and many variables that might not be needed for a specialised simulation experiment could be excluded. Although, the original simulation program was not intended to be run over continuous square kilometres of forests (Kruse et al., 2016), this is already possible with the current version. The programming language C++ and the process-based structure of the code support an easy and fast forward development of this model.

4.3.2. Computation time needed for millions of trees, seeds and pollination

The computational effort of pollination for each seed’s ovule increases with the number of mature trees present on a simulated plot. Therefore, to allow simulations to be run on standard computers in manageable time, it was a major goal to minimise the time needed for each simulated year. To meet this requirement, we parallelised parts of the program code that are computationally intensive, namely the processes of pollination and seed dispersal. With our approach, we have been able to decrease the time so far by a factor of six when using 8 CPUs, in comparison to using only one. Still, overheads from using a standard template library (STL)-list container lead to a negative exponential progression of the computation time needed per
year rather than linear improvements (Fig. 4). Additional gains for other not yet parallelised processes are much smaller than these, but there is further potential to reduce the computation time by using different implementations of the parallelisation.

4.4. Potential model applications

The new model version LAVESI-WIND allows for the evaluation of the importance of driving processes, which determine the response speed of tree stands growing at the treeline in Siberia. With this, we can approach novel research questions, such as “Do wind regime shifts explain faster or slower migration rates in past climate changes?” Furthermore, one could test how different treeline types determine the migration behaviour in changing environments. These can vary widely, based on the treeline type, being abrupt or with stand densities decreasing with the abiotic gradient and might further be influenced by shrubs that respond faster responding to current climate warming (e.g. Frost and Epstein, 2014). In addition, this may be influenced by single-tree stands growing ahead of the migration front (Holtmeier and Broll, 2005). Further interesting questions could be addressed, such as the role of refugia during past glacial periods and their influence on present-day tundra colonisation by trees (Wagner et al., 2015), with a simplified and thus computational effective approach. Finally, by connecting the borders of a simulation plot along the meridional borders we already implemented boundary conditions that allow the simulation of south-to-north transects, which are representative of the treeline area where highest tree densities occur in the south and treeless areas in the north. Thus, with this model, past migration corridors and timings can be revealed by a landscape-scale simulation, potentially answering important questions of the past biogeography of larch species in Siberia.

Before applying this new model version, however, a proper parameterisation is necessary. Molecular methods can help to improve the seed dispersal function, especially microsatellite markers, which can uncover connections among subpopulations and even kinships by parentage analyses at the stand level, which would make the effective seed dispersal distances directly inferable (Ashley, 2010; Dow and Ashley, 1996; Piotti et al., 2009; Pluess, 2011). Additionally, these methods can be used to estimate the fat tail of the dispersal function indirectly (Piotti et al., 2009).

The dispersal potential is influenced by species’ traits, which are under selection and thus variable in time (Ackerly, 2003; Ronce, 2007). Trait variants that support a genetic lineage to disperse into new colonisable habitats can be superior when climate is warming and new habitats are available, and, vice versa, under colder climates, variants with a shorter dispersal distance potential that remain in refugia are superior. With this new model, the influence of this trait variability could be systematically assessed, because it is able to transmit maternal genetic information by seed dispersal and paternal genetic information via pollination.

Another interesting application would be to use this model to estimate the pollen influx in lakes (cf. Sugita, 2007). Pollen influx rates are widely used for vegetation reconstructions at the tundra-taiga transition zone (e.g. Klemm et al., 2016) and could now be used either to tune the dispersal parameters for a more precise population dynamics prediction, or inversely, to reconstruct ancient tree stands by simulations. Before the genetics or the influx rates are included in the model, however, a revision of boundary conditions for pollen in the model is necessary. This must include a relevant source area for the pollen...
(cf. Sugita, 2007) to determine to what extent genetic traits are delivered by pollen from beyond the borders of the simulated area. If this can be efficiently parameterised, the model could further be used to track genetic lineages in time.

Finally, by connecting the borders of a simulation plot along the meridional borders we already implemented boundary conditions that allow the simulation of south-to-north transects, which are representative of the treeline area where highest tree densities occur in the south and treeless areas in the north. Thus, with this model, past migration corridors and timings can be revealed by a landscape-scale simulation, potentially answering important questions of the past biogeography of larch species in Siberia.

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5. Conclusions

We conclude that it is feasible to implement wind-driven seed dispersal and pollination in an individual-based model, which is then able to run across broader areas. However, the simulated area and duration of the simulation are constrained by available computer power and memory, and thus further effort is needed to minimise the computational load of this model in order to allow landscape-scale simulations on a standard computer. With the new model setup, further applications in combination with the genetics of the represented species are now feasible and can bring us detailed knowledge about the behaviour of the treeline and the biogeography of larch species through time.

6. Code availability

7. Author contributions

S.K. and A.G. planned the study, N.K., A.G. and S.K. updated the model and implemented new functions. A.G. and S.K. performed the simulations and the statistical analysis. S.K. and A.G. wrote the manuscript. U.H. provided substantial advice in the process of data analysis and paper writing.

8. Competing interests

The authors declare no competing interests.

9. Acknowledgements

We acknowledge Sven Willner for valuable advice in the process of parallelising the program code and Cathy Jenks for proofreading and improving the manuscript. The position of Stefan Kruse is funded by the Helmholtz Initiative Fund.

10. References


11. Figures

Figure 1. Schematic representation of wind pollination as newly implemented in the LAVESI-WIND model. Based on actual winds, a distance-dependent pollination probability of ovules is estimated for each adult tree (father/potential pollen source) and for each seed source (mother) in the simulated area. The shaded areas on the ground represent the pollination probability for the labelled seed source for winds from the upper-right corner. These are generally higher for adult trees in upwind direction of the central seed source.

Figure 2. Dispersal distances of seeds are wind dependent and positively correlated with the height of the releasing tree. The simulated and hypothetically calculated dispersals were compared across evenly distributed height classes; the results are similar for north and south winds, and here the results with north winds are presented.
Figure 3. Wind forcing (upper row), simulated seed dispersal (middle row), and pollination distances (lowest row) by distance and cardinal direction. Simulations were performed on 200 x 200 m plots and seed dispersal events tracked away from source trees; pollination events were recorded from pollen donor trees standing in the plot area into the central plot of 20 x 20 m plot.
Figure 4. Simulation consumption time in relation to the number of trees present, the number of CPUs used, and for different types of parallelisation of the code. The time increases exponentially with the number of trees and more quickly when simulating the additional pollination (+POLL) compared with just the explicit seed dispersal (SEED). The inset summarises the simulation time for simulated typical northern taiga stands, ranging between 30,000 and 40,000 trees. The letters next to the boxes indicate similar groups inferred with a Wilcoxon-test and Holm correction for multiple testing.
## 12. Tables

Table 1. Overview of model parameters and processes for *L. gmelinii* individuals that are different from the original version (Kruse et al., 2016).

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value and dimension</th>
<th>References</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Growth</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Quadratic term of the equation for diameter growth rate</td>
<td>-0.003 ln(cm)/cm²</td>
<td>data-based estimate similar to Fyllas et al. (2010)</td>
</tr>
<tr>
<td>Linear term of the growth function</td>
<td>0.030 ln(cm)/cm</td>
<td></td>
</tr>
<tr>
<td>Constant term of the growth function</td>
<td>-1.98 ln(cm)</td>
<td></td>
</tr>
<tr>
<td><strong>Seed production, dispersal and establishment</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Factor of seed productivity</td>
<td>8</td>
<td>literature-based estimate (Kruklis &amp; Milyutin, 1977, cited in Abaimov, 2010)</td>
</tr>
<tr>
<td>Background germination rate</td>
<td>0.01</td>
<td>estimated, tuned</td>
</tr>
<tr>
<td>Horizontal seed dispersal distance at wind speed of 10 km/h</td>
<td>60.1 m</td>
<td>estimated after Matlack (1987)</td>
</tr>
<tr>
<td>Seed descent rate</td>
<td>0.86 m/s</td>
<td>estimated descent rate based on Matlack (1987)</td>
</tr>
<tr>
<td><strong>Mortality</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Background mortality rate</td>
<td>0.0001 yr⁻¹</td>
<td>data-based estimate</td>
</tr>
<tr>
<td>Current tree growth influence factor on tree mortality</td>
<td>0.0</td>
<td>tuned, estimated</td>
</tr>
<tr>
<td>Weather influence factor on tree mortality</td>
<td>0.1</td>
<td>tuned, estimated</td>
</tr>
<tr>
<td>Density influence factor on tree mortality</td>
<td>2.0</td>
<td>tuned, estimated</td>
</tr>
<tr>
<td>Seed fertility</td>
<td>2 years</td>
<td>Ban et al. (1998)</td>
</tr>
<tr>
<td>Mean temperature of the coldest month (January) at the border of the species’ geographical range</td>
<td>-45 °C</td>
<td>Shugart et al. (1992)</td>
</tr>
<tr>
<td>Exponent scaling the height influence</td>
<td>0.2</td>
<td>tuned, estimated</td>
</tr>
<tr>
<td><strong>Weather processing</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Exponent scaling the influence of surrounding density for a tree</td>
<td>0.1</td>
<td>tuned, estimated</td>
</tr>
<tr>
<td>Exponent scaling the density value</td>
<td>0.5</td>
<td>tuned, estimated</td>
</tr>
</tbody>
</table>
### Table 2. Parameter values evaluated in the sensitivity analysis for seed dispersal, migration patterns, and pollination.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Reference value and dimension</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Seed dispersal function</strong></td>
<td></td>
</tr>
<tr>
<td>Maximal flight distance for <em>L. gmelinii</em> seeds at 10 km h(^{-1}) (from Matlack, 1987)</td>
<td>60.1 m</td>
</tr>
<tr>
<td>Species-specific fall speed of propagules (<em>V(_d)</em>)</td>
<td>0.86 m s(^{-1})</td>
</tr>
<tr>
<td>Distance ratio weighing factor (<em>sdist</em>)</td>
<td>0.16</td>
</tr>
<tr>
<td>Factor of seed productivity (<em>f(_s)</em>)</td>
<td>8</td>
</tr>
<tr>
<td>Background germination rate (<em>f(_{Background Germination})</em>)</td>
<td>0.01</td>
</tr>
<tr>
<td>Influence factor of weather on germination rate (<em>f(_{Weather Germination})</em>)</td>
<td>0.447975</td>
</tr>
<tr>
<td>Maximum age of seeds (<em>age(_{Maximum Seeds})</em>)</td>
<td>2 yrs</td>
</tr>
<tr>
<td>Seed mortality rate on trees (in cones, <em>P(_{Seed Mortality, cones})</em> and at the ground, <em>P(_{Seed Mortality, Ground})</em>)</td>
<td>0.44724, 0.55803</td>
</tr>
<tr>
<td>Factor for release height estimation (<em>h(_r)</em>)</td>
<td>0.75</td>
</tr>
<tr>
<td>Factor for the actual wind direction (<em>(\bar{\theta})</em>)</td>
<td>1</td>
</tr>
<tr>
<td>Factor for wind speeds (<em>V(_w)</em>)</td>
<td>1</td>
</tr>
<tr>
<td>Probability of seed release from cones (<em>P(_{Seed Release})</em>)</td>
<td>0.63931</td>
</tr>
<tr>
<td><strong>Pollination</strong></td>
<td></td>
</tr>
<tr>
<td>Inverse of the von Mises distribution’s variance (<em>(\kappa)</em>)</td>
<td>10</td>
</tr>
<tr>
<td>Gregory’s parameter <em>C</em></td>
<td>0.6 cm(^{-1})(\cdot)0.5m</td>
</tr>
<tr>
<td>Gregory’s parameter <em>m</em></td>
<td>1.25</td>
</tr>
<tr>
<td>Pollen descending velocity (<em>V(_d), pollen</em></td>
<td>0.126 m s(^{-1})</td>
</tr>
<tr>
<td>Factor for the actual wind direction (<em>(\bar{\theta})</em>)</td>
<td>1</td>
</tr>
</tbody>
</table>
Table 3. Sensitivity values for varied model parameters influencing the seed dispersal process.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Sensitivity</th>
<th>Stand density</th>
<th>Forested area</th>
<th>Stemcount</th>
<th>Peak recruit position</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>S-5%</td>
<td>S+5%</td>
<td>S-50%</td>
<td>S+50%</td>
</tr>
<tr>
<td>Maximum Seeds</td>
<td>0.6±1.4</td>
<td>0.2±1.5</td>
<td>0.1±0.1</td>
<td>0.0±0.2</td>
<td>0.0±3.2</td>
</tr>
<tr>
<td>$V_d$</td>
<td>0.0±1.6</td>
<td>0.5±1.7</td>
<td>0.0±0.2</td>
<td>0.0±0.1</td>
<td>1±2.7</td>
</tr>
<tr>
<td>sdist</td>
<td>0.0±1.4</td>
<td>0.2±1.6</td>
<td>0.1±0.2</td>
<td>0.0±0.1</td>
<td>0.2±2.8</td>
</tr>
<tr>
<td>$f_s$</td>
<td>-0.2±1.6</td>
<td>0.7±1.5</td>
<td>-0.6±0.1</td>
<td>0.4±0.2</td>
<td>-0.8±3.3</td>
</tr>
<tr>
<td>$f_{Background Germination}$</td>
<td>0.2±1.5</td>
<td>0.6±1.7</td>
<td>0.0±0.1</td>
<td>0.1±0.2</td>
<td>0.0±3.5</td>
</tr>
<tr>
<td>$f_{Weather Germination}$</td>
<td>-0.1±1.6</td>
<td>0.6±1.5</td>
<td>-0.5±0.1</td>
<td>0.3±0.2</td>
<td>-0.6±3.6</td>
</tr>
<tr>
<td>ageMaximum Seeds $1$</td>
<td></td>
<td>-0.4±0.1</td>
<td>0.2±0.2</td>
<td>0±1.8</td>
<td>-1.1±0.2</td>
</tr>
<tr>
<td>$P_{Seed Mortality, Cones}$</td>
<td>0.6±1.6</td>
<td>-0.3±1.6</td>
<td>0.3±0.2</td>
<td>-0.5±0.1</td>
<td>0.6±3</td>
</tr>
<tr>
<td>$P_{Seed Mortality, Ground}$</td>
<td>0.1±1.5</td>
<td>-0.1±1.3</td>
<td>0.2±0.2</td>
<td>-0.1±0.1</td>
<td>0.1±3</td>
</tr>
<tr>
<td>$H_t$</td>
<td>0.4±1.3</td>
<td>0.2±1.7</td>
<td>0.0±0.2</td>
<td>0.0±0.1</td>
<td>0.1±3.1</td>
</tr>
<tr>
<td>$\bar{\theta}$</td>
<td>0.0±1.4</td>
<td>0.2±1.4</td>
<td>0.0±0.2</td>
<td>0.0±0.2</td>
<td>-0.4±2.2</td>
</tr>
<tr>
<td>$V_w$</td>
<td>0.1±1.6</td>
<td>0.1±1.7</td>
<td>0.1±0.2</td>
<td>0.0±0.1</td>
<td>0.2±2.9</td>
</tr>
<tr>
<td>$P_{Seed Release}$</td>
<td>-0.1±1.5</td>
<td>0.4±1.7</td>
<td>-0.5±0.1</td>
<td>0.3±0.2</td>
<td>-0.1±2.9</td>
</tr>
</tbody>
</table>

1The integer variable maximum age of seeds was excluded from the 5% change sensitivity analysis having as only for 50% changes had valid values.
Table 4. Sensitivity values of the model’s results assessed by mean distance per pollination event into an area of 20 x 20 m in the north, middle, and south of 100-m-wide and 1-km-long transects. Bold values are highly significant with $p<0.01$, italic with $p<0.05$, and grey values non-significantly different from the reference run.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Sensitivity</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>S-5%</td>
</tr>
<tr>
<td>North (influx from south)</td>
<td></td>
</tr>
<tr>
<td>$\kappa$</td>
<td>-0.05±0.33</td>
</tr>
<tr>
<td>$C$</td>
<td>0.08±0.31</td>
</tr>
<tr>
<td>$m$</td>
<td>0.07±0.28</td>
</tr>
<tr>
<td>$V_{d, pollen}$</td>
<td>0.05±0.31</td>
</tr>
<tr>
<td>$\theta$</td>
<td>0.05±0.31</td>
</tr>
<tr>
<td>Middle (influx from all directions)</td>
<td></td>
</tr>
<tr>
<td>$\kappa$</td>
<td>0.02±0.54</td>
</tr>
<tr>
<td>$C$</td>
<td>0.1±0.58</td>
</tr>
<tr>
<td>$m$</td>
<td>-0.04±0.61</td>
</tr>
<tr>
<td>$V_{d, pollen}$</td>
<td>0.07±0.69</td>
</tr>
<tr>
<td>$\theta$</td>
<td>0.01±0.66</td>
</tr>
<tr>
<td>South (influx from north)</td>
<td></td>
</tr>
<tr>
<td>$\kappa$</td>
<td>0.03±0.43</td>
</tr>
<tr>
<td>$C$</td>
<td>-0.01±0.4</td>
</tr>
<tr>
<td>$m$</td>
<td>-0.07±0.41</td>
</tr>
<tr>
<td>$V_{d, pollen}$</td>
<td>0.08±0.39</td>
</tr>
<tr>
<td>$\theta$</td>
<td>-0.05±0.36</td>
</tr>
</tbody>
</table>

Table 2. Pollination event comparison between simulated and expected values. The statistics are based on 50 simulation repeats. Significant differences between expected and simulated distances tested with a Welch two-sample t-test.

<table>
<thead>
<tr>
<th>Cardinal direction of winds</th>
<th>Direction of pollination [°]</th>
<th>Distance (simulated/expected) [m]</th>
<th>Fraction of observations (simulated/expected) [%]</th>
<th>Fraction of significant differences</th>
</tr>
</thead>
<tbody>
<tr>
<td>North</td>
<td>135-165</td>
<td>44.32/43.79</td>
<td>9.00/8.39</td>
<td>20%</td>
</tr>
<tr>
<td></td>
<td>165-195</td>
<td>39.03/38.90</td>
<td>81.53/82.68</td>
<td>4%</td>
</tr>
<tr>
<td></td>
<td>195-225</td>
<td>40.03/40.19</td>
<td>9.47/8.93</td>
<td>14%</td>
</tr>
<tr>
<td>South</td>
<td>315-345</td>
<td>40.94/40.47</td>
<td>7.55/7.92</td>
<td>12%</td>
</tr>
<tr>
<td></td>
<td>-15-15</td>
<td>36.98/37.90</td>
<td>82.92/82.8</td>
<td>6%</td>
</tr>
<tr>
<td></td>
<td>15-45</td>
<td>42.76/40.84</td>
<td>9.51/9.28</td>
<td>22%</td>
</tr>
<tr>
<td></td>
<td>45-75</td>
<td>53.80/-</td>
<td>0.01/0.00</td>
<td>#</td>
</tr>
</tbody>
</table>

* only one observation, thus excluded from further analyses.
1. Supplement

1.1. Verification of wind-dependency

1.1.1. Simulation setup

The simulation experiments were conducted on a 200 x 200 m plot using the model with the new processes for verification. Populations were initiated on empty areas by randomly distributing a fixed number of seeds during the first 100 years of a 1,000 year long stabilisation period. The simulation model randomly drew weather conditions for each year from the complete available period 1934–2013 during the stabilisation period. In the final 80 simulation years, the actual weather data were used. First, we performed simulation experiments with constant wind conditions to verify the implemented dispersal processes. Wind forcing was from the north or from the south, both with a constant wind speed of 10 km h\(^{-1}\). Simulations were repeated 50 times with an input of 250 seeds per year during initialisation.

Second, we evaluated the functionality of the seed dispersal function by forcing the model with wind data from the reanalysis data set ERA-Interim (Balsamo et al., 2015). Simulations were repeated 10 times and population growth initiated by introducing 100 seeds per year during initialisation. The dispersal distance and direction as well as the release height of every 100\(^{th}\) seed dispersal event were recorded during each year of the complete simulation run. Pollination was assessed by recording the distance and direction from the selected pollen sources to the seed positions prior to seed release of all tree individuals present at the final year of the simulation.

1.1.2. Evaluation of dispersal processes

The seed dispersal and pollination distances were evaluated by calculating the mean dispersal distances for both processes in bins of 30° cardinal directions over the complete simulation run for years with available wind data (1979–2012). In addition, we selected two years with contrasting wind patterns, the year 1990 with predominant winds from the Eeast, and 1998 from the wWest. The results were qualitatively compared to observed values from the literature. During the simulations, we recorded only one pollination event per tree per year reaching the central area of 20 x 20 m of the plot and every 100\(^{th}\) seed dispersal event.

1.1.3. Analyses

We verified the wind-dependent seed dispersal by comparing the simulation results with the simulated results from the implemented dispersal function and refer to these values as ‘expected’. Therefore, we estimated the dispersal distances with the implemented dispersal functions (seeds Eq.1 and pollen Eq.5) under the same conditions as used for driving the model, namely winds from north or south with a constant speed of 10 km h\(^{-1}\). The observed mean log-transformed (to achieve normal distribution) dispersal distances were compared to each other with a Welch two-sample t-test. We compared simulated to expected dispersal distances in each wind direction in height classes of trees in 10% steps of the sorted values, excluding the
minimum and maximum values where only few observations could be recorded. The simulated data values in the range of ±5% at the determined height classes were first tested for an interaction between the release height and the dispersal distance with a Spearman’s rank-based measure of association (rho) and a t-test. Then we compared the simulated distances for each height class to the expected distances, both log-transformed prior to analysis, with a t-test. Furthermore, we compared the dispersal in both directions to each other using the same procedure.

The simulated pollination distances were compared to estimates from the implemented function under the same conditions, namely the adult tree’s position and constant north or south winds with a speed of 10 km h⁻¹. The resulting three-dimensional pollination distribution probabilities at simulation year 2011 (first year of field-work) were binned to cardinal directions in steps of 30°, starting with North between 345° and 15°. The simulated and directly estimated log-transformed pollination distances were tested for differences in each individual direction with a Welch two-sample t-test for cases with > 10 observations. We tested whether the mean of the p-values is significantly greater than 0.01 with a Student t-test.

1.1.4. Results

All simulated values were highly correlated to the directly estimated distances (p>0.05, Table S2; Fig. 2). The mean log-transformed simulated distances in a north or south direction were not different when comparing releasing trees of the same height (p>0.05, Table S3).

The distances, simulated and expected from direct calculation, are more similar for those pollination directions with more samples, and only 4-6% of tests show significant differences (Table S4). The higher distance values for these directions may be based on the uniform sampling of fathers and the associated smaller sample sizes in these directions. In all comparisons, we find no evidence that the differences are significant (Table S5).

<table>
<thead>
<tr>
<th>Structure</th>
<th>Substructure</th>
<th>Total for each element in structure [b]</th>
<th>Total in each simulation [kb]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Parameter</td>
<td></td>
<td>642</td>
<td>0.64</td>
</tr>
<tr>
<td>Weather¹</td>
<td>Year(i)</td>
<td>390</td>
<td>31.2</td>
</tr>
<tr>
<td>Environment²</td>
<td>Grid(i)</td>
<td>54</td>
<td>2,700</td>
</tr>
<tr>
<td>Trees³</td>
<td>Tree(i)</td>
<td>120</td>
<td>3,000</td>
</tr>
<tr>
<td>Seeds⁴</td>
<td>Seed(i)</td>
<td>98</td>
<td>9,016</td>
</tr>
<tr>
<td>Evaluation⁵</td>
<td>Evaluation(i)</td>
<td>117</td>
<td>105.86</td>
</tr>
<tr>
<td><strong>TOTAL</strong></td>
<td></td>
<td><strong>14,853.7</strong></td>
<td></td>
</tr>
</tbody>
</table>

1: with 80 years of weather input data on a monthly basis;
2: 50,000 grid tiles at a resolution of 20 x 20 cm tiles on a hectare;
3: ~25,000 larch individuals appear per hectare in simulations of a typical dense forest plot;
4: ~92,000 larch seeds are present on a hectare of a typical dense forest plot simulation;
5: the length of the simulation is calculated with 1,000 years stabilization and 80 years simulation phase.
Table S2. — Comparison of simulated to directly estimated seed dispersal from the implemented functions of north and south winds at the same observed release heights calculated for each direction separately.

<table>
<thead>
<tr>
<th>Wind direction</th>
<th>Tree height [cm]</th>
<th>Significance value (p)</th>
<th>Degrees of freedom</th>
<th>Statistic value (t)</th>
<th>Distances percentile [m]</th>
<th>0%</th>
<th>1%</th>
<th>25%</th>
<th>50%</th>
<th>75%</th>
<th>99%</th>
<th>100%</th>
</tr>
</thead>
<tbody>
<tr>
<td>North</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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<td></td>
</tr>
<tr>
<td>215</td>
<td>0.405</td>
<td>1067</td>
<td>0.832</td>
<td>0.1 0.8 4.0 6.2 9.1 60.8 214,580.7</td>
<td></td>
<td></td>
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</tr>
<tr>
<td>274</td>
<td>0.272</td>
<td>1049</td>
<td>1.100</td>
<td>0.1 0.9 5.1 7.9 11.4 58.5 839,991.5</td>
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<td></td>
<td></td>
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<td></td>
</tr>
<tr>
<td>337</td>
<td>0.317</td>
<td>1048</td>
<td>-1.001</td>
<td>0.1 1.2 6.2 9.7 13.9 65.4 106,316.3</td>
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</tr>
<tr>
<td>406</td>
<td>0.356</td>
<td>1034</td>
<td>-0.924</td>
<td>0.1 1.5 7.6 11.7 16.7 70.7 7,540,295.2</td>
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<tr>
<td>486</td>
<td>0.119</td>
<td>1027</td>
<td>-1.561</td>
<td>0.2 1.7 9.0 13.8 19.9 75.6 1,800,875.2</td>
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</tr>
<tr>
<td>580</td>
<td>0.971</td>
<td>1038</td>
<td>-0.036</td>
<td>0.2 2.0 10.8 16.6 23.7 79.8 295,290.7</td>
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<tr>
<td>698</td>
<td>0.815</td>
<td>1047</td>
<td>0.234</td>
<td>0.2 2.4 12.8 20.0 28.3 90.7 366,330.3</td>
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<tr>
<td>860</td>
<td>0.393</td>
<td>1056</td>
<td>0.855</td>
<td>0.1 3.0 15.8 24.5 35.0 99.6 22,430,488.9</td>
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<td></td>
<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>South</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
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</tr>
<tr>
<td>214</td>
<td>0.328</td>
<td>1081</td>
<td>0.979</td>
<td>0.1 0.8 4.0 6.3 9.1 54.8 142,464.5</td>
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<tr>
<td>270</td>
<td>0.049</td>
<td>1054</td>
<td>1.969</td>
<td>0.1 0.9 5.0 7.8 11.3 56.0 1,386,968.5</td>
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<tr>
<td>330</td>
<td>0.721</td>
<td>1054</td>
<td>-0.358</td>
<td>0.1 1.2 6.2 9.5 13.7 65.2 316,950.6</td>
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<tr>
<td>397</td>
<td>0.796</td>
<td>1045</td>
<td>0.258</td>
<td>0.1 1.4 7.4 11.4 16.3 67.7 3,506,206.1</td>
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<tr>
<td>476</td>
<td>0.440</td>
<td>1040</td>
<td>-0.772</td>
<td>0.1 1.7 8.8 13.6 19.4 69.2 15,711,413.0</td>
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<td></td>
<td></td>
</tr>
<tr>
<td>570</td>
<td>0.794</td>
<td>1036</td>
<td>0.262</td>
<td>0.1 2.0 10.6 16.4 23.3 78.3 160,559.1</td>
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<tr>
<td>685</td>
<td>0.361</td>
<td>1033</td>
<td>-0.914</td>
<td>0.2 2.5 12.6 19.7 27.9 89.0 1,290,583.5</td>
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<td></td>
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<td></td>
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<tr>
<td>851</td>
<td>0.306</td>
<td>1058</td>
<td>-1.025</td>
<td>0.2 2.9 15.7 24.3 34.6 104.8 1,459,702.6</td>
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<td></td>
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<td></td>
<td></td>
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<td></td>
</tr>
</tbody>
</table>
Table S3. Comparison of seed dispersal distances in simulations forced with winds from north and south directions.

<table>
<thead>
<tr>
<th>Wind direction</th>
<th>Tree height [cm]</th>
<th>Distances percentile</th>
<th>Significance value (p)</th>
<th>Degrees of freedom D. f.</th>
<th>Statistic value (t)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>0% 1% 25% 50% 75% 99% 100%</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>North</td>
<td>215</td>
<td>0.1 0.7 4.0 6.2 9.0 60.2 21.4,580.7</td>
<td>0.336</td>
<td>58,956</td>
<td>-0.961</td>
</tr>
<tr>
<td>South</td>
<td></td>
<td>0.1 0.8 4.0 6.3 9.1 55.9 14.2,464.5</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>North</td>
<td>272</td>
<td>0.1 0.9 5.1 7.8 11.3 58.8 9.4,025.3</td>
<td>0.235</td>
<td>88,336</td>
<td>-1.189</td>
</tr>
<tr>
<td>South</td>
<td></td>
<td>0.1 0.9 5.1 7.9 11.3 58.3 13.8,968.5</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>North</td>
<td>333</td>
<td>0.1 1.2 6.1 9.6 13.8 65.0 10.6,316.3</td>
<td>0.047</td>
<td>59,926</td>
<td>-1.985</td>
</tr>
<tr>
<td>South</td>
<td></td>
<td>0.1 1.2 6.2 9.6 13.9 67.1 31.6,950.6</td>
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<td></td>
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<td>North</td>
<td>402</td>
<td>0.1 1.4 7.5 11.6 16.5 71.2 7.5,4,295.2</td>
<td>0.164</td>
<td>100,519</td>
<td>1.393</td>
</tr>
<tr>
<td>South</td>
<td></td>
<td>0.1 1.4 7.4 11.5 16.4 68.6 22.6,0,443.8</td>
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<tr>
<td>North</td>
<td>481</td>
<td>0.2 1.7 8.9 13.7 19.7 73.8 1.8,0,875.2</td>
<td>0.388</td>
<td>101,366</td>
<td>0.864</td>
</tr>
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<td>South</td>
<td></td>
<td>0.1 1.7 8.9 13.7 19.6 70.3 32.2,285.9</td>
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<td>North</td>
<td>575</td>
<td>0.1 2.0 10.7 16.5 23.5 80.5 29.5,290.7</td>
<td>0.565</td>
<td>101,072</td>
<td>0.576</td>
</tr>
<tr>
<td>South</td>
<td></td>
<td>0.1 2.0 10.7 16.6 23.6 79.8 16.0,559.1</td>
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<td></td>
<td></td>
</tr>
<tr>
<td>North</td>
<td>692</td>
<td>0.2 2.4 12.7 19.8 28.1 91.8 36.3,330.3</td>
<td>0.230</td>
<td>92,599</td>
<td>-1.201</td>
</tr>
<tr>
<td>South</td>
<td></td>
<td>0.2 2.5 12.8 19.9 28.2 89.8 12.9,0,583.5</td>
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<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>North</td>
<td>856</td>
<td>0.1 3.0 15.7 24.4 34.8 99.3 90.1</td>
<td>0.921</td>
<td>74,922</td>
<td>0.100</td>
</tr>
<tr>
<td>South</td>
<td></td>
<td>0.2 2.9 15.7 24.5 34.7 105.8 1.45,9,702.7</td>
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</table>

Table S4. Pollination event comparison between simulated and expected values. The statistics are based on 50 simulation repeats. Significant differences between expected and simulated distances tested with a Welch two-sample t-test.

<table>
<thead>
<tr>
<th>Cardinal direction of winds</th>
<th>Direction of pollination [°]</th>
<th>Distance (simulated/expected) [m]</th>
<th>Fraction of observations (simulated/expected) [%]</th>
<th>Fraction of significant differences</th>
</tr>
</thead>
<tbody>
<tr>
<td>North</td>
<td>135-165</td>
<td>44.32/43.79</td>
<td>9.00/8.39</td>
<td>20%</td>
</tr>
<tr>
<td>South</td>
<td>165-195</td>
<td>39.03/38.90</td>
<td>81.53/82.68</td>
<td>4%</td>
</tr>
<tr>
<td>South</td>
<td>195-225</td>
<td>40.03/40.19</td>
<td>9.47/8.93</td>
<td>14%</td>
</tr>
<tr>
<td>South</td>
<td>315-345</td>
<td>40.94/40.47</td>
<td>7.55/7.92</td>
<td>12%</td>
</tr>
<tr>
<td>South</td>
<td>345-15</td>
<td>36.98/37.90</td>
<td>82.92/82.8</td>
<td>6%</td>
</tr>
<tr>
<td>South</td>
<td>15-45</td>
<td>42.76/40.84</td>
<td>9.51/9.28</td>
<td>22%</td>
</tr>
<tr>
<td>South</td>
<td>45-75</td>
<td>53.80/-</td>
<td>0.01/0.00</td>
<td>*</td>
</tr>
</tbody>
</table>

* only one observation, thus excluded from further analyses.
Table S4-Table S5.— Comparison of pollination dispersal distances with Student’s t-test of the mean p-values at a significance level of 0.01. Only cases with >10 pollination events of the five trees producing most seeds were considered.

<table>
<thead>
<tr>
<th>Cardinal direction of winds</th>
<th>Wind direction [°]</th>
<th>Mean p-value</th>
<th>Significance value (p)</th>
<th>d.f. Degrees of freedom</th>
<th>Statistic value (t)</th>
</tr>
</thead>
<tbody>
<tr>
<td>North</td>
<td>165-195</td>
<td>0.449</td>
<td>&lt;0.001</td>
<td>49</td>
<td>10.133</td>
</tr>
<tr>
<td></td>
<td>135-165</td>
<td>0.277</td>
<td>&lt;0.001</td>
<td>38</td>
<td>5.629</td>
</tr>
<tr>
<td></td>
<td>195-225</td>
<td>0.406</td>
<td>&lt;0.001</td>
<td>37</td>
<td>6.704</td>
</tr>
<tr>
<td>South</td>
<td>345-15-15</td>
<td>0.415</td>
<td>&lt;0.001</td>
<td>49</td>
<td>10.171</td>
</tr>
<tr>
<td></td>
<td>15-45</td>
<td>0.302</td>
<td>&lt;0.001</td>
<td>40</td>
<td>5.734</td>
</tr>
<tr>
<td></td>
<td>315-345</td>
<td>0.408</td>
<td>&lt;0.001</td>
<td>39</td>
<td>8.315</td>
</tr>
<tr>
<td>Simulation version</td>
<td>Model formula</td>
<td>Aikaike’s Information Criterion (AIC)</td>
<td>Dispersion parameter for Gaussian family</td>
<td>Model term</td>
<td>D.f. Degree of freedom</td>
</tr>
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<td>---------------</td>
<td>---------------------------------------</td>
<td>------------------------------------------</td>
<td>------------</td>
<td>-----------------------</td>
</tr>
<tr>
<td><strong>+POLLEN_PAR A</strong></td>
<td>$t^\sim Nt$</td>
<td>9644722</td>
<td>0.17</td>
<td>$Nt$</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>$t^\sim Ns$</td>
<td>10424167</td>
<td>0.29</td>
<td>$Ns$</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>$t^\sim Nt+Ns$</td>
<td>11674042</td>
<td>0.15</td>
<td>$Nt$</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td>$t^\sim Nt+Ns$</td>
<td>1722964</td>
<td>0.14</td>
<td>$Nt$</td>
<td>1</td>
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<td></td>
<td></td>
<td>$Ns$</td>
<td>1</td>
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<td>$Nt:Ns$</td>
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</tr>
<tr>
<td><strong>+POLLEN</strong></td>
<td>$t^\sim Nt$</td>
<td>8844754</td>
<td>0.17</td>
<td>$Nt$</td>
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<tr>
<td></td>
<td>$t^\sim Ns$</td>
<td>9754183</td>
<td>0.29</td>
<td>$Ns$</td>
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<tr>
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<td>$t^\sim Nt+Ns$</td>
<td>1183925</td>
<td>0.14</td>
<td>$Nt$</td>
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<td>$Ns$</td>
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<td>$Nt:Ns$</td>
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<tr>
<td><strong>+POLLEN_PAR B</strong></td>
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<td>$Nt$</td>
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<tr>
<td></td>
<td>$t^\sim Ns$</td>
<td>8331045</td>
<td>0.25</td>
<td>$Ns$</td>
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<td>1045833</td>
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<td>$Ns$</td>
<td>1</td>
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<td>$Nt:Ns$</td>
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<tr>
<td><strong>SEED</strong></td>
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<td>-40340</td>
<td>0.05</td>
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<td>$t^\sim Ns$</td>
<td>-375231</td>
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<td>$Ns$</td>
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<td>$t^\sim Nt+Ns$</td>
<td>-233275</td>
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<td>$Nt$</td>
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<td>$Ns$</td>
<td>1</td>
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<td>$Nt:Ns$</td>
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</tbody>
</table>

*Table S5: Table S6.* Test statistics for generalised nonparametric regression analyses (significance level: *** p<0.001).