Dear Editor,

in this document we report our point-by-point replies to the anonymous Referee and your comments, and the marked-up version of the manuscript (attached at the end).

We have implemented all the minor comments of the Referee and yours. We did not address completely the comments about the “detrained ice” issue raised by the Referee as it goes beyond the scope of this manuscript.

Best regards,

Sara Bacer
Reply to the Referee’s comments

We really appreciate the careful work of revision carried out by the Referee and we are grateful for the helpful comments. Below there are our replies.

Major Issue

Detraining ice water content, but not ice crystal number.

We explained the issue raised by the Referee in Subsection 2.1 (EMAC model), between L1 and L9 P5. We notice that we did not specify that the CLOUD submodel assumes a temperature dependent radius to estimate the ice crystal number from ice mass detrained from convection. Thus, we substituted the sentence at L10, P5 (“The size and numbers of the detrained condensate are not taken into account explicitly”) with:

“The number of detrained ice crystals is estimated from the ice condensate detrained from convection by assuming an only temperature dependent radius.”

Nevertheless, the ice crystal size and the detrainment from convection such as the distinction of liquid vs. in-situ formed ice go beyond the scope of this manuscript and will be subject of future studies.

We also changed the sentence at L19-20 P14 from: “This is probably caused by the bigger radii of the newly formed ice crystals simulated in this area, both by KL02 and BN09” to “This is probably caused by the larger radius of ice crystals simulated in this area” since we cannot exclude that also the radius of detrained ice crystals is too large (unfortunately, this radius is not an output of our simulations).

Minor Comments

General comment: ICNC changes.

• I am puzzled to see how little the ICNC burden for cirrus clouds changed. Why is that? What confuses me is that you take the 200 hPa level as representative for cirrus. However, the ICNC changes there are significantly different compared with the integrated ICNC burden for cirrus.

ICNC\textsubscript{burden} is the vertical integration of ice crystal number concentrations derived from different sources, ice nucleation but also convective detrainment, instantaneous freezing, and secondary ice production. On the other hand, ICNC at 200 hPa is mainly produced by ice nucleation, and partially by convective detrainment and instantaneous freezing (we do not to show plots about this because they are part of a future work). Thus, it is correct to expect that ICNC\textsubscript{burden} changes are different from ICNC changes (which are mainly due to the different ice nucleation schemes used in the cirrus regime).

• I think you actually nicely prepared the answer to my question with Figure 4 in the response document to reviewer 1. I find the binning by temperature very informative. Could you add one in the paper and comment it briefly in the text? It would be great to see the anomalies of BN+LD, KL+BN, and BN+BN with respect to DEF. Also, I like its right panel too as it clearly summarizes the main ice crystal number changes (if you extended it to the lowest temperature range).

I think extending the panel beyond 30S, where the heterogeneous freezing doesn’t occur too frequently, should also not affect its general interpretation. Maybe this right panel with the extended temperature range alone would be enough to strengthen some of your conclusions, if you include it in the manuscript.
We plotted the annual zonal means as functions of latitude and temperature and the absolute changes (extending the lower temperature range) as requested by the Referee, see Figure 1 of this file. The last row of plots considers the averages computed over different latitudinal coverages: 90S – 90N and 25S – 27N (i.e. the same considered in the comparison with flight measurements in Figure 5 of the manuscript). Indeed, the absolute changes show a similar behaviour (as said by the Referee). Since Figure 1 is equivalent to Figure 2 of the manuscript, we added it in the supplement file and wrote the following sentences:

“The absolute changes of ICNC annual zonal means computed as a function of latitude and temperature (Figure S1 in the supplement file) show that ICNCs in BN+KL are lower than the default case by 300 \( L^{-1} \) at temperatures below 220 K.” (at L13 P11 of the manuscript).

“This is also evident from Figure S1 in the supplement file (last row), where the absolute changes are, in average, between 200 and -200 \( L^{-1} \) when BN09 is used in the cirrus regime and between 50 and -50 \( L^{-1} \) when comparing KL+BN with KL+LD.” (at L3 P12 of the manuscript).

• To sum up, I miss a discussion in section 3.1 (and conclusions) which is more clearly pointing at the (1) ICNC increase in mixed phase due to heterogeneous freezing, (2) ICNC increase around 230 K due to heterogeneous freezing in cirrus, (3) ICNC decrease at the coldest temperatures due to the PREICE effect. Is there a way you could prove the last point? It sounds plausible from the text, however, a more direct proof would strengthen your findings.

We addressed the first point at L19-21 P11.

Regarding the second point, we did not write explicitly about this ICNC increase which is close to the transition between the two cloud regimes. However, as the heterogeneous contribution is very small in comparison with the homogeneous nucleation (not shown), it is more likely that the ICNC increase is due to a faster sedimentation of larger IC from higher altitudes, as written at L20-21 P11.

We already addressed the third point at L14-15 P11 and later in Subsection 4.2 (P18). To prove that ICNC decreases at lower temperatures because of the PREICE effect, we compared two simulations (using the BN+BN configuration) with and without the PREICE effect. The difference has a pattern really similar to Figure 2d (ICNC: BN+BN vs DEF). Therefore, we have a confirmation that the differences at those altitudes/temperatures are due to the PREICE effect. This information will be part of a future study.

P2 L31-33: Homogeneous nucleation is dominant? Yes, but based on some modelling studies. Not all of them. At least that’s what one of the authors nicely showed in a previous study (see plot below from Barahona et al., 2017). Of course, I would agree that homogeneous nucleation is the dominant source of ice crystal number or similar statements, but not when looking at ice crystal nucleation events.

We slightly changed the sentence and added some citations:

“In several modeling studies, homogeneous nucleation has been considered the dominant process for cirrus formation (e.g. Haag et al., 2003; Hendricks et al. 2011; Gettelman et al., 2012; Barahona et al. 2014) because ... ”

P4 L33: You referenced the wrong Tost et al., 2006 paper (looking at the references).

Do you use the scheme of Tiedtke 1989 or Tiedtke 1989 with modifications from Nor-
Thanks for noticing it. We corrected the reference in the revised version.
We used the Tiedtke (1989) scheme with modifications by Nordeng (1994). We specified it at L33 P4:
“In this work the scheme of Tiedtke (1989) with modifications by Nordeng (1994) has been used.”

P7 L20: “The only expedient adopted by the CLOUD submodel is...” That word (expedient) does not make sense in the context used. Please use simple and understandable words instead.

We made the sentence simpler: “Finally, the influence of the pre-existing ice particles is not taken into account. The CLOUD submodel simply reduces the number of aerosol particles available for ice nucleation by the existing ice particle number in the cirrus regime”.

P11 L18: Cziczo et al., 2009 is not a good reference for northern hemisphere, being dominated by heterogeneous nucleation, as it talks/speculates about lead-containing natural dust. Li et al., 2012, Storelvmo et al., 2014, Gasparini et al., 2016 and also Barahona et al., 2017 show some of that, although being highly model and parameterization dependent.

Thanks for pointing it out. We cited: “Li et al., 2012; Kuebbeler et al. 2014; Storelvmo et al., 2014; Shi et al. 2015; Gasparini et al., 2016; Barahona et al., 2017”.

P12 L29-30: “Such a reduction occurs mostly because of the PREICE effect, being the ice crystals mainly of homogeneous origin at this altitude” Please rephrase this sentence as it is not grammatically correct.

We changed the sentence to: “As the ice crystals are mainly of homogeneous origin at this altitude, such a reduction is probably due to the PREICE effect.”

P14 L13-14: Could you add a sentence explaining why the mixed-phase is less sensitive to the change in ice nucleation scheme?

In the model, ICNC is the sum of tendencies associated to different processes, such as sedimentation, secondary ice production, aggregation, ice nucleation. A possible explanation is that the rate associated to heterogeneous nucleation has a low effect, in comparison to the other processes, on the final ICNC. Thus, ICNC is only slightly perturbed from the choice of the ice nucleation scheme used in the mixed-phase regime.

We added the following sentence in the manuscript at L3 P12:
“Possibly, the rate associated to heterogeneous nucleation in the mixed-phase regime is masked by other processes, like sedimentation and aggregation, which also contribute to ICNC in this regime.”

Moreover, we slightly changed L13 P14, from:
“In general, we find that the ICNC in the mixed-phase regime is less sensitive to the ice nucleation scheme changes than the ICNC in the cirrus regime” to
“Thus, we can reiterate that the ICNC in the mixed-phase regime is less sensitive to the ice nucleation scheme changes than the ICNC in the cirrus regime.”

P14 L19-20: These mentioned ice crystals are simply too large compared to any kind of observations at such levels of the atmosphere.
Please, see our first reply. The ice crystal size goes beyond the scope of this manuscript and will be subject of future studies.

P16 L7-9: *I would either rephrase this or remove the reference to Lohmann et al. 2008 as the sentence gets very hard to understand, when explaining that Lohmann et al. 2008 did not include the competition effects.*

We removed the second citation: “The ice water path (IWP) decreases by almost 7% when BN09 is used in the cirrus regime, similarly to what has been found in Kuebbeder et al. (2014), who compared simulations assuming pure homogeneous nucleation against simulations including water vapour competition.”

P16 L10: *Also Gasparini et al., 2018 for a recent ECHAM-HAM paper showing IWP anomalies.*

We cited Gasparini et al. 2018.

P16 L11: *Add a reference for your liquid water path estimates.*

The IWP values are actually taken from Table 2, and the references are written in the caption of the Table.

We specified “..., between 23 and 87 g/m² (Li et al. 2012 and Han et al. 1994).”

P16 L13: *Duncan and Eriksson 2018 might be a fresh good reference for IWP variations between observation and reanalysis datasets.*

We modified the sentence at L9-10 P16: “Overall, the model underestimates the IWP, also found in other studies that applied ECHAM-HAM (...), however, there are still large discrepancies among observational datasets which make problematic the validation of the models (Duncan and Eriksson 2018).”

P16 L19-20: *SCRE becomes less strong. I would not call that an “increase”, despite its value becoming less negative. For me an increase in SCRE would imply a stronger reflection of clouds and consequently a more negative SCRE.*

It sounds actually better. We replaced “SCRE increases more than 5% with BN09 because of...” with “SCRE with BN09 becomes weaker (more than 5%) because of...”

P16 L21: *“NCRE diminishes”. Please rephrase also here to a more clear expression – maybe “NCRE becomes more negative”.*

We changed the sentence to: “As a result, NCRE becomes more negative, with statistically significance over...”

P17 L5-8: *If your scheme produces fewer and larger ice crystals that indeed might lead to increased precipitation. However, this will contribute to the large-scale precipitation budget, and not to the convective one. Your interpretation of the result is therefore not explaining the increase in convective precipitation.*

The Referee is right. Our results about precipitation shows that the changes are mostly caused by the convective precipitation changes, but the sentence at L5-7 P17 does not explain this. As written at L32-33 P12, there are some feedbacks in the convection activity due to the ice nucleation scheme used. Thus, we wrote: “When BN09 is used in the cirrus regime, $P_{tot}$ grows by 4% especially because of the increase of the convective precipitation contribution, due to some feedbacks on the convective activity generated by the different ice nucleation schemes used, as mentioned in Subsection 3.2.”
I would argue that the changes in LCRE and SCRE are quite considerable and not negligible (as you also mentioned earlier in the text).

Actually, we wrote the changes in percentages (5% and 15%) at L14-22 P16 and that “There are clear effects on SCRE and LCRE from changing the cirrus ice nucleation scheme” at L13-15 P17. In order to highlight this sentence, we changed it to: “Mostly, the experiments do not yield evident differences among each other at the global scale, as regional variations may cancel out, however, there are clear effects on SCRE and LCRE from changing the cirrus ice nucleation scheme.”

I would suggest to rather plot the radiative anomalies in absolute terms, using W/m$^2$ as a unit. Relative changes are tricky to interpret, in particular when looking at SCRE (and NCRE).

Done.

Table 2: Why do you compute also a spatial standard deviation when showing globally averaged results? Please use just global annual means, and get the (temporal) standard deviation from those 5 points (I agree 5 points are rather at the lower limit, but that is certainly more meaningful than looking at variability in both space and time).

We changed the standard deviations following the Referee’s suggestion.

Figure 1: New Figure for the supplement file. Annual zonal mean of (grid-averaged) ice crystal number concentration (ICNC, $[L^{-1}]$) for the default simulation KL+LD and the absolute changes of BN+LD, KL+BN, and BN+BN with respect to it as functions of latitude and temperature. (Last row) Absolute changes of annual zonal means averaged along the latitude 90S – 90N (left) and 25S – 75N (right): (BN+LD)-(DEF) in green, (KL+BN)-(DEF) in cyan, and (BN+BN)-(DEF) in red. Only the plot on the left has been added in the supplement.
Reply to the Editor’s comments

We really thank the Editor for his work and his helpful comments. Below we report our replies.

1. *I read multiple times the term cold/warm temperature which is a common mistake in cloud physics literature. Temperatures are high or low and tell whether an air parcel or some other material is warm or cold. Please change to low/high temperature.*
   
   Done.

2. *A bin model may explicitly compute the size distribution, but a two moment scheme certainly does not. Please reformulate p.5, l.25.*
   
   Thanks for pointing it out. We changed the sentence to:
   “The advantage of using a two-moment scheme is that it allows aerosol-cloud interactions improving calculations of cloud microphysical processes and radiative transfer.”

3. *p.8, l.20 “required to KEEP (?) s_max below s_hom.”*
   
   Done.

4. *p.10, l.19: I guess what you want to say is that “the standard deviations are constants depending only on the mode”. The word “differentiated” is misleading.*
   
   Yes. We changed to: “the standard deviations $\sigma_M$ are constant depending only on the mode ...”

5. *Sometimes you use the word “to comment” where I would favour the word “to remark” (e.g. p.11, l.25).*
   
   We used “remarked” at L25 P11 and L1 P13.

6. *p.12, l.5: as a function of LATITUDE AND altitude.*
   
   Done.

7. *replace big by large: p.14,l.33; p.15, l.24*
   
   Done.

8. *p.17, l.5: “(in total, 113 flights with about ...)”*
   
   Done.

   
   We wrote: “… in the cirrus regime, likely due to a faster sedimentation of larger ice crystals produced by BN09 in cirrus clouds at higher altitudes.”

10. *check “?” in Brinkop reference.*
   
   Thanks for noticing it.
Implementation of a comprehensive ice crystal formation parameterization for cirrus and mixed-phase clouds into the EMAC model (based on MESSy 2.53)

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**Abstract.** A comprehensive ice nucleation parameterization has been implemented in the global chemistry-climate model EMAC to improve the representation of ice crystal number concentrations (ICNCs). The parameterization of Barahona and Nenes (2009, hereafter BN09) allows the treatment of ice nucleation taking into account the competition for water vapour between homogeneous and heterogeneous nucleation in cirrus clouds. Furthermore, the influence of chemically-heterogeneous, polydisperse aerosols is considered by applying one of the multiple ice nucleating particle parameterizations which are included in BN09 to compute the heterogeneously formed ice crystals. BN09 has been modified in order to consider the pre-existing ice crystal effect and implemented to operate both in the cirrus and in the mixed-phase regimes. Compared to the standard EMAC parameterizations, BN09 produces fewer ice crystals in the upper troposphere but higher ICNCs in the middle troposphere, especially in the Northern Hemisphere where ice nucleating mineral dust particles are relatively abundant. Overall, ICNCs agree well with the observations, especially in cold cirrus clouds (at temperatures below 205 K), although they are underestimated between 200 K and 220 K. As BN09 takes into account processes which were previously neglected by the standard version of the model, it is recommended for future EMAC simulations.

1 **Introduction**

Clouds play an important role in the Earth System by affecting the global radiative energy budget, the hydrologic cycle, the scavenging of gaseous and particulate substances, and by providing a medium for aqueous-phase chemical reactions. Nevertheless, clouds remain one of the less understood components of the atmospheric system, and their representation in models
including processes like cloud droplet formation, ice nucleation, cloud phase transitions, secondary ice production, aerosol-cloud interactions) is one of the major challenges in climate studies (IPCC, 2013; Seinfeld et al., 2016). Compared to the liquid droplet activation process, the ice crystal formation (in mixed-phase and cirrus clouds) is affected by large uncertainties because of the poor understanding of the chemical and physical principles underlying ice nucleation and the complexity of ice nucleation mechanisms and aerosol-ice interactions (Cantrell and Heymsfield, 2005; Gultepe and Heymsfield, 2016; Heymsfield et al., 2017; Korolev et al., 2017).

Cirrus clouds form at high altitudes and very low temperatures (below 238 K) and consist purely of ice crystals. They strongly impact the transport of water vapour entering the stratosphere (Jensen et al., 2013) and play an important role as modulator of radiation fluxes in the global radiative budget: they scatter solar radiation back into the space (albedo effect) and absorb and re-emit longwave terrestrial radiation (greenhouse effect). Differently from other types of clouds, cirrus clouds produce a net warming at the top of the atmosphere (TOA) (e.g. Chen et al., 2000; Hong et al., 2016; Matus and L’Ecuyer, 2017). In addition, mixed-phase clouds consist of both supercooled liquid cloud droplets and ice crystals and appear at subfreezing temperatures above 238 K. Mixed-phase clouds generate a net cooling at TOA, although the estimates of their radiative effects are complicated by the coexistence of both ice and liquid cloud phases (Matus and L’Ecuyer, 2017). Due to the difference between vapour pressure over water and over ice, ice crystals grow at the expense of water droplets (Wegener-Bergeron-Findeisen process), thus, mixed-phase clouds are thermodynamically unstable and can convert into ice-only clouds (e.g. Korolev, 2007; Korolev et al., 2017). As ice crystals can grow quickly to precipitation-sized particles, precipitation is mainly formed in mixed-phase clouds, while precipitation from cirrus clouds does not usually reach the surface (Lohmann, 2017). The mixed phase is also important for cloud electrification and intracloud lightning, which occur through the in-cloud charge separation via a transition from supercooled raindrops to graupel over the mixed-phase temperature range (Korolev et al., 2017). The fraction of cloud ice has a profound impact on the cloud forcing in global climate models, one of the reasons why cloud radiative forcing is so diverse and uncertain (McCoy et al., 2016; Tan et al., 2016; Vergara-Temprado et al., 2018).

Ice crystal formation takes place via homogeneous and heterogeneous nucleation, depending on environmental conditions (e.g. temperature, supersaturation, vertical velocity) and aerosol populations (i.e. aerosol number concentrations and physical-chemical characteristics) (Pruppacher and Klett, 1997; Kanji et al., 2017; Heymsfield et al., 2017; Korolev et al., 2017). Homogeneous nucleation occurs through the freezing of supercooled liquid droplets at low temperatures ($T < 238$ K) and high supersaturation over ice ($140\% - 160\%$) (Koop et al., 2000). Heterogeneous nucleation refers to the formation of ice on an aerosol surface, which reduces the energy barrier for ice nucleation and lets ice crystals form at lower supersaturations and/or at warmer higher (subfreezing) temperatures than homogeneous nucleation. The aerosols that lead to the generation of ice crystals are called ice nucleating particles (INPs) and are mostly insoluble, like mineral dust, soot, organics, and biological particles (Pruppacher and Klett, 1997). Heterogeneous nucleation occurs via different mechanisms called “nucleation modes” (deposition, condensation, immersion, and contact nucleation). Based on In several modeling studies, homogeneous nucleation has been considered the dominant process for cirrus formation (e.g. Haag et al., 2003; Gettelman et al., 2012) but higher concentrations of liquid droplets is higher than that of INPs in the upper troposphere. However, some field measurements found a predominance of heterogeneous nucleation and lower ice crystal number concentrations (ICNCs) than produced by
homogeneous nucleation (e.g. Cziczo et al., 2013; Jensen et al., 2013). What process is dominant is still under debate, although recent studies suggested the overestimation of the vertical velocity as possible cause of the discrepancy between modeled results and observations (e.g. Barahona and Nenes, 2011; Zhou et al., 2016; Barahona et al., 2017).

Overall, two different regimes for ice crystal formation are distinguished. The *cirrus regime* at cold low temperatures ($T < 238$ K), where ice crystals originate via heterogeneous and homogeneous nucleation to form cirrus clouds. The *mixed-phase regime* at subfreezing temperatures between 238 K and 273 K, where ice crystals form exclusively via heterogeneous nucleation and alter the phase composition of the mixed-phase clouds. In the latter regime, besides primary nucleation, another mechanism which controls ICNCs is the secondary ice production, i.e. the production of new ice crystals via the multiplication of pre-existing ice particles without the action of INPs.

As heterogeneous nucleation takes place at lower supersaturation than homogeneous nucleation, the available water vapour and the degree of supersaturation decrease, reducing or inhibiting the formation of ice crystals from homogeneous nucleation. This competition between homogeneous and heterogeneous nucleation for water vapour drastically affects the ICNC in the cirrus regime, even at low INP concentrations (Kärcher and Lohmann, 2003; Spichtinger and Cziczo, 2010). On the other hand, both in the cirrus regime and in the mixed-phase regime, water vapour can also be reduced by depositional growth onto pre-existing ice crystals and ice crystals carried into the cloud via convective detrainment and advective transport, thus, inhibiting ice nucleation. The impact of pre-existing ice crystals (PREICE) can be especially important in cirrus clouds, when ice crystals are of small size and have low sedimentation rates at low temperatures (Barahona and Nenes, 2011), leading to optically thinner cirrus clouds characterized by fewer ice crystals with a diverse age distribution and high supersaturation levels, especially in the case of tropical upper troposphere/lowermost stratosphere (UTLS) cirrus clouds (Barahona and Nenes, 2011; Hendricks et al., 2011; Kuebbeler et al., 2014).

Cloud schemes in atmospheric and climate models have evolved from using only macrophysical properties like cloud cover to representing the microphysics explicitly, e.g. formation, evolution, and removal of cloud droplets and ice crystals (Kärcher et al., 2006; Lohmann et al., 2008; Gettelman et al., 2010; Barahona et al., 2014). Including sophisticated schemes in general circulation models (GCMs) allows for a more realistic description of the variability of cloud properties and cloud radiative effects, improving the model climate predictions (Lohmann and Feichter, 2005; Barahona et al., 2014). Recently, sophisticated parameterizations have been developed, taking into account the aerosol influence on ice formation and different modes of heterogeneous nucleation. Liu and Penner (2005) presented an ice nucleation scheme based on numerical parcel model simulations which considers the competition between homogeneous and heterogeneous nucleation following the classical nucleation theory (CNT). Kärcher et al. (2006) developed a physically based parameterization scheme of ice initiation and ice crystal initial growth in cirrus clouds, considering the PREICE effect and allowing for the competition between heterogeneous and homogeneous nucleation. Barahona and Nenes (2009) introduced an ice cloud formation parameterization, based on the analytical solution of the cloud parcel model equations, which calculates the competition for water vapour between homogeneous and heterogeneous nucleation and takes into account the variability (in size and chemical composition) of different aerosol species through a variety of INP parameterizations. Since then, these parameterizations have been included in GCMs in order to better predict cloud phase partitioning. Hendricks et al. (2011) and Kuebbeler et al. (2014) have implemented the parameterization
of Kärcher et al. (2006) into the ECHAM4 and ECHAM5-HAM models, respectively. Liu et al. (2007) and Liu et al. (2012) have implemented the parameterization of Liu and Penner (2005) into the CAM3 and CAM5 models, respectively. Also, Liu et al. (2012) and Barahona et al. (2014) have implemented the scheme of Barahona and Nenes (2009) in CAM5 and GEOS-5, respectively.

In this study the parameterization of Barahona and Nenes (2009, hereafter BN09) has been implemented into the ECHAM/MESy Atmospheric Chemistry (EMAC) global model to improve the representation of ice nucleation. The BN09 algorithm has been modified in order to include the PREICE effect and has been used to compute the new ice crystals formed both in the cirrus regime and/or in the mixed-phase regime. Its performance has been compared with the results generated via the standard model configuration, and the model evaluation has been carried out paying particular attention to the ice-related results. The paper is organised as follows: the description of the operational model and the BN09 scheme are in Section 2, as well as the information about the implementation work and the simulations run for this study, Section 3 describes the modeled ice-related products, Section 4 contains the evaluation of the model, and Section 5 presents our conclusions.

2 Model description and set-up of simulations

2.1 EMAC model

The EMAC model is a numerical chemistry-climate model (CCM) which describes tropospheric and middle-atmosphere processes and their interactions with ocean, land, and human influences. Such interactions are simulated via dedicated submodels in the MESy framework (Modular Earth Submodel System, Jöckel et al., 2010), while the 5th generation European Centre Hamburg GCM (ECHAM5, Roeckner et al., 2006) is used as core of the atmospheric dynamics. For the present study we have used ECHAM5 version 5.3.02 and MESSy version 2.53.

The EMAC model has been extensively described and evaluated against in-situ observations and satellite data, e.g. aerosol optical depth, acid deposition, meteorological parameters (e.g. Pozzer et al., 2012, 2015; Karydis et al., 2016; Tsimpidi et al., 2016; Klingmüller et al., 2017). It computes gas-phase species on-line through the MECCA (Module Efficiently Calculating the Chemistry of the Atmosphere) submodel (Sander et al., 2011) and provides a comprehensive treatment of chemical processes and dynamical feedbacks through radiation (Dietmüller et al., 2016). Aerosol microphysics and gas/aerosol partitioning are calculated by the GMXe (Global Modal-aerosol eXtension) submodel (Pringle et al., 2010), a two-moment aerosol module which predicts the number concentration and the mass mixing ratio of the aerosol modes, along with the mixing state. The aerosol size distribution is described by 7 lognormal modes (defined by total number concentration, number mean radius, and geometric standard deviation): 4 hydrophilic modes, which cover the aerosol size spectrum of nucleation, Aitken, accumulation, and coarse modes, and 3 hydrophobic modes, which have the same size range except for the nucleation mode which is not required. The aerosol composition within each mode is uniform in size (internally mixed) but it varies among modes (externally mixed). The aging of aerosols, through coagulation or condensation of water vapour and sulfuric acid, is described by GMXe by transferring aerosols from the externally mixed to the internally mixed modes. Convective and large-scale clouds are separately treated and individually calculated by the submodels CONVECT and CLOUD, respectively. The CONVECT
submodel contains multiple convection parameterizations (Tost et al., 2006a) (Tost et al., 2006b). In this work the scheme of Tiedtke (1989) with modifications by Nordeng (1994) has been used. Convective cloud microphysics is highly simplified and neither explicit aerosol activation into liquid droplets nor aerosol effects in the ice formation processes are taken into account, i.e., convective microphysics is solely based on temperature and updraft strength. Detrainment from convection is treated by taking updraft (and downdraft) concentrations of water vapour and cloud condensate and the corresponding mass flux detrainment rates into account. These are merged including turbulent detrainment (i.e., exchange of mass through the cloud edges) and organized detrainment (i.e., organized outflow at cloud top). The detrained water vapour is added to the large-scale water vapour field, while the detrained cloud condensate is directly used as a source term for cloud condensate by the large-scale cloud scheme (i.e., the CLOUD submodel), which considers the detrained condensate either liquid or ice depending on the temperature (if \( T < 238 \) K the phase is ice) and the updraft velocity. The size and numbers of the detrained condensate are not taken into account explicitly; number of detrained ice crystals is estimated from the ice condensate detrained from convection by assuming an only temperature dependent radius. The CLOUD submodel uses a double-moment stratiform cloud microphysics scheme for cloud droplets and ice crystals (Lohmann et al., 1999; Lohmann and Kärcher, 2002; Lohmann et al., 2007) which defines prognostic equations for specific humidity, liquid cloud mixing ratio, ice cloud mixing ratio, cloud droplet number concentration \((CDNC)\), and ICNC. The advantage of using a two-moment scheme is that it allows for the explicit computation of cloud particle size distribution, which interacts with radiation and influences the evolution of cloud properties. Aerosol-cloud interactions improving calculations of cloud microphysical processes and radiative transfer. In the CLOUD submodel, ice crystals form via homogeneous nucleation in the cirrus regime, via immersion and contact freezing in the mixed-phase regime (more details about ice nucleation are given in the next Subsection). Cloud droplet formation is parameterized by the “unified activation framework” (UAF) (Kumar et al., 2011; Karydis et al., 2011). It is an advanced physically based parameterization which merges two theories: \( \kappa \)-Köhler theory (KT) (Petters and Kreidenweis, 2007), which governs the activation of soluble aerosols, and Frenkel-Halsey-Hill adsorption activation theory (FHH-AT) (Kumar et al., 2009), which describes the droplet activation due to water adsorption onto insoluble aerosols (e.g., mineral dust). Aerosol modes that consist of only soluble material follow the KT, and the required effective hygroscopicity \((\kappa)\) is calculated based on the chemical composition of the mode as described by the ISORROPIA thermodynamic equilibrium model (Fountoukis and Nenes, 2007). Aerosol modes that consist of an insoluble core with soluble coating follow the UAF scheme, which takes into account the effects of adsorption and absorption on the cloud condensation nuclei (CCN) activity of the mixed aerosol. More details about the UAF scheme and its implementation in the EMAC model can be found in Karydis et al. (2017). The diagnostic cloud cover scheme of Sundqvist et al. (1989) based on the grid mean relative humidity is used; it assumes that a grid box is partly covered by clouds when the relative humidity exceeds a threshold and is totally covered when saturation is reached. Other microphysical processes, like phase transitions, autoconversion, aggregation, accretion, evaporation of rain, melting of snow, sedimentation of cloud ice, are also taken into account by the CLOUD submodel. An evaluation of the double-moment cloud microphysics scheme used by ECHAM5 was presented in Lohmann et al. (2007, 2008) and Lohmann and Hoose (2009), applying the two-moment aerosol microphysics scheme HAM (Stier et al., 2005). Lauer et al. (2007) and Righi et al. (2013, 2015, 2016) showed an evaluation of the CLOUD submodel in conjunction with the aerosol microphysics submodel MADE (Ackermann et al., 1998), while Tost
Figure 1. Scheme of the new ice crystal formation in the CLOUD submodel: different ice nucleation schemes can be used in the cirrus and in the mixed-phase regimes. nienc and limm_BN09 are variables defined in the namelist-file “cloud.nml”; red parts are new; three dots indicate other processes coded in the CLOUD submodel.

(2017) evaluated the CLOUD submodel in combination with the GMXe submodel. In Section 4 we will extend the comparison with various observations. Finally, physical loss processes, like dry deposition, wet deposition, and sedimentation of aerosol, are explicitly considered by the submodels DRYDEP, SEDI, and SCAV (Kerkweg et al., 2006; Tost et al., 2006a).

2.2 Default ice nucleation in EMAC

The CLOUD submodel describes the evolution of the prognostic variables which undergo all cloud microphysical processes (e.g. precipitation, deposition, evaporation/sublimation). As far as the formation of new ice crystals is concerned, they are computed via two independent parameterizations, as shown in black in Figure 1.

In the cirrus regime ($T \leq 238.15$ K) it is assumed that cirrus clouds form exclusively homogeneously using the parameterization of Kärcher and Lohmann (2002, hereafter referred to as KL02). Such parameterization computes the newly formed ice crystals via homogeneous nucleation ($N_{i, hom}^{NEW}$) of supercooled solution droplets and allows supersaturation with respect to ice.
Alternatively, it is possible to use the parameterization of Kärcher and Lohmann (2003) to simulate cirrus formation via pure heterogeneous freezing, however, by default the model operates with KL02, under the assumption that the dominant freezing mechanism for cirrus clouds is homogeneous nucleation.

In the mixed-phase regime (238.15 K < T ≤ 273.15 K) heterogeneous nucleation occurs via immersion ($N_{\text{NEW}}^{i,\text{imm}}$) and contact ($N_{\text{NEW}}^{i,\text{cnt}}$) freezing as described in Lohmann and Diehl (2006, hereafter referred to as LD06). Insoluble dust can initiate contact nucleation in the presence of supercooled water droplets following the parameterization of Levkov et al. (1992). Soluble dust and black carbon can act as immersion nuclei, according to the stochastic freezing hypothesis described in Diehl and Wurzler (2004). Possibly, contact freezing via thermophoresis can be included ($N_{\text{NEW}}^{i,\text{therm}}$), but it is usually not considered (i.e. $N_{\text{NEW}}^{i,\text{therm}} = 0$) since its contribution is negligible (Lohmann and Hoose, 2009). The Wegener-Bergeron-Findeisen (WBF) process at subfreezing temperatures is parameterized, so liquid water is forced to evaporate from cloud droplets and deposit onto existing ice crystals.

In the CLOUD submodel, a single updraft velocity ($w$) is used for the whole grid cell, although $w$ can vary strongly in reality within the cell horizontal dimension (e.g. Guo et al., 2008). This is a simplification which is commonly used by GCMs, nevertheless, important progress has been recently achieved on this front to describe the subgrid-scale variability of updraft velocity using high resolution simulations (Barahona et al., 2017). In EMAC, the subgrid-scale variability of vertical velocity is introduced by a turbulent component ($w_{\text{sub}}$) which depends on the subgrid-scale turbulent kinetic energy ($TKE$) described by Brinkop and Roeckner (1995), such that $w_{\text{sub}} = 0.7 \sqrt{TKE}$. The vertical velocity is given by the sum of the grid mean vertical velocity ($\overline{w}$) and the turbulent contribution: $w = \overline{w} + 0.7 \sqrt{TKE}$ (Kärcher and Lohmann, 2002). Zhou et al. (2016) analysed the effect of different updraft velocity representations on ice number concentrations and showed that using $w_{\text{sub}}$ overestimates the ICNCs at temperatures below 205 K, but agrees better with the observations at higher temperatures. Other studies, e.g. Kärcher and Ström (2003) and Joos et al. (2008), showed that $w$ is in good agreement with vertical velocity observations. Given the importance of updraft velocities for ice formation (Donner et al., 2016; Sullivan et al., 2016), future studies could implement a complete probability distribution of updrafts. Finally, the influence of the pre-existing ice particles is not taken into account.

The only expedient adopted by the CLOUD submodel is to reduce the number of aerosol particles available for ice nucleation by the existing ice particle number in the cirrus regime.

2.3 Ice nucleation parameterization BN09

2.3.1 Scheme characteristics

The BN09 parameterization is computationally efficient and suitable for large-scale atmospheric models. It explicitly considers the competition for water vapour between homogeneous and heterogeneous nucleation in the cirrus regime, the influence of chemically-heterogeneous, polydisperse aerosols acting as INPs, and allows to use different heterogeneous nucleation parameterizations.

The BN09 algorithm can be divided in three subsequent parts. First, the limiting number of INPs ($N_{\text{lim}}$) needed to inhibit homogeneous nucleation is computed if temperatures are below 238 K. Indeed, at such cold temperatures homogeneous
and heterogeneous nucleation compete for water vapour decreasing ice supersaturation. When INPs exceed $N_{\text{lim}}$ and the maximum supersaturation ($s_{\text{max}}$) is less than the threshold for homogeneous nucleation ($s_{\text{hom}}$), homogeneous nucleation is suppressed and ice crystals are formed only heterogeneously. $N_{\text{lim}}$ is determined by computing the number of INPs required to keep $s_{\text{max}}$ below $s_{\text{hom}}$.

In the second step, ice crystals nucleated heterogeneously ($N_{i,\text{het}}$) are computed via the selected INP parameterization at $s_{\text{hom}}$, then two cases can follow. If the condition $N_{i,\text{het}}(s_{\text{hom}}) \geq N_{\text{lim}}$ is satisfied, ice crystals are formed only heterogeneously at $s_{\text{max}}$ (i.e. $N_{i,\text{het}}(s_{\text{max}})$), as homogeneous nucleation is suppressed. Here, the $s_{\text{max}}$ is determined using a bisection method to balance the supersaturation within the air parcel. If $N_{i,\text{het}}(s_{\text{hom}}) < N_{\text{lim}}$, the competition between homogeneous and heterogeneous nucleation is simulated. The ice crystals nucleated homogeneously ($N_{i,\text{hom}}$) are determined via the homogeneous nucleation parameterization of Barahona and Nenes (2008, 2009) (hereafter BNhom):

$$f_c = f_{c,\text{hom}} \left[ 1 - \left( \frac{N_{i,\text{het}}(s_{\text{hom}})}{N_{\text{lim}}} \right)^{3/2} \right]^{3/2}$$

$$N_{i,\text{hom}} = N_{c} e^{-f_c} (1 - e^{-f_c})$$

where $N_{c}$ is the number concentration of supercooled liquid cloud droplets and $f_c$ is the fraction of freezing soluble aerosol. The first factor of $f_c$ (i.e. $f_{c,\text{hom}}$) is defined by Barahona and Nenes (2008), while the second factor is the correction introduced by Barahona and Nenes (2009) to take into account the reduction of the probability of homogeneous nucleation due to the change in the droplet size distribution during crystal formation.

Third, the total concentration of new ice crystals formed in the cirrus regime ($N_{i,cirrus}^{\text{NEW}}$) is determined by the contribution of both heterogeneous and homogeneous nucleation. i.e. $N_{i,cirrus}^{\text{NEW}} = N_{i,\text{het}} + N_{i,\text{hom}}$ (see Figure 1). On the other hand, if the temperature is higher than 238 K, the algorithm uses the INP parameterization to compute $N_{i,\text{het}}(s_{\text{max}})$.

It is important to stress that the BN09 code actually includes five INP parameterizations to deal with heterogeneous nucleation (as mentioned before) and these are described by (i) Meyers et al. (1992), (ii) Phillips et al. (2007), (iii) Phillips et al. (2008), (iv) Phillips et al. (2013), and (v) Barahona and Nenes (2009). They are all empirically based except the latter, which is derived from the CNT. Sensitivity studies have shown that global means of ICNC vary up to a factor twenty according to the INP parameterization used (when the competition between homogeneous and heterogeneous nucleation is taken into account) and empirical based parameterizations better agree with observations, while CNT overestimates the number of ice crystals (Barahona et al., 2010; Sullivan et al., 2016). Therefore, the simulations described in Subsection 2.4 use the parameterization of Phillips et al. (2013, hereafter referred to as P13) to simulate heterogeneous nucleation, since it better agrees with observations (Sullivan et al., 2016). P13 is the improved version of Phillips et al. (2008), a comprehensive empirical formulation which takes into account the surface area contribution of different insoluble aerosols (with diameters larger than 0.1 $\mu$m) to deposition and immersion/condensation nucleation modes, besides the temperature and the supersaturation with respect to ice. The aerosol particles responsible for ice nucleation are divided in four groups: mineral dust (DU), inorganic black carbon (BC), biological aerosols (BIO), and soluble organics (OCsol). Dust and soot, the aerosol species considered in this work for
the reasons explained in Subsection 2.4, contribute to determine \( N_{i,\text{het}} \) in the following way:

\[
n_{\text{INP},X} = \int_{\log(0.1\,\mu m)}^{\infty} \left[ 1 - e^{-\mu_X(D_X,S_i,T)} \right] \frac{dN_X}{d\log D_X} d\log D_X \quad X = DU, \, BC; \quad T < 273.15 \, K
\]

(3)

\[
N_{i,\text{het}}(s_{\text{max}}) = \sum_{X=1}^{N_X} n_{\text{INP},X}
\]

(4)

where \( n_{\text{INP},X} \) is the number concentration of INPs activated at a saturation ratio with respect to ice \( S_i \) and temperature \( T \) for the aerosol species \( X \), \( \mu_X \) represents the mean number of activated ice embryos per insoluble aerosol particle of species \( X \) with diameter \( D_X > 0.1 \, \mu m \), \( n_X \) is the number concentration of aerosol particles (interstitial and INP immersed in cloud droplets) of species \( X \), and \( N_X \) is the number of different aerosol species. Equation (3) can be further extended for biological aerosols and soluble organics, as shown in Phillips et al. (2013), and \( N_{i,\text{het}} \) denotes the new ice crystals formed via deposition and immersion/condensation nucleation modes.

Summarizing (see Figure 1), according to BN09 the new ice crystals formed in the cirrus regime are:

\[
N_{i,\text{cirrus}}^{\text{NEW}} = \begin{cases} 
N_{i,\text{hom}} + N_{i,\text{het}}(s_{\text{hom}}) & N_{i,\text{het}}(s_{\text{hom}}) < N_{\text{lim}}, \ s_{\text{max}} = s_{\text{hom}} \\
N_{i,\text{het}}(s_{\text{max}}) & N_{i,\text{het}}(s_{\text{hom}}) \geq N_{\text{lim}}, \ s_{\text{max}} < s_{\text{hom}} 
\end{cases}
\]

(5)

while in the mixed-phase regime they are computed as:

\[
N_{i,\text{imm}}^{\text{NEW}} = N_{i,\text{het}}(s_{\text{max}})
\]

(6)

In order to account for sub-grid variabilities, the output variables of BN09 which depend on the vertical velocity \( f(w) \) are weighted over a Gaussian updraft velocity distribution by numerically calculating the integral (Morales and Nenes, 2010; Sullivan et al., 2016):

\[
f(w) = \frac{\int_0^\infty f(w')P(w')dw'}{\int_0^\infty P(w')dw'}
\]

(7)

where \( P(w') \) is the Gaussian probability density function of sub-grid vertical velocities \( w' \) with mean 0.1 cm s\(^{-1}\) and standard deviation equal to \( w_{\text{sub}} \).

### 2.3.2 Implementation

The BN09 parameterization has been added in the MESSy framework in order to compute the newly formed ice crystals in the cirrus regime and/or in the mixed-phase regime. The input variables of BN09 are: temperature \( T, \, [K] \); pressure \( P, \, [Pa] \); width of the vertical velocity distribution \( w_{\text{sub}} , \, [m \, s^{-1}] \) with upper limit 3 m s\(^{-1}\) and lower limit 0.01 m s\(^{-1}\); number concentration of activated cloud droplets \( N_c, \, [m^{-3}] \), dry diameter of Aitken soluble mode \( D_c, \, [m] \), see Appendix A) and standard deviation of Aitken soluble mode \( \sigma_c \); number concentrations \( N_X, \, [m^{-3}] \), geometric mean dry diameters \( (D_M, \, [m]) \), and lognormal standard deviations \( \sigma_M \) of interstitial aerosol of species \( X \) (which can be DU, BC, OCsol, BIO,

...
depending on the choice of the INP parameterization). Given the internally mixed representation of aerosols in EMAC, the diameters \( D_M \) are not distinguished among aerosol species but only among the modes (Aitken \((K)\), accumulation \((A)\), coarse \((C)\), i.e. \( M = K, A, C \)) which the species belong to. Similarly, the standard deviations \( \sigma_M \) are differentiated only by constant depending only on the mode (in EMAC \( \sigma_K = \sigma_A = 1.59 \) and \( \sigma_C = 2.0 \)).

A schematic overview of how BN09 has been implemented in EMAC through the CLOUD submodel is shown in Figure 1. Moreover, the PREICE effect has been included in the BN09 code. This effect is parameterized by reducing the vertical velocity for ice nucleation \( (w_{sub}) \) by a factor depending on the pre-existing ice crystal number concentration and size, limiting the expansion cooling. Such “corrected” vertical velocity \( (w_{sub, pre}) \) has been computed as defined in equation (24) by Barahona et al. (2014). Further information about the implementation is given in Appendix A.

2.4 Setup of simulations

In this study EMAC simulations have been carried out with T42L31ECMWF resolution, which corresponds to a spherical truncation of T42 (i.e. quadratic Gaussian grid of approx. \( 2.8^\circ \times 2.8^\circ \) in latitude and longitude) and 31 vertical hybrid pressure levels up to 10 hPa (approx. 25 km) at the lower stratosphere. All simulations have been run for 6 years (1 year as spin-up time plus 5 years for the analysis) using emissions starting from the year 2000 (GFEDv3.1 from van der Werf et al. 2010 for biomass burning and CMIP5-RCP4.5 from Clarke et al. 2007 for anthropogenic emissions). As in Pozzer et al. (2012), dust is offline prescribed using monthly emission files based on the AEROCOM data set (Dentener et al., 2006). Also volcanic and secondary organic aerosol emissions are based on AEROCOM, while GFEDv3.1 and CMIP5-RCP4.5 have been used to simulate emissions of black carbon and organic aerosols, respectively. Finally, aerosol climatologies have been used for the interactions with radiation (Tanre et al., 1984) and heterogeneous chemistry (Aquila et al., 2011). Prescribed climatologies of sea surface temperatures (SST) and sea-ice concentrations (SIC) from AMIP (30 years: 1980-2009) have been used as boundary conditions. Daily means have been saved as output, and monthly means have been used for the analysis in Sections 3 and 4.1.

Table 1 lists all simulations of this study and summarises their main characteristics. The default experiment (DEF or KL+LD) is performed with the standard configuration of the EMAC model, i.e. using the parameterization of Kärcher and Lohmann (2002) for cirrus clouds and the parameterization of Lohmann and Diehl (2006) for immersion nucleation in the mixed-phase regime. The UAF scheme is used as cloud droplet formation parameterization, like in Karydis et al. (2017). In order to investigate the model performance using the BN09 scheme, we carried out three other experiments where BN09 operates in the two cloud regimes in different combinations: BN09 computing the new ice crystals in the cirrus regime (BN+LD), in the mixed-phase regime (KL+BN), and in both regimes (BN+BN).

In all experiments, contact nucleation is computed according to LD06, while thermophoresis contact nucleation is not considered since its contribution is negligible (as commented remarked in Subsection 2.2). The P13 parameterization is used to simulate deposition and immersion/condensation nucleation whenever BN09 is called (for the reasons explained in Subsection 2.3). Since LD06 takes into account only dust and soot for immersion nucleation, we set the same aerosol species as contributions for P13 and turned off the biological and organic contributions.
<table>
<thead>
<tr>
<th>Experiment name</th>
<th>Ice nucleation scheme</th>
<th>Cirrus regime</th>
<th>Mixed-phase regime</th>
</tr>
</thead>
<tbody>
<tr>
<td>KL+LD or DEF</td>
<td>KL02, pure homogeneous nucleation</td>
<td></td>
<td>LD06, immersion nucleation</td>
</tr>
<tr>
<td>BN+LD</td>
<td>BN09, competition and PREICE</td>
<td></td>
<td></td>
</tr>
<tr>
<td>KL+BN</td>
<td>KL02, pure homogeneous nucleation</td>
<td></td>
<td>BN09, immersion/condensation and deposition nucleation via P13</td>
</tr>
<tr>
<td>BN+BN</td>
<td>BN09, competition and PREICE</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 1. All experiments carried out in this study.

3 Model results

BN09 improves the ice nucleation representation in EMAC by taking into account processes (e.g. water vapour competition, influence of polydisperse aerosols, PREICE effect) which were previously neglected by KL02 and LD06. In this Section we investigate the changes and the effects obtained by using BN09 in the different regimes.

5 3.1 Annual zonal means

The annual zonal means of ICNC and ice water content (IWC) are shown as a function of latitude and altitude in Figure 2, where the isolines at 273 K and 238 K indicate the approximate bounds of cirrus and mixed-phase regimes. Despite the different ice nucleation parameterizations, ICNCs show similar qualitative patterns in all simulations, indicating the important role of atmospheric dynamics. Their numbers decrease towards lower altitudes (Figure 2a) because the ice nucleation rate reduces with increasing temperature, while they are much higher over the mid-latitudes in the Northern Hemisphere (NH) because of larger INP concentrations and the influence of big mountain chains, e.g. Rocky Mountains and the Himalayas. Looking at the relative changes, we note that ICNCs computed with BN09 in the cirrus regime are much lower than the default ICNCs in the upper troposphere and at high latitudes in the Southern Hemisphere (SH), where they are lower by up to 80% (Figure 2b). The absolute changes of ICNC annual zonal means computed as a function of latitude and temperature (Figure S1 in the supplement file) show that ICNCs in BN+KL are lower than the default case by 300 L⁻¹ at temperatures below 220 K. As ice crystals are formed almost exclusively via homogeneous nucleation here (not shown) and BNhom and KL02 produce the same order of magnitude of ICNCs (Barahona and Nenes, 2008), the negative bias is likely due to the PREICE effect predicted by BN09. Indeed, it has been demonstrated that homogeneous nucleation dominates in the upper troposphere in the tropics and in the SH (Haag et al., 2003; Liu et al., 2012; Barahona et al., 2017), while heterogeneous nucleation is important in the NH (Cziez et al., 2009; Li et al., 2012; Kuebeler et al., 2014; Storelmo and Herger, 2014; Shi et al., 2015; Gasparini and Lohmann, 2016; Barahona et al., 2017). Cirrus clouds are formed from a combination of homogeneous and heterogeneous processes. Interestingly, ICNCs at lower altitudes are also influenced by the ice nucleation parameterization used in the cirrus regime. In fact, there is an increase of ICNCs in the mixed-phase regime probably due to a faster sedimentation of the larger ice crystal crystals produced by BN09 in cirrus clouds, especially in the NH where there are larger sources of efficient ice-nucleating mineral dust. Overall, as remarked later in Subsection 4.1, the total ICNC in BN+LD globally decreases. The changes produced by applying BN09
in the mixed-phase regime (Figure 2c) result from the different heterogeneous ice nucleation parameterizations used to simulate immersion nucleation, P13 vs. LD06. The changes are especially evident in the NH (more than 40%), where mineral dust is more abundant than in the SH. As P13 produces fewer new ice crystals than LD06 (not shown), the positive biases in the mixed-phase regime are possibly due to influences from the cirrus regime (e.g. ice crystal sedimentation) and convective detrainment. Overall, the ICNC deviations in the mixed-phase regime obtained using the two different parameterizations are smaller (mostly within ±20%) than in the cirrus regime. This is also evident from Figure S1 in the supplement file (last row), where the absolute changes are, in average, between 200 and −200 L\(^{-1}\) when BN09 is used in the cirrus regime and between 50 and −50 L\(^{-1}\) when comparing KL+BN with KL+LD. Possibly, the rate associated to heterogeneous nucleation in the mixed-phase regime is masked by other processes, like sedimentation and aggregation, which also contribute to ICNC in this regime. Finally, the simulation using BN09 in both regimes combines the effects described so far (Figure 2d). Since cirrus clouds do not occur throughout the whole year, we present in the supplement file (Figure S1-S2) the ICNC seasonal means for summer (June-July-August, JJA) and winter (December-January-February, DJF). The seasonal analysis helps to understand why there is cirrus occurrence at temperatures warmer than 238 K, showing that the ICNC growth in the mixed-phase region predicted by BN+LD is actually very small, as expected given that the ice scheme used in the mixed-phase regime is the same as the default simulation.

The IWC pattern (Figure 2e) qualitatively follows the ICNC distribution. It is quite symmetrical between the two hemispheres except at high latitudes in the NH, where IWC is slightly higher because of the higher values of ICNC. Particularly, IWC exhibits three local maxima: two over the mid-latitudes in both hemispheres and one in the tropics, associated to storm tracks and deep convections, respectively (Li et al., 2012), in agreement with satellite observations, e.g. Waliser et al. (2009), Li et al. (2012). The relative changes in Figure 2f show a pattern very similar to Figure 2b, therefore, IWC decreases where ICNC reduces (and vice versa) when BN09 is used in the cirrus regime. On the other hand, IWC in KL+BN slightly reduces (up to 20%) in the mixed-phase regime in areas where ICNC increases, especially in the NH at high latitudes (Figure 2g). This could be due to the different sizes of ice crystals, however, the areas with significance are rather small. Finally, BN+BN in Figure 2h simulates an overall reduction of IWC except in the three areas with higher values of IWC described in Figure 2e.

### 3.2 Global distributions

Figure 3 shows the global distributions of ICNC annual means at two different altitudes: 200 hPa (where temperatures vary between 200 K and 220 K) to represent the cirrus regime and 600 hPa (where temperatures are approximately between 240 K and 260 K) to represent the mixed-phase regime. ICNCs in the cirrus regime (Figure 3a) show areas with high values over land and in correspondence with mountainous regions, e.g. the Rocky Mountains, Andes, and Tibetan Plateau with ICNCs > 500 L\(^{-1}\). Such pattern is strongly related to the turbulent contribution of the vertical velocity \(w_{sub}\) and in agreement with Gryspeerdt et al. (2017), who detected in these areas mostly orographic cirrus clouds. Figure 3a also shows higher ICNCs around the edge of the Antarctic ice sheet and over those regions which experience a strong convective activity, i.e. the Inter Tropical Convergence Zone (ITCZ) and the Tropical Warm Pool (TWP), as observed in Sourdeval et al. (2018). The annual global mean of ICNC at 200 hPa is about 200 L\(^{-1}\) (∼390 L\(^{-1}\) over land and ∼124 L\(^{-1}\) over ocean). The relative changes
Figure 2. Annual zonal means of (grid-averaged) ice crystal number concentration \( (ICNC, [L^{-1}]) \) and non-precipitable ice water content \( (IWC, [mg \text{ kg}^{-1}]) \) for the default simulation KL+LD and the relative percentage changes of BN+LD, KL+BN, and BN+BN with respect to it (i.e. \( \frac{(experiment - DEF)}{|DEF|} \cdot 100 \)), computed where \( ICNC_{DEF} \geq 1 \text{ L}^{-1} \) and \( IWC_{DEF} \geq 0.1 \text{ mg kg}^{-1} \). The isotherms at 273 K and 238 K are annual means, the crossed pattern indicates areas with a significance level of 95%.
clearly show that BN09 used in the cirrus regime (Figure 3b, d) reduces ICNC (up to 60%) worldwide with respect to the default experiment, and the ICNC annual global mean drops to 137 L\(^{-1}\) (i.e. more than 30%). Such a reduction occurs mostly because of the PREICE effect, being As the ice crystals are mainly of homogeneous origin at this altitude, such a reduction is probably due to the PREICE effect. However, there are positive biases along the ITCZ and over the TWP area. As the concentrations of new ice crystals produced by BN09 are not particularly remarkable in these regions (not shown), convective detrainment is likely to play a role. Indeed, there is a certain response of the convective activity to the choice of the ice nucleation scheme used in the cirrus regime. On the contrary, KL+BN is characterised by a general increase of ICNC (Figure 3c). However, most of the areas with strong positive changes (larger than 60%) correspond to regions characterized by low ICNC (< 30 L\(^{-1}\)), thus, the global annual mean increases just up to 218 L\(^{-1}\) (i.e. +9%). At 600 hPa, ICNCs increase towards high latitudes, in particular over Greenland (up to 2000 L\(^{-1}\)) and Antarctica (mostly > 2000 L\(^{-1}\)) (Figure 3e). It must be said that, due to the very low temperatures in the latter region, even at 600 hPa the conditions are typical of the cirrus regime, and the high ICNCs can be related to the high values of both \(w_{\text{sub}}\) and ice supersaturation. Gryspeerdt et al. (2017) found that cirrus clouds over Antarctica have primarily synoptic origin. However, differently from Figure 3e, observations do not present such a high peak of ICNC over Antarctica (Gryspeerdt et al., 2018; Sourdeval et al., 2018). The annual global mean is about 53 L\(^{-1}\), which means about one quarter with respect to the ICNC global mean at 200 hPa. Figure 3f confirms what already noticed in Figure 2b, that is the ice nucleation scheme used in the cirrus regime affects the ICNC at the mixed-phase regime altitudes predicting higher ICNCs especially in the NH. However, the largest differences occur in areas where ICNCs are very low and slightly affect the absolute ICNC values. As a result, the annual global mean actually decreases to 47 L\(^{-1}\) because of the negative contribution in the SH. Figure 3g also shows strong positive biases, but ICNCs do not change globally (52 L\(^{-1}\)). In general, we find Thus, we can reiterate that the ICNC in the mixed-phase regime is less sensitive to the ice nucleation scheme changes than the ICNC in the cirrus regime. Vertically integrated ice crystal number concentrations (\(\text{ICNC}_{\text{burden}}\), Figure S2–S3 in the supplement file) clearly show that concentrations are higher over continents (\(\sim 48 \cdot 10^8 \text{ m}^{-2}\)), where vertical updrafts are stronger and aerosol concentrations more abundant, than over oceans (\(\sim 11 \cdot 10^8 \text{ m}^{-2}\)).

IWC at 200 hPa and 600 hPa (Figure 4) presents a pattern qualitatively similar to the ICNCs at the corresponding heights. Nevertheless, two interesting features appear. First, the high IWC values (> 10 mg kg\(^{-1}\)) over the TWP at 200 hPa, where ICNCs are not particularly high. This is probably caused by the bigger radii of the newly formed larger radius of ice crystals simulated in this area, both by KL02 and BN09. Second, IWC at 600 hPa is rather low over Antarctica (likely because of the low water vapour concentration), which is instead one of the regions with the highest ICNC. The relative changes of IWC with respect to the default simulation (Figure S3–S4 in the supplement file) approximately follow the changes obtained for ICNC, i.e. IWC reduces where ICNC decreases and vice versa.
Figure 3. Annual means of (grid-averaged) ice crystal number concentration ($ICNC$, $[L^{-1}]$) at 200 hPa (cirrus regime) and 600 hPa (mixed-phase regime) for the default simulation KL+LD and the relative percentage changes of BN+LD, KL+BN, and BN+BN with respect to it (i.e. $(\text{experiment} - \text{DEF})/|\text{DEF}| \cdot 100$). The crossed pattern indicates areas with a significance level of 95%.

4 Model comparisons and observations

4.1 Annual global means

Table 2 shows an overview of the global annual means of cloud microphysical variables and radiative fluxes computed for different observations and for all experiments, and the percentage changes with respect to the default simulation. The global
vertically integrated ice crystal number concentration changes considerably depending on the ice scheme used in the cirrus regime and in mixed-phase regime. When BN09 operates in the cirrus regime, ICNC_{burden} decreases by 10% due to the competition between homogeneous and heterogeneous nucleation and the PREICE effect (a similar result has been found also by Liu et al. 2012, Kuebbeler et al. 2014, and Shi et al. 2015). On the other hand, ICNC_{burden} increases by almost 7% when BN09 is used in the mixed-phase regime, i.e. when P13 simulates heterogeneous nucleation. On a large scale, these effects offset each other in BN+BN, where the global annual mean is basically unchanged with respect to the default simulation. Overall, the ICNC_{burden} values are very close to the global annual means found by Lohmann et al. (2008) and Kuebbeler et al. (2014), while they are an order of magnitude higher compared to the results of Wang and Penner (2010) and Shi et al. (2015). ICNC_{burden,cirri} and ICNC_{burden,mixed} are vertically integrated ICNCs in the cirrus regime and in the mixed-phase regime, respectively. It is interesting to see quantitatively the different contributions to the total ICNC_{burden}: ICNCs in the cirrus regime are about 6 times bigger/larger than the ICNCs in the mixed-phase regime when KL02 is used and about 5 times when BN09 is applied in the cirrus regime. In general, we observe that the variability of ICNC increases when BN09 is used. Vertically integrated cloud droplet number concentration (CDNC_{burden}) is basically not influenced by the choice of the ice nucleation scheme. Its values are comparable with previous modeling studies (e.g. Lohmann et al., 2007; Hoose et al., 2008; Salzmann et al., 2010; Wang and Penner, 2010; Kuebbeler et al., 2014; Shi et al., 2015) and observations, although satellite observations are still affected by strong uncertainties (Bennartz and Rausch, 2017).

The ice water path (IWP) decreases by almost 7% when BN09 is used in the cirrus regime, similarly to what has been found in Kuebbeler et al. (2014) and Lohmann et al. (2008), who compared, respectively, simulations assuming pure homogeneous nucleation against simulations including water vapour competition and against simulations considering homogeneous and heterogeneous nucleation (in different grid boxes). Overall, the model underestimates the IWP, also found in other studies that applied ECHAM-HAM (e.g. Lohmann et al., 2008; Lohmann and Hoose, 2009; Kuebbeler et al., 2014) (e.g. Lohmann et al., 2008; Lohmann and Hoose, 2009) (Lohmann et al., 2008). However, there are still large discrepancies among observational datasets which make problematic the validation of the models (Duncan and Eriksson, 2018). The liquid water path (LWP) estimates derived from satellite observations vary substantially, between 23 and 87 g/m² (Li et al., 2012; Han et al., 1994). The modeled results fall within this range and the one indicated as
acceptable by Mauritsen et al. (2012), which is 50 – 80 g/m². The LWP variations among the experiments are much smaller than the IWP variations.

The absolute values of the shortwave cloud radiative effect (SCRE) and longwave cloud radiative effect (LCRE) are higher than those derived from satellite data, especially when KL02 is employed in the cirrus regime. However, when the net cloud radiative effect (NCRE) is computed, the same simulations with KL02 in the cirrus regime are closer to the observations. Looking at the percentage absolute changes and the global distributions in the supplement file (Figure S4-S5) it is evident that the cloud radiative effects are sensitive to the ice nucleation scheme used for cirrus clouds. Indeed, SCRE increases with BN09 becomes weaker (more than 5% with BN09) because of the less efficient scattering of shortwave radiation by fewer and larger crystals. More importantly, LCRE decreases up to 15% in BN+LD because cirrus clouds, at the same, can trap less longwave radiation in the Earth-atmosphere system. As a result, NCRE diminishes becomes more negative, with statistically significance over some areas in the tropics and high latitudes, and the cooling effect is enhanced. The total cloud cover (TCC) is slightly overestimated by the model (likely explaining why the cloud radiative forcing is high despite IWP being half of the observed values). However, Mauritsen et al. (2012) assert that a global model is acceptable if TCC is higher than 60%. The changes with respect to the default simulation are very low (below 2%), and the biggest change is in BN+LD where TCC reduces by 1.39%, since lower ICNCs leads to higher sedimentation rates. Finally, the model tends to overestimate the total precipitation (P_{tot}), i.e. the sum of large scale and convective precipitations, but this has also been found with other global models (e.g. Barahona et al. 2014 with GEOS-5, Shi et al. 2015 with CAM5, and Lohmann et al. 2008 and Kuebbeler et al. 2014 with ECHAM-HAM as well). When BN09 is used in the cirrus regime, P_{tot} grows by 4% especially because of the increase of the convective precipitation contribution due to some feedbacks on the convective activity generated by the different ice nucleation schemes used, as mentioned in Subsection 3.2. BN09 predicts fewer and larger crystals over tropical, continental regions where previous studies show that the majority of precipitation initiates in the ice-phase (e.g. Mülmenstädt et al., 2015).

The annual zonal means of vertically integrated number concentration of ice crystals and cloud droplets, ice water path, liquid water path, shortwave and longwave cloud radiative effects, and total cloud cover are shown in Figure S5-S6 (in the supplement file) and are comparable with the literature cited before. The annual zonal mean profiles show clearly that the simulations using the same ice nucleation scheme in the cirrus regime are very close to each other, i.e. KL+LD and KL+BN, and BN+LD and BN+BN (as already visible in Table 2).

Overall, the model performs well with respect to observations and the literature. Mostly, the experiments do not yield evident differences among each other at the global scale, as regional variations may cancel out. There, however, there are clear effects on SCRE and LCRE from changing the cirrus ice nucleation scheme. As there is not a clear indication which simulation performs better, in the next Subsection we extend our analysis including a statistical comparison with aircraft measurements.

### 4.2 Comparison with aircraft measurements

The validation of climate models with measurements from field experiments or aircraft campaigns is always limited by the fact that the models have difficulties to capture individual meteorological events. Nevertheless, here we consider a big collection...
Table 2. Global annual means for simulations and observations. Shown are grid-averaged vertically integrated cloud droplet number concentration (CDNC burden, \(10^{10} \text{m}^{-2}\)), vertically integrated ice crystal number concentration in the cirrus regime (ICNC burden, cirri, \(10^{8} \text{m}^{-2}\)), vertically integrated ice crystal number concentration in the mixed-phase regime (ICNC burden,mixed, \(10^{8} \text{m}^{-2}\)), grid-averaged liquid water path (LWP, \(\text{g m}^{-2}\)) and ice water path (IWP, \(\text{g m}^{-2}\)), net shortwave radiative flux (SW\textsubscript{NET,TOA}, [W m\(^{-2}\)]), longwave radiative flux (LW\textsubscript{TOA}, [W m\(^{-2}\)]), and radiative imbalance (Imbalance\textsubscript{TOA}, [W m\(^{-2}\)]) at TOA, shortwave cloud radiative effect (SCRE, [W m\(^{-2}\)]), longwave cloud radiative effect (LCRE, [W m\(^{-2}\)]), net cloud radiative effect (NCRE, [W m\(^{-2}\)]), total cloud cover (TCC, [%]), total precipitation (P\textsubscript{tot}, [mm day\(^{-1}\)]). The values in brackets are (temporal and spatial) standard deviations. The sixth column contains the annual global means computed using the satellite data from ERBE 1985-1990 (1), 2000-2006 (4), CERES-SYN1deg 2004-2010 (2), CERES-EBAF 2000-2016 (3), MODIS-TERRA 2004-2008 (5), CMAP 1970-2016 (6), GPCP 1979-2009 (7), and global means taken from the literature: (A) is derived from AVHRR data (Gettelman et al., 2010), (B) from NOAA-9 and NOAA-10 data (Han et al., 1994), (C) from CloudSat data (Li et al., 2012), and (D) from ISCCP data (Storelvmo et al., 2008). Last three columns show the percentage changes [%] of the experiments 2, 3, 4 with respect to the default simulation, i.e. \((\text{experiment} - \text{DEF})/|\text{DEF}| \cdot 100\)

<table>
<thead>
<tr>
<th>CDNC\textsubscript{burden}</th>
<th>BN+LD (2)</th>
<th>KL+BN (3)</th>
<th>BN+BN (4)</th>
<th>OBSERVATIONS</th>
<th>2 vs DEF</th>
<th>3 vs DEF</th>
<th>4 vs DEF</th>
</tr>
</thead>
<tbody>
<tr>
<td>4.15 (0.04)</td>
<td>4.21 (0.05)</td>
<td>4.12 (0.03)</td>
<td>4.18 (0.06)</td>
<td>4.01(^{(A)})</td>
<td>1.32</td>
<td>-0.72</td>
<td>0.72</td>
</tr>
<tr>
<td>21.86 (0.27)</td>
<td>19.61 (0.32)</td>
<td>23.33 (0.24)</td>
<td>21.75 (0.50)</td>
<td></td>
<td>-10.29</td>
<td>6.72</td>
<td>-0.50</td>
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<tr>
<td>18.95 (0.24)</td>
<td>16.47 (0.31)</td>
<td>20.26 (0.18)</td>
<td>18.40 (0.41)</td>
<td></td>
<td>-13.09</td>
<td>6.91</td>
<td>-2.90</td>
</tr>
<tr>
<td>3.06 (0.10)</td>
<td>3.29 (0.13)</td>
<td>3.23 (0.12)</td>
<td>3.52 (0.16)</td>
<td></td>
<td>7.44</td>
<td>5.52</td>
<td>14.82</td>
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<tr>
<td>LWP</td>
<td>75.38 (0.20)</td>
<td>72.73 (0.24)</td>
<td>76.59 (0.36)</td>
<td>74.62 (0.63)</td>
<td>87.1(^{(B)}), 23.0(^{(B)})</td>
<td>-3.52</td>
<td>1.61</td>
</tr>
<tr>
<td>IWP</td>
<td>12.79 (0.04)</td>
<td>11.95 (0.06)</td>
<td>12.70 (0.02)</td>
<td>11.85 (0.03)</td>
<td>25.8(^{(A)}), 29.0(^{(A)})</td>
<td>-6.57</td>
<td>-0.70</td>
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<tr>
<td>SW\textsubscript{NET,TOA}</td>
<td>229.30 (0.11)</td>
<td>232.20 (0.06)</td>
<td>229.10 (0.26)</td>
<td>231.70 (0.26)</td>
<td>241.70(^{(C)}), 240.50(^{(C)})</td>
<td>1.26</td>
<td>-0.09</td>
</tr>
<tr>
<td>LW\textsubscript{TOA}</td>
<td>-224.80 (0.20)</td>
<td>-230.70 (0.16)</td>
<td>-224.40 (0.10)</td>
<td>-230.10 (0.12)</td>
<td>-235.40(^{(C)}), -239.80(^{(C)})</td>
<td>-2.62</td>
<td>0.18</td>
</tr>
<tr>
<td>Imbalance\textsubscript{TOA}</td>
<td>4.52 (0.22)</td>
<td>1.53 (0.14)</td>
<td>4.65 (0.14)</td>
<td>1.58 (0.26)</td>
<td>5.87(^{(C)}), 0.71(^{(C)})</td>
<td>-66.15</td>
<td>2.88</td>
</tr>
<tr>
<td>SCRE</td>
<td>-57.82 (0.12)</td>
<td>-54.83 (0.08)</td>
<td>-58.07 (0.09)</td>
<td>-55.38 (0.25)</td>
<td>-48.50(^{(D)}), -47.14(^{(D)}), -47.04(^{(D)})</td>
<td>5.17</td>
<td>-0.43</td>
</tr>
<tr>
<td>LCRE</td>
<td>33.95 (0.11)</td>
<td>28.90 (0.10)</td>
<td>34.40 (0.06)</td>
<td>29.53 (0.09)</td>
<td>29.42(^{(D)}), 26.87(^{(D)}), 26.00(^{(D)})</td>
<td>-14.87</td>
<td>1.33</td>
</tr>
<tr>
<td>NCRE</td>
<td>-23.87 (0.18)</td>
<td>-25.93 (0.10)</td>
<td>-23.68 (0.14)</td>
<td>-25.86 (0.27)</td>
<td>-19.07(^{(D)}), -19.7(^{(D)}), -21.04(^{(D)})</td>
<td>-8.63</td>
<td>0.80</td>
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<tr>
<td>TCC</td>
<td>70.01 (0.13)</td>
<td>69.04 (0.11)</td>
<td>70.04 (0.14)</td>
<td>69.23 (0.16)</td>
<td>66.83(^{(C)}), 66.7(^{(C)})</td>
<td>-1.39</td>
<td>0.04</td>
</tr>
<tr>
<td>$P_{\text{tot}}$</td>
<td>2.902 (1.9E-05)</td>
<td>3.032 (1.4E-05)</td>
<td>2.892 (2.6E-05)</td>
<td>3.024 (3.1E-05)</td>
<td>2.624(^{(C)}), 2.669(^{(C)})</td>
<td>4.48</td>
<td>-0.34</td>
</tr>
</tbody>
</table>

18 field campaigns (113 total number of flights and in total, 113 flights with about 127 hours in cirrus clouds) covered Europe, Australia, Africa, Seychelles, Brazil, USA, Costa Rica, and tropical Pacific (i.e. between 25\(^{\circ}\)S and 75\(^{\circ}\)N) in the temperature range of 185 – 243 K. This extensive observational data set is compared to the modeled in-cloud ICNCs in Figure 5 (left). The observed ICNC varies between 8 and 80 L\(^{-1}\) over the entire temperature range, and the lower and upper quartiles vary between 0.6 and 300 L\(^{-1}\).

Again, the simulations can be grouped in two sets according to the ice nucleation scheme used in the cirrus regime, i.e. KL+LD/KL+BN and BN+LD/BN+BN, because of their similarities. For most of the temperature range, the simulations which use KL02 in the cirrus regime overestimate the observed ICNCs (although they mostly remain below the 75\(^{th}\) percentile). The overestimation of ICNCs is common to other modeling studies (e.g. Wang and Penner, 2010; Liu et al., 2012; Shi et al., 2015) and especially in cold cirrus clouds (for $T < 205$ K). On the other hand, the simulations which use BN09 in the cirrus regime
are very close to the observations at temperatures below 200 K and between 220 K and 230 K, while they underestimate ICNCs between 200 K and 220 K. In this temperature range the simulations can exceed the observed 25\textsuperscript{th} percentile (although remaining within the 5\textsuperscript{th} percentile). In comparison with the other two simulations, BN+LD and BN+BN always predict lower ICNCs at temperatures below 230 K, as expected because of the competition and PREICE effects. Finally, all four simulations overestimates ICNCs by one order of magnitude in the temperature range 230 – 240 K.

Overall, the simulations BN+LD and BN+BN agree particularly well with the measurements at temperatures lower than 200 K but underestimate the ICNCs within the interval 200 – 220 K, due to an overestimation of the competitive nucleation and PREICE effects. Barahona et al. (2010) showed that the competitive nucleation effect is small using P13. Also, Liu et al. (2012) found that BN09 (using the parameterization of Phillips et al. (2008) for heterogeneous nucleation) and BNhom produced very similar results in the cirrus regime, suggesting that the competitive nucleation effect was small because of the low ICNCs formed heterogeneously. Thus, we can deduce that the PREICE effect is the one which is likely overestimated in our simulations. Interestingly, modeled ICNCs do not show any particular trend, like also Kuebbeler et al. (2014) who used ECHAM-HAM. Differently, other studies found that ICNCs are inversely proportional with temperature, e.g. Liu et al. (2012) and Shi et al. (2015) with CAM5, indifferently if they used the ice nucleation scheme of Liu and Penner (2005) or BN09, and Barahona et al. (2010) with GEOS-5 and BN09. Such distinct behaviours are likely derived from the wide model variabilities in reproducing subgrid-scale processes, like vertical velocity, which play a role in ice nucleation. We reiterate that ICNC is highly dependent on the vertical velocity which is usually poorly represented in terms of spatial and temporal variability (Barahona et al., 2017).

For further information, in Figure 5 (right) we also show the modeled in-cloud ICNCs in the mixed-phase regime, considering the same latitudes as the case before (25\textdegree S - 75\textdegree N). The simulations do not show significant differences among each other. The distinctive features are the ICNC decrease with increasing temperatures and a positive “bulge” between 265 K and 270 K caused by secondary ice production (rime splintering). The modeled ICNCs are in quite good agreement with two data sets of flight measurements taken from the projects Winter Icing Storms Project (WISP-94) and Ice in Clouds Experiment-Layer Clouds (ICE-L), which consider about 99 and 46 flight hours, respectively. It is important to stress that this comparison is less accurate than the previous one because the observations here are much more limited both in time and in space than the extensive observational data used for the cirrus regime. It should be also noted that the measurements actually concern INPs. When the INP number is not high enough to deplete the ambient supersaturation, INP concentrations and ICNCs can correspond, however, it is well known that the two concentrations show discrepancies with increasing temperature because of the secondary ice formation (Kanji et al., 2017). Finally, ICNCs in Figure 5 (right) are in good agreement with the results of Heymsfield et al. (2013), also based on flight campaigns. They found that ICNCs decrease as temperature increases and are within the range 5 – 50 L\textsuperscript{–1} in the mixed-phase regime.

Besides the flight measurements, the recent ICNC estimates from lidar-radar satellite retrievals must be mentioned, e.g. Sourdeval et al. (2018) and Gryspeerdt et al. (2018). In particular, Gryspeerdt et al. (2018) analysed the behaviour of ICNCs within clouds as a function of temperature. Differently from Figure 5 (left), they showed that there is a weak temperature dependence of ICNC, which increases with decreasing temperature. On the other hand, similarly to Figure 5, they found a
Figure 5. In-cloud ice crystal number concentrations ($ICNC_{in-cloud}$, $[L^{-1}]$) versus temperature for modeled results and flight measurements. Medians are computed for modeled results (using daily means between $25^\circ$S and $75^\circ$N, masking $ICNC_{in-cloud} < 0.1 \ L^{-1}$, i.e. the minimum observed value) and observations, for each 1 K temperature bin. They are shown with colored lines: KL+LD (blue), BN+LD (green), KL+BN (light blue), BN+BN (red), and observations (black). Darker gray/red colors indicate the observations/BN+BN between 25$^{th}$ and 75$^{th}$ percentiles, while lighter gray/red colors indicate the observations/BN+BN between 5$^{th}$ and 95$^{th}$. (Left) Cirrus regime: the modeled medians are computed approximately in the range of 4 – 20 km height, the observations come from Krämer (personal communication, not yet published). (Right) Mixed-phase regime: the modeled medians are computed approximately in the range of 0 – 20 km height, the observations belong to the projects WISP-94 (solid line) and ICE-L (dashed line) and concern INP concentrations.

small increase of ICNC around 265 – 270 K and, interestingly, a small peak at about 233 K due to orographic and frontal regimes, which could explain our higher modeled ICNCs between 230 K and 240 K.

5 Conclusions

In this study we have implemented the ice nucleation scheme of Barahona and Nenes (2009) into the global chemistry-climate model EMAC. The parameterization takes into account the water vapour competition between homogeneous and heterogeneous nucleation and has been modified to consider also the depositional growth of pre-existing ice crystals. Heterogeneous nucleation can be computed through different INP parameterizations, and we have chosen the empirical INP parameterization of Phillips et al. (2013) for our experiments. We have tested the BN09 scheme operating in the the cirrus and/or in the mixed-phase regimes and compared the results with the standard configuration of the model, which assumes that cirrus clouds form via pure homogeneous nucleation (Kärcher and Lohmann, 2002) and uses the immersion nucleation parameterization of Lohmann and Diehl (2006) for mixed-phase clouds.

Focusing on the ice-related results, e.g. ICNC and IWC, we found that using BN09 in the cirrus regime strongly reduces the total ICNC worldwide because of the competition and PREICE effects, however, increases ICNC along the tropics. In contrast, BN09 in the mixed-phase regime produces slightly higher ICNCs, especially in the NH where mineral dust particles are more
abundant. We found that changing the ice nucleation scheme in the cirrus regime generates larger differences of ICNC and IWC than changing parameterization in the mixed-phase regime, that is the simulations using the same parameterization in the cirrus regime (e.g. BN+LD and BN+BN) are easily discernible from the others (LD+KL and LD+BN). Interestingly, we observed a certain dependence of ICNC and IWC in the mixed-phase regime on the parameterization used for cirrus clouds, likely due to a faster sedimentation of larger ice crystals produced by BN09 in cirrus clouds at higher altitudes.

Overall, all modeled results agree well with global observations and the literature data. The comparison made with flight measurements has pointed out that ICNCs are overestimated by KL02 in the cirrus regime. BN09 agrees well with the observations in cold cirrus clouds, however, the PREICE effect is likely overestimated causing the underestimation of ICNCs between 200 K and 220 K.

As BN09 takes into account additional processes which were previously neglected by the standard version of the model, without consuming extra computational resources, we recommend to apply this ice nucleation scheme in future EMAC simulations. We also suggest to select P13 among the INP parameterizations available in BN09, since it incorporates the ice-nucleating ability of different aerosol species (dust, soot, bioaerosols, and soluble organics) and simulates both deposition and immersion/condensation nucleation. By using the configuration BN+BN, the EMAC model becomes one of the few GCMs which take into account in a detailed manner the complexity of ice nucleation. Finally, this work offers further material for future GCM comparisons with focus on ICNC estimates and for future modeling evaluations against flight measurements and lidar-radar satellite retrievals.

\textit{Code and data availability.} The Modular Earth Submodel System (MESSy) is continuously further developed and applied by a consortium of institutions. The usage of MESSy and access to the source code is licensed to all affiliates of institutions, which are members of the MESSy Consortium. Institutions can become a member of the MESSy Consortium by signing the MESSy Memorandum of Understanding. More information can be found on the MESSy Consortium Website (http://www.messy-interface.org). All code modifications presented in this article will be included in the next version of MESSy.

\textbf{Appendix A}

In this Appendix we provide some additional technical information about the implementation of BN09 into the EMAC model. The BN09 parameterization has been added as a Fortran95 module in the submodel core layer (SMCL) of MESSy (named as \texttt{messy\_cloud\_ice\_BN09.f90}). BN09 operates in the cirrus regime and/or in the mixed-phase regime according to the calls made in the CLOUD submodel (\texttt{messy\_cloud\_lohmann10.f90}). As shown in Figure 1, BN09 computes the newly formed ice crystals in the cirrus regime when ni\textsubscript{nc}=3 and in the mixed-phase regime when limm\textsubscript{BN09}=\texttt{.TRUE.}, where ni\textsubscript{nc} and limm\textsubscript{BN09} are variables defined in the namelist-file \texttt{cloud.nml} (the setup of \texttt{cloud.nml} for the simulation BN+BN is shown in Table S1 as an example).

Other changes made during the implementation are the following ones.
– **Temperature threshold.** The original BN09 assumes the value $235 \, K$ as temperature threshold between the two regimes, while the CLOUD submodel uses the value $238.15 \, K$. For consistency, we used the second threshold as limit condition to call BN09, and we changed the original threshold of BN09 to the value $238.15 \, K$ inside the BN09 code.

– **Number concentration and diameter of cloud droplets.** The original BN09 computes the cloud droplet number concentration starting from the number concentration of sulfate aerosol in the Aitken mode. However, since the EMAC model computes the activated cloud droplet number concentration via other parameterizations (e.g. Abdul-Razzak and Ghan, 2000; Lin and Leaitch, 1997; Karydis et al., 2017), we provide BN09 with such variable (neglecting the corresponding computations inside the BN09 code). Unfortunately, these parameterizations do not compute the diameter of the new cloud droplets, therefore, BN09 still computes the diameter using the wet diameter of aerosol in the Aitken mode (i.e. $D_c$).

*Competing interests.* The authors declare that they have no conflict of interest.

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References


Fountoukis, C. and Nenes, A.: ISORROPIA II: a computationally efficient thermodynamic equilibrium model for $K^+\cdot Ca^{2+}\cdot Mg^{2+}\cdot NH_4^+\cdot Na^+\cdot SO_4^{2-}\cdot NO_3^-\cdot Cl^-\cdot H_2O$ aerosols, Atmospheric Chemistry and Physics, 7, 4639–4659, https://doi.org/10.5194/acp-7-4639-2007, https://www.atmos-chem-phys.net/7/4639/2007/, 2007.


