



1 **Fast domain-aware neural network emulation of a planetary  
2 boundary layer parameterization in a numerical weather forecast  
3 model**

4 <sup>1</sup>Jiali Wang, <sup>2</sup>Prasanna Balaprakash, and <sup>1</sup>Rao Kotamarthi\*

5 <sup>1</sup>Environmental Science Division, Argonne National Laboratory, 9700 South Cass Avenue,  
6 Lemont, IL 60439, USA

7 <sup>2</sup>Mathematics and Computer Science Division, Argonne National Laboratory, 9700 South Cass  
8 Avenue, Lemont, IL 60439, USA

9 *Correspondence to:* Rao Kotamarthi ([vrkotamarthi@anl.gov](mailto:vrkotamarthi@anl.gov))

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11 **Abstract.** Parameterizations for physical processes in weather and climate models are  
12 computationally expensive. We use model output from a set of simulations performed using the  
13 Weather Research Forecast (WRF) model to train deep neural networks and evaluate whether  
14 trained models can provide an accurate alternative to the physics-based parameterizations.  
15 Specifically, we develop an emulator using deep neural networks for a planetary boundary layer  
16 (PBL) parameterization in the WRF model. PBL parameterizations are commonly used in  
17 atmospheric models to represent the diurnal variation of the formation and collapse of the  
18 atmospheric boundary layer—the lowest part of the atmosphere. The dynamics of the atmospheric  
19 boundary layer, mixing and turbulence within the boundary layer, velocity, temperature, and  
20 humidity profiles are all critical for determining many of the physical processes in the atmosphere.  
21 PBL parameterizations are used to represent these processes that are usually unresolved in a typical  
22 numerical weather model that operates at horizontal spatial scales in the tens of kilometers. We  
23 demonstrate that a domain-aware deep neural network, which takes account of underlying domain  
24 structure that are locality specific (e.g., terrain, spatial dependence vertically), can successfully  
25 simulate the vertical profiles within the boundary layer of velocities, temperature, and water vapor  
26 over the entire diurnal cycle. We then assess the spatial transferability of the domain-aware neural  
27 networks by using a trained model from one location to nearby locations. Results show that a single  
28 trained model from a location over the midwestern United States produces predictions of wind  
29 components, temperature, and water vapor profiles over the entire diurnal cycle and all nearby  
30 locations with errors less than a few percent when compared with the WRF simulations used as  
31 the training dataset.



## 32 1 Introduction

33 Model developers use approximations to represent the physical processes involved in climate and  
34 weather that cannot be resolved at the spatial resolution of the model grids or in cases where the  
35 phenomena are not fully understood (Williams, 2005). These approximations are referred to as  
36 parameterizations (McFarlane, 2011). While these parameterizations are designed to be  
37 computationally efficient, calculation of a model physics package still takes a good portion of the  
38 total computational time. For example, in the community atmospheric model (CAM) developed  
39 by National Center for Atmospheric Research (NCAR), with spatial resolution of approximately  
40 300 km and 26 vertical levels, the physical parameterizations account for about 70% of the total  
41 computational burden (Krasnopolksy and Fox-Rabinovitz, 2006). In the Weather Research  
42 Forecast (WRF) model, with spatial resolution of tens of kilometers, time spent by physics is  
43 approximately 40% of the computational burden. The input and output overhead is around 20% of  
44 the computational time at low node count (100's) and can increase significantly at higher node  
45 count as a percentage of the total wall-clock time.

46 An increasing need in the climate community is performing high spatial resolution simulations (10  
47 km or less grid spacing) and generating large ensembles of these simulations in order to address  
48 uncertainty in the model projections and to assess risk and vulnerability. Developing process  
49 emulators (Leeds et al., 2013; Lee et al., 2011) that can reduce the time spent in calculating the  
50 physical processes will lead to much faster model simulations, enabling researchers to generate  
51 high spatial resolution simulations and a large number of ensemble members.

52 A neural network (NN) is composed of multiple layers of simple computational modules, where  
53 each module transforms its inputs to a nonlinear output. Given sufficient data, an appropriate NN  
54 can model the underlying nonlinear functional relationship between inputs and outputs with  
55 minimal human effort. During the past two decades, NN techniques have found a variety of  
56 applications in atmospheric science. For example, Collins and Tossot (2015) developed an  
57 artificial NN model by taking numerical weather prediction model (e.g., WRF) output as input to  
58 predict thunderstorm occurrence within a few hundreds of square kilometers about 12 hours in  
59 advance. Krasnopolksy et al. (2016) used NN techniques for filling the gaps in satellite  
60 measurements of ocean color data. Scher (2018) used deep learning to emulate the complete  
61 physics and dynamics of a simple general circulation model and indicated a potential capability of



weather forecasts using this NN-based emulator. Neural networks are particularly appealing for emulations of model physics parameterizations in numerical weather and climate modeling, where the goal is to find nonlinear functional relationship between inputs and outputs (Cybenko, 1989; Hornik, 1991; Chen and Chen, 1995a,b; Attali and Pagès, 1997). NN techniques can be applied to weather and climate modeling in two ways. One approach involves developing new parameterizations by using NNs. For example, Chevallier et al. (1998; 2000) developed a new NN-based longwave radiation parameterization, NeuroFlux, which has been used operationally in the European Centre for Medium-Range Weather Forecasts four-dimensional variational data assimilation system and is eight times faster than the previous parameterization. Krasnopolksy et al. (2013) developed a stochastic convection parameterization based on learning from data simulated by a cloud-resolving model, CRM, initialized with and forced by the observed meteorological data. The NN convection parameterization was tested in the NCAR CAM and produced reasonable and promising results for the tropical Pacific region. Jiang et al. (2018) developed a deep NN-based algorithm or parameterization to be used in the WRF model to provide flow-dependent typhoon-induced sea surface temperature cooling. Results based on four typhoon case studies showed that the algorithm reduced maximum wind intensity error by 60–70% compared with using the WRF model. The other approach for applying NN to weather and climate modeling is to emulate existing parameterizations in these models. For example, Krasnopolksy et al. (2005) developed an NN-based emulator for imitating an existing atmospheric longwave radiation parameterization for the NCAR CAM. They used output from the CAM simulations with the original parameterization for the NN training. They found the NN-based emulator was 50–80 times faster than the original parameterization and produced almost identical results.

We study NN models to emulate existing physical parameterizations in atmospheric models. Process emulators that can reproduce physics parameterization can ultimately lead to the development of a faster model emulator that can operate at very high spatial resolution as compared with most current model emulators that have tended to focus on simplified physics (Kheshgi et al., 1999). Specifically, this study involves the design and development of a domain-aware NN to emulate a PBL parameterization using 22-year-long output created by a set of WRF simulations. To the best of our knowledge, we are among the first to apply deep neural networks to the WRF model to explore the emulation of physics parameterizations. As far as we know from the literature available at the time of this writing, the only application of NNs for emulating the



parameterizations in the WRF model is by Krasnopolsky et al. (2017). In their study, a three-layer NN was trained to reproduce the behavior of the Thompson microphysics (Thompson 2008) scheme in the WRF-ARW model. While we focus on learning the PBL parameterization and developing domain-aware NN for emulation of PBL, the ultimate goal of our on-going project is to build an NN-based algorithm to empirically understand the process in the numerical weather/climate models that could be used to replace the physics parameterizations that were derived from observational studies. This emulated model would be computationally efficient, making the generation of large ensemble simulations feasible at very high spatial/temporal resolutions with limited computational resources. The key objectives of this study are to answer the following questions specifically for PBL parameterization emulation: (1) What and how much data do we need to train the model? (2) What type of NN should we apply for the PBL parameterization studied here? (3) Is the NN emulator accurate compared with the original physical parameterization? This paper is organized as follows. Section 2 describes the data and the neural network developed in this study. The efficacy of the neural network is investigated in Section 3. Discussion and summary follow in Section 4.

## 2 Data and Method

### 2.1 Data

The data we use in this study is output from the regional climate model WRF version 3.3.1. WRF is a fully compressible, nonhydrostatic, regional numerical prediction system with proven suitability for a broad range of applications. The WRF model configuration and evaluations are given by Wang and Kotamarthi (2014). Covering all the troposphere are 38 vertical layers, between the surface to approximately 16 km (100 hPa). The lowest 17 layers cover from the surface to about 2 km above the ground. The PBL parameterization we used for this WRF simulation is known as the YSU scheme (Yonsei University; Hong et al., 2006). The YSU scheme uses a nonlocal-mixing scheme with an explicit treatment of entrainment at the top of the boundary layer and a first-order closure for the Reynolds-averaged turbulence equations of momentum of air within the PBL.

We use the output of the WRF model driven by NCEP-R2 for the period 1984–2005. The 22-year data was partitioned into three parts: a training set consisting of 20 years (1984–2003) of 3-hourly



122 data to train the NN; a development set (also called validation set) consisting of 1 year (2004) of  
123 3-hourly data used to tune the algorithm's hyperparameters and to control overfitting (the situation  
124 where the trained network predicts well on the training data but not on the test data); and a test set  
125 consisting of 1 year of records (2005) for prediction and evaluations. The goal of the work  
126 described here is to develop an NN-based parameterization that can be used to replace the PBL  
127 parameterization in the WRF model. Thus, we expect the NN submodel to receive a set of inputs  
128 that are equivalent to the inputs provided to the YSU scheme at each timestep. However, a key  
129 difference in our approach is that the vertical profiles of various state variables are reconstructed  
130 by the NN using only the inputs (near-surface variables and 700 hPa geostrophic winds).

131 Table 1 shows the architecture in terms of inputs and outputs used in our experiments. The inputs  
132 are near-surface characteristics including 2-meter water vapor, 2-meter air temperature, 10-meter  
133 zonal and meridional wind, ground heat flux, incoming shortwave radiation, incoming longwave  
134 radiation, PBL height, sensible heat flux, latent heat flux, surface friction velocity, ground temp,  
135 soil temperature at 2 m below the ground, soil moisture at 0–0.3cm below the ground, and  
136 geostrophic wind component at 700 hPa. The outputs for the NN architecture are the vertical  
137 profiles of the following model prognostic and diagnostic fields: temperature, water vapor mixing  
138 ratio, and zonal and meridional wind (including speed and direction). In this study we develop an  
139 NN emulation of the PBL parameterization; hence we focus only on predicting the profiles within  
140 the PBL, which is on average around 200 m and 400 m during the night and afternoon of winter,  
141 respectively, and around 400 m and 1300 m during the night and afternoon of summer,  
142 respectively, for the locations studied here. The middle and upper troposphere (all layers above  
143 the PBL) are considered fully resolved by the dynamics simulated by the model and hence not  
144 parameterized. Therefore, we do not consider the levels above PBL height because (1) they carry  
145 no information about input/output functional dependence that affects the PBL and (2) if not  
146 removed, they introduce additional noise in training. Specifically, we use the WRF output from  
147 the first 17 layers, which are within 1,900 meters and well cover the PBL.

## 148 **2.2 Deep neural networks for PBL parameterization emulation**

149 A class of machine learning approaches that is particularly suitable for emulation of PBL  
150 parameterization is supervised learning. This approach models the relationship between the  
151 outputs and independent input variables by using training data  $(x_i, y_i)$ , for  $x_i \in T \subset D$ , where  $T$  is



152 a set of training points,  $D$  is the full data set, and  $x_i$  and  $y_i = f(x_i)$  are inputs and its corresponding  
153 output  $y_i$ , respectively. The function  $f$  that maps the inputs to the outputs is typically unknown and  
154 hard to derive analytically. The goal of the supervised learning approach is to find a surrogate  
155 function  $h$  for  $f$  such that the difference between  $f(x_i)$  and  $h(x_i)$  is minimal for all  $x_i \in T$ . Many  
156 supervised learning algorithms exist in the machine learning literature. In this paper, we focus on  
157 deep neural networks (DNNs).

158 DNNs are composed of neural layers: a stack of nodes organized in a hierarchical way to model a  
159 nonlinear function. Within each neural layer, nodes receive inputs from previous neural layers and  
160 perform certain nonlinear transformations through a system of weighted connections on the  
161 received input values. The training data is given to the neural network through the input neural  
162 layer. The last neural layer of the stack in the network is the output neural layer from which the  
163 predicted values are obtained. The training procedure consists of modifying the weights of the  
164 connections in the network to minimize a user-defined objective function that measures the  
165 prediction error of the network. Each iteration of the training procedure comprises two phases: the  
166 forward pass consists of passing the training data to the network and computing the prediction  
167 error; in the backward pass, the gradients of the error function with respect to all the weights in  
168 the network is computed and used to update the weights in order to minimize the error. Once the  
169 entire dataset is passed both forward and backward through the neural network (with many  
170 iterations), one epoch is completed.

171 We consider three variants of DNN (see below). We construct all of them using a neural block that  
172 comprises a dense neural layer with  $N$  nodes and a rectified linear activation function, where  $N$  is  
173 user-defined parameters.

174 **Naïve DNN:**

175 **Deep feed-forward neural network (FFN):** This is a fully connected feed-forward deep neural  
176 network constructed as a sequence of  $K$  neural blocks, where the input of the  $i$ th neural block is  
177 from  $\{i-1\}$ th block and the output of the  $i$ th neural block is given as the input of the  $\{i+1\}$ th neural  
178 block. The sizes of the input and output neural layers are 16 (= near-surface variables) and 85 (=  
179 17 vertical levels  $\times$  5 output variables). See Figure 1a for an illustration.

180 **Domain-aware DNN:**



181 While the FFN is a typical way of applying NN for finding the nonlinear relationship between  
182 input and output, a key drawback of the naïve FFN is that it does not consider the underlying PBL  
183 domain structure, such as the patterns that are locality specific and the vertical dependence between  
184 different vertical levels of each profile. This is not typically needed for NNs in general and in fact  
185 is usually avoided because, for classification and regression, one can find visual features regardless  
186 of their locations. For example, a picture can be classified as a certain object even that object has  
187 never appeared in the given location in the training set. In our case, however, the location is fixed  
188 and the profiles over that location is distinguishable from other locations if they have different  
189 terrain conditions. Consequently, we want to learn the particular influence of location in the  
190 forecast. For example, the feature at a lower level of a profile plays a role in the feature at a higher  
191 level and can help refine the output at the higher level and accordingly the entire profile. This  
192 dependence may inform the NN and provide better accuracy and data efficiency. To that end, we  
193 develop two variants of domain-aware DNNs for PBL emulation.

194 **Hierarchically connected network with previous layer only connection (HPC):** We assume  
195 that the outputs at each altitude level depend not only on the 16 near-surface variables but also on  
196 the altitude level below it. To model this explicitly, we develop a domain-aware DNN variant in  
197 which 17 neural blocks are connected as follows: the input to an  $i$ th ( $i > 1$ ) neural block comprises  
198 the input neural layer of the 16 near-surface variables and the 5 outputs of the  $\{i-1\}$ th neural block.  
199 The first neural block, which is next to the input layer, receives inputs only from the input neural  
200 layer of the 16 near-surface variables. See Figure 1b for an example.

201 **Hierarchically connected network with all previous layers connection (HAC):** We assume that  
202 the outputs at each PBL depend not only on the 16 near-surface variables but also on all altitude  
203 levels below it. The input to an  $i$ th neural block comprises the input neural layer of the 16 near-  
204 surface variables and all outputs of the  $\{1, 2, \dots, i-1\}$  neural blocks below it. See Figure 1c for an  
205 example.

## 206 **2.3 Setup**

207 For preprocessing, we applied StandardScaler (removes the mean and scales each variable to unit  
208 variance) and MinMaxScaler (scales each variable between 0 and 1) transformations before



209 training, and we applied the inverse transformation after prediction so that the evaluation metrics  
210 are computed on the original scale.

211 We note that there is no default value for  $N$  nodes in a dense neural layer. We conducted an  
212 experimental study on FFN and found that setting  $N$  to 16 results in good predictions. Therefore,  
213 we used the same value of  $N = 16$  in HPC and HAC.

214 For the implementation of DNN, we used Keras (version 2.0.8), a high-level neural network  
215 Python library that runs on the top of the TensorFlow library (version 1.3.0). We used the scikit-  
216 learn library (version 0.19.0) for the preprocessing module. The experiments were run on a Python  
217 (Intel distribution, version 3.6.3) environment.

218 All three DNNs used the following setup for training: optimizer = adam, learning rate = 0.001,  
219 epochs = 1000, batch size = 64. Note that batch size and number of epochs define the number of  
220 randomly sampled training points required before updating the model parameters and the number  
221 times that training will work through the entire training dataset. To avoid overfitting issues in  
222 DNNs, we use an early stopping criterion in which the training stops when the validation error  
223 does not reduce for 10 subsequent epochs.

224 We ran training and inference on a NVIDIA DGX-1 platform: Dual 20-Core Intel Xeon E5-2698  
225 v4 2.2 GHz processor with 8 NVIDIA P100 GPUs with 512 GB of memory. The DNN's training  
226 and inference leveraged only a single GPU.

### 227 **3 Results**

228 In the following discussion we evaluate the efficacy of the three DNNs by comparing their  
229 prediction results with WRF model simulations. We refer to the results of WRF model simulations  
230 as observations because the DNN learns all the knowledge from the WRF model output, not from  
231 in situ measurements. We refer to the values from the DNN models as predictions. We initiate our  
232 DNN development at one grid cell from WRF output that is close to a site in the midwestern United  
233 States (Logan, Kansas, latitude= 38.8701°N; longitude= 100.9627°W) and another grid cell at a  
234 site in Alaska (Kenai Peninsula Borough, AK, latitude= 60.7237 °N; longitude=150.4484 °W) to  
235 evaluate the robustness of the developed DNNs. We then apply our DNNs to stations within 800  
236 km from the Logan site to assess the spatial transferability of the DNNs. While the Alaska site has



237 different vertical profiles, especially for wind directions, and lower PBL heights in both January  
238 and July, the conclusion in terms of the model performance is similar to the site over Logan,  
239 Kansas.

### 240 **3.1 DNN performance in temperature and water vapor**

241 Figure 2 shows the diurnal variation (explicitly 3 PM and 12 AM local time at Logan, Kansas) of  
242 temperature and water vapor mixing ratio vertical profiles in the first 17 layers from the  
243 observation and three DNN model predictions. The 17 layers are within 1,900 meters and well  
244 cover the PBL. The figures present results for both January and July. The dashed lines show the  
245 lowest and highest (5<sup>th</sup> and 95<sup>th</sup> percentile, respectively) PBL heights for that particular time. In  
246 general, the DNNs are able to produce similar shapes of the observed profiles, especially within  
247 the PBL. Both the temperature and water vapor mixing ratio are lower in January and higher in  
248 July. Within the PBL, the temperature and water vapor do not change much with height; above the  
249 PBL to the entrainment zone, the temperature and water vapor start decreasing. Among the three  
250 DNNs, HAC and HPC show very low bias and high accuracy in the PBL, but the FFN shows a  
251 relatively large discrepancy from the observation. Figure 3 shows the root-mean-square error  
252 (RMSE) and Pearson correlation coefficient (COR) between observation and three DNN  
253 predictions in the afternoon and midnight of January and July. The RMSE and COR consider not  
254 only the time series of observation and prediction but also their vertical profiles below the PBL  
255 heights for each particular time. Among the three DNNs, HPC and HAC always show better skill  
256 with smaller RMSEs and higher CORs than does FFN. The reason is that the FFN uses only the  
257 16 near-surface variables as inputs and does not consider dependence between each of the vertical  
258 levels. In contrast, HPC and HAC use not only the near-surface variables but also the five variables  
259 of one previous vertical level (HPC) or all previous vertical levels (HAC) as inputs for predicting  
260 the profiles of each field. This approach is important because PBL parameterizations are used to  
261 represent the vertical dependence of these variables and are usually unresolved in a typical climate  
262 and weather models that operate at horizontal spatial scales in the tens of kilometers. Compared  
263 with HAC, HPC sometimes shows slightly better accuracy with smaller RMSEs and higher CORs,  
264 but in other cases HPC performs similar to HAC. These results indicate that the information from  
265 all previous levels is not as important as information from the previous layer right below the  
266 predicted layer.



### 267 3.2 DNN performance in wind component

268 Figure 4 shows the diurnal variation of wind (including wind speed and direction) profiles in  
269 January and July 2005 from observation and three DNN predictions. Compared with the  
270 temperature and water vapor profiles, the wind profiles are more difficult to predict, especially for  
271 days (e.g., summer) that have a higher PBL. The wind direction does not change much below the  
272 majority of the PBL, and it turns to westerly winds when going up and beyond the PBL. The DNN  
273 prediction has difficulty predicting the profile above the PBL height, as is expected because these  
274 layers are considered fully resolved by the dynamics simulated by the WRF model and hence not  
275 parameterized. Therefore, we do not consider DNN performance at the levels above PBL height,  
276 because the DNNs carry no information about input/output functional dependence that affects the  
277 PBL. The wind speed increases with height in both January and July within the PBL. Above the  
278 PBL heights, the wind speed still increases in January but decreases in July. The reason is that in  
279 January the zonal wind, especially westerly wind, is dominant in the atmosphere and the wind  
280 speed increases with height; in July, however, the zonal wind is relatively weak, and the meridional  
281 wind is dominant with southerly wind below ~2 km and northerly wind above 2 km. The decrease  
282 in wind speed above the PBL is just about the transition of wind direction from southerly to  
283 northerly wind. Figure 5 shows the RMSEs and CORs between the observed and predicted wind  
284 component within the PBL. The wind component is fairly well predicted especially by the HAC  
285 and HPC networks with correlation above 0.8 for wind speed and 0.7 for wind direction except in  
286 July at midnight, which is below zero. Similar to the predictions for temperature and water vapor,  
287 the FFN shows the poorest prediction accuracy, especially for wind direction. For accurately  
288 predicting the wind direction, we found that using the geostrophic wind at 700 hPa as one of the  
289 inputs for the DNNs is important.

### 290 3.3 DNN dependence on length of training period

291 Next, we evaluate how sensitive the DNN is to the amount of available training data and how much  
292 data one would need in order to train a DNN. While we present Figures 2–5 using 20-year (1984–  
293 2003) training data, here we gradually decrease the length of the training set to 12 (1992–2003), 6  
294 (1998–2003), 2 (2002–2003) years, and 1 (2003) year. The validation data (for tuning hyper-  
295 parameters and controlling overfit) and the test data (for prediction) are kept the same as in our  
296 standard training dataset, which is year 2004 and 2005, respectively. Figures 6 and 7 show the



297 RMSE and CORs between observed and predicted profiles of temperature, water vapor, and wind  
298 component for January and July at their local midnight. Overall, the FFN network depends heavily  
299 on the length of training dataset. For example, the RMSE of FFN predicted temperature decreases  
300 from 7.2 K using one year of training data to 3.0 K using 20-year training data. HAC and HPC  
301 also depend on the length of training data especially when less than 6-year training data is  
302 available, but even their worst prediction accuracy (using one year of training data) is still better  
303 than FFN using 20-year training data. The RMSEs of HPC and HAC predicted temperature  
304 decrease from ~2.4 using 1 year of training data to ~1.5 using 20 years of training data. The CORs  
305 of FFN predicted temperature increase from 0.73 using one year of training data to 0.92 using 20  
306 years of training data. The CORs for HPC and HAC increase slightly with more training data, but  
307 overall they are above 0.85 using one year to 20 years of training data.

308 Regarding the question about how much data one would need to train a DDN, for FFN, at least  
309 from this study, the performance is not stable until one has 12 or more years of training data, which  
310 is significantly better than having only 6 years or less of training data. For HAC and HPC, however,  
311 having 6 years of training data seems sufficient to show a stable prediction. Increasing the amount  
312 of training data shows only marginal improvement in predictive accuracy. In fact, in contrast to  
313 HAC and HPC, the performance of FFN has not reached a plateau even with the 20 years of  
314 training data. This suggests that with longer training sets the predicting skill of an even naïve  
315 approach like FFN could be further improved and eventually reach the accuracy of HAC and HPC  
316 using 6 or more years of training data.

### 317 **3.4 DNN performance for nearby stations**

318 This section assesses the spatial transferability of the domain-aware neural networks (specifically  
319 HAC and HPC) by using a trained model from one location (at Logan, Kansas, as presented above)  
320 to other locations within 800 kilometers from the Logan site with different terrain conditions and  
321 vegetation types. We choose ten locations, as shown in Figure 8, among which two (Sites 1 and 2)  
322 are 300 km away from the Logan site; three (Sites 3, 4, and 5) are 430 km away from the Logan  
323 site; and five (Sites 6 to 10) are 450–800 km away from the Logan site, with Sites 9 and 10 the  
324 furthest and having the most different elevations from the Logan site. Different from the preceding  
325 section, here we calculate normalized RMSEs relative to each site's observations at a particular  
326 time, in order to make the comparison feasible between different sites. As shown in Figures 9 and



327 10 by the normalized RMSEs and Pearson correlations, in general, when going farther from Logan  
328 site, where our domain-aware neural networks (HPC and HAC) were developed, the prediction  
329 skill either does not change or gets slightly worse depending on the locations and the difference in  
330 terrain conditions between the reference site (Logan, Kansas) and the remote sites (S1 to S10 in  
331 Figure 8). For example, the RMSEs for wind direction over Sites 2, 4, and 8 are similar to that  
332 over the Logan site. However, the RMSEs over the other sites, which have different elevations  
333 (either higher or lower) than that for Logan site, are much larger, suggesting the DNNs developed  
334 based on Logan site are not applicable for these locations. These results indicate that, at least for  
335 this study, as long as the terrain conditions (slope, elevation, and orientation) are similar, the DNNs  
336 can be applied with similar prediction skill for locations that are as far as 520 km (equal to more  
337 than 40 grid cells in the WRF output used in this study) to predict the wind and also other variables  
338 assessed in this study. The results also suggest that when implementing the NN-based algorithm  
339 into the WRF model, if a number of grid cells are over a homogenous region, one may not need to  
340 train the NN over every grid cell. This will significantly save computing time because the training  
341 process takes the majority of the computing resource (see below). Similar to Figure 6, we see that  
342 the HPC network works better than HAC especially for temperature and water vapor over all the  
343 sites and for wind component over most of the sites examined here, indicating that the input from  
344 all previous layers is not as important as that from the input from only the layer next to the predicted  
345 layer.

### 346 **3.5 DNN training and prediction time**

347 Table 2 shows the number of epochs and time required for training FNN, HPC, and HAC for  
348 various numbers of training years. Because of the early stopping criterion, the number of training  
349 epochs performed by different methods is not same. Despite setting the maximum epochs to 1,000,  
350 all these methods terminate within 178 epochs. We observed that HPC performs more training  
351 epochs than do FFN and HAC: given the same optimizer and learning rate for all the methods,  
352 HPC has a better learning capability because it can improve the validation error more than HAC  
353 and FNN can. For a given set of training data, the difference in the training time per epoch can be  
354 attributed to the number of trainable parameters in FNN, HPC, and HAC (10,693, 16,597, and  
355 26,197, respectively). As we increase the size of training data, the training time per epoch increases  
356 significantly for all three DNN models. The increase also depends on the number of parameters in



357 the model. For example, increasing the training data from 1 year to 20 years increases the training  
358 time per epoch from 1.4 seconds to 11.4 seconds for FNN, from 1.1 seconds to 17.4 seconds, and  
359 from 1.4 seconds to 19.6 seconds for HPC and HAC, respectively.

360 The prediction times of FNN, HPC, and HAC are within 0.5 seconds for one-year data, making  
361 these models promising for PBL emulation deployment. The difference in the prediction time  
362 between models can be attributed to the number of parameters in the DNNs: the larger the number  
363 of parameters, the higher the prediction time. For example, the prediction times for FFN are below  
364 0.2 seconds when using different numbers of years for training, while those for HAC are around  
365 0.4 seconds. Despite the difference in the number of training years, the number of parameters for  
366 a given model is fixed. Therefore, once the model is trained, the DNN prediction time depends  
367 only on the model and the number of points in the test data (1 year in this study). Theoretically,  
368 for the given model and the test data, the prediction time should be constant even with different  
369 amounts of training dataset. However, we observed slight variations in the prediction times that  
370 range from 0.17 to 0.29 seconds for FNN, 0.30 to 0.34 seconds for HPC, and 0.36 to 0.42 seconds  
371 for HAC, which can be attributed to the system software.

## 372 **4 Summary and Discussion**

373 This study developed DNNs for emulating a PBL parameterization that is used by the WRF model.  
374 Two of the DNNs take into account the domain-specific features such as spatial dependence in the  
375 vertical direction over the location where we develop the DNNs. The input and output data for the  
376 DNNs are taken from a set of 22-year-long WRF simulations. We developed the DNNs based on  
377 a midwestern location in the United States. We found that the domain-aware DNNs can reproduce  
378 the vertical profiles of wind, temperature, and water vapor mixing ratio with high accuracy yet  
379 require fewer data than the traditional DNN, which does not care about the domain-specific  
380 features. The training process takes the majority of the computing time. Once trained, the model  
381 can quickly predict the variables with decent accuracy. This ability makes the deep neural network  
382 appealing for parameterization emulator.

383 Following the same architecture that we applied for Logan, Kansas, we also built DNNs for one  
384 location at Alaska. The results share the same conclusion as we have seen for the Logan site. For  
385 example, among the three DNNs, HPC and HAC show much better skill with smaller RMSEs and



386 higher correlations than does FFN. The wind profiles are more difficult to predict than the profiles  
387 of temperature and water vapor. For FFN, the prediction accuracy increases with more training  
388 data; for HPC and HAC, the prediction skill stays similar when having six or more years of training  
389 data.

390 While we trained our DNNs over individual locations in this study using only one computing node  
391 (with multiple processors), there are 300,000 grid cells over our WRF model domain, which  
392 simulated the North American continent as a horizontal resolution of 12 km. To train a model for  
393 all the grid cells or all the homogeneous regions over this large domain, we will need to scale up  
394 the algorithm to hundreds if not thousands of computing nodes to accelerate the training time and  
395 the make the entire NN-based simulation faster than the original parameterization.

396 The ultimate goal of this project is to build an NN-based algorithm to empirically understand the  
397 process in the numerical weather and climate models and to replace the PBL parameterization and  
398 other time-consuming parameterizations that were derived from observational studies. This  
399 emulated model thus would be computationally efficient and enable researchers to generate large  
400 ensemble simulations at very high spatial/temporal resolutions with limited computational  
401 resources. The DNNs developed in this study can provide numerically efficient solutions to a wide  
402 range of problems in environmental numerical models where lengthy, complicated calculations  
403 describing physical processes must be repeated frequently or need a large ensemble of simulations  
404 to represent uncertainty. A possible future direction for this research is implementing these NN-  
405 based schemes in WRF for a new generation of hybrid regional-scale weather/climate models that  
406 fully represent the physics at a very high spatial resolution at a fast computational time so as to  
407 provide the means for generating large ensemble model runs.

408 *Data and code availability.* The data used and the code developed in this study are available at  
409 <https://github.com/pbalapra/dl-pbl>.

410 *Author contributions.* JW participated in the entire project by providing domain expertise and  
411 analyzing the results from the NN-based emulator. PB developed the deep neural networks and  
412 did all the experiments presented in this study. RK proposed the idea of this project and provided  
413 high-level guidance and insight for the entire study.



414     *Competing interests.* The authors declare that they have no conflict of interest.  
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507

## 508 **Figure captions**

509 **Figure 1:** Three variants of DNN developed in this study: (a) fully connected feed forward  
510 neural network (FFN), (b) hierarchically connected network with previous layer only  
511 connection (HPC), and (c) hierarchically connected network with all previous layers  
512 connection (HAC).

513 **Figure 2:** Temperature and water vapor mixing ratio from the observation and three DNN  
514 predictions: FFN, HPC, and HAC in January and July 2005 at 3 PM and 12 AM local time.  
515 The y-axis uses log scale. The training data are from 20 years (1984 to 2003) of 3-hourly WRF  
516 output. The lower and upper dash lines show the lowest and highest (5<sup>th</sup> and 95<sup>th</sup> percentile)  
517 PBL heights at that particular time. For example, in January 12 AM, the lowest PBL height  
518 is about 19 m, while the highest PBL height is about 365 m.

519 **Figure 3:** RMSE and correlations for time series of temperature and water vapor vertical  
520 profiles within the PBL predicted by the three DNNs compared with the observations. The  
521 vertical lines show the range of RMSEs and correlations when considering the lowest and  
522 highest PBL heights at each particular time (shown by the dashed horizontal lines in Figure  
523 2). The training data are 3-hourly WRF output from 1984 to 2003.

524 **Figure 4:** Same as Figure 2 but for wind direction and wind speed.

525 **Figure 5:** Same as Figure 3 but for wind components.

526 **Figure 6:** RMSEs for temperature, water vapor, and wind components at midnight of  
527 January using three DNNs. Left y-axis is for RMSEs of HAC and HPC; right y-axis is for  
528 RMSE of FFN. The RMSEs are calculated along the time series below the PBL height for  
529 January midnight at local time. The lower and upper end of the dash lines are RMSEs that  
530 consider the lowest and highest PBL heights as shown in Figure 2.



- 531 **Figure 7:** Same as Figure 6 but for Pearson correlations.
- 532 **Figure 8:** Terrain height (left) and vegetation types (right) for Logan, Kansas, and other  
533 locations that we used to assess the spatial transferability of our domain-aware DNNs.
- 534 **Figure 9:** Normalized RMSEs relative to their corresponding observations at midnight of  
535 January for temperature, water vapor mixing ratio, and wind component. The sites are in  
536 the order of short to long distance from the reference site at Logan, Kansas.
- 537 **Figure 10:** Same as Figure 9 but for correlations between DNN predictions and observations.



538 **Table 1: Inputs and outputs for the NN developed in this study. The variable names of these  
539 inputs and outputs in the WRF are shown in the parentheses.**

Input Variable	Output Variable
2-meter water vapor mixing ratio (Q2),	zonal wind (U)
2-meter air temperature (T2),	meridional wind (V)
10-meter zonal and meridional wind (U10, V10)	temperature (tk)
Ground heat flux (GRDFLX)	water vapor mixing ratio (QVAPOR)
Downward short wave flux (SWDOWN)	
Downward long wave flux (GLW)	
Latent heat flux (LH)	
Upward heat flux (HFX)	
Planetary boundary layer height (PBLH)	
Surface friction velocity (UST)	
Ground temp (TSK)	
Soil temperature at 2 m below ground (TSLB)	
Soil moisture for 0-0.3cm below ground (SMOIS)	
Geostrophic wind component at 700 hPa (Ug, Vg)	

540



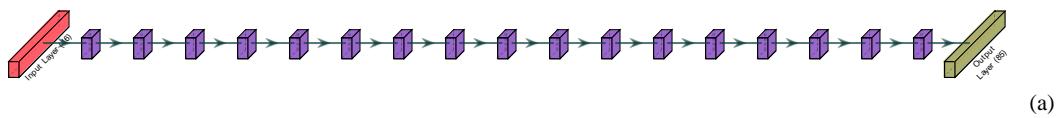
541 **Table 2: Training and prediction time (unit: seconds) for the three DNNs using different**  
542 **lengths of training data. The predicted period is for one year (2005).**

DNN Type	Training Data (years)	Training Time (s)	Number of Epochs	Training Time (s) per Epoch	Prediction Time (s) for 1 Year (2005)
FNN	1	85.969	61	1.409	0.197
FNN	2	137.359	47	2.923	0.196
FNN	6	376.209	70	5.374	0.171
FNN	12	199.468	23	8.673	0.193
FNN	20	306.665	27	11.358	0.199
HPC	1	199.152	178	1.119	0.336
HPC	2	454.225	91	4.991	0.343
HPC	6	1233.908	133	9.278	0.317
HPC	12	1225.880	88	13.930	0.302
HPC	20	1181.716	68	17.378	0.331
HAC	1	131.104	95	1.380	0.366
HAC	2	468.884	85	5.516	0.411
HAC	6	870.753	80	10.884	0.406
HAC	12	737.921	47	15.700	0.420
HAC	20	1351.898	69	19.593	0.381

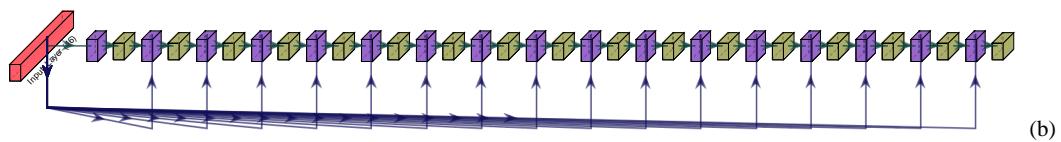
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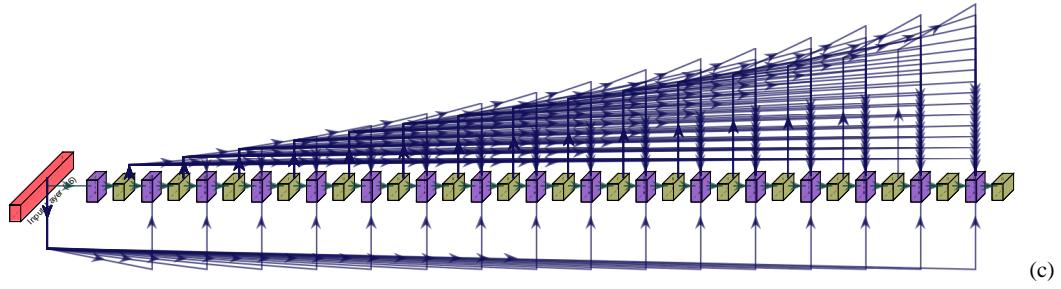
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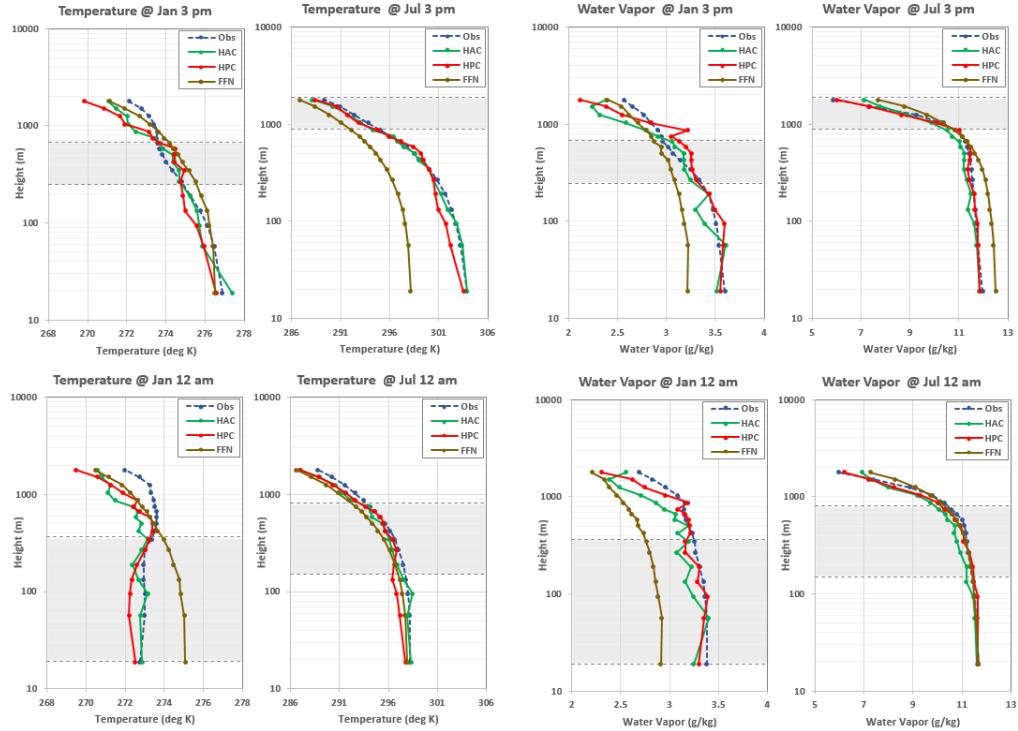
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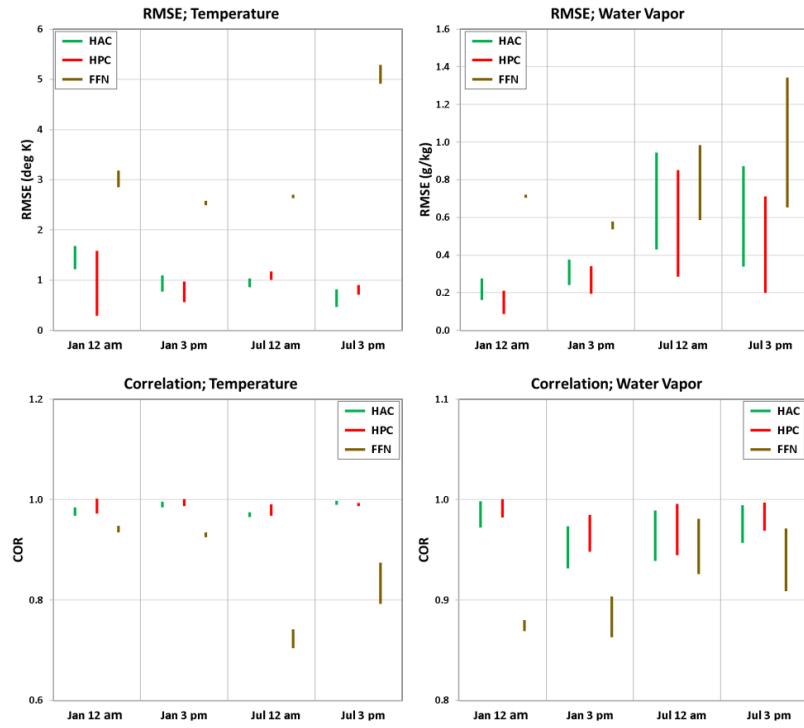


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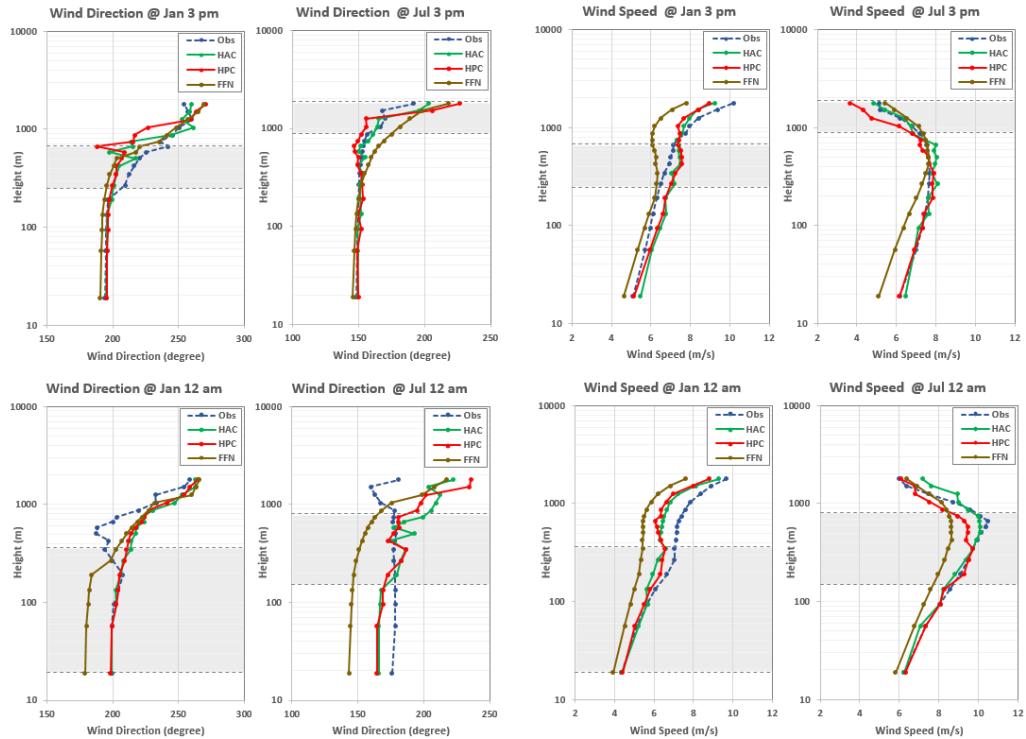
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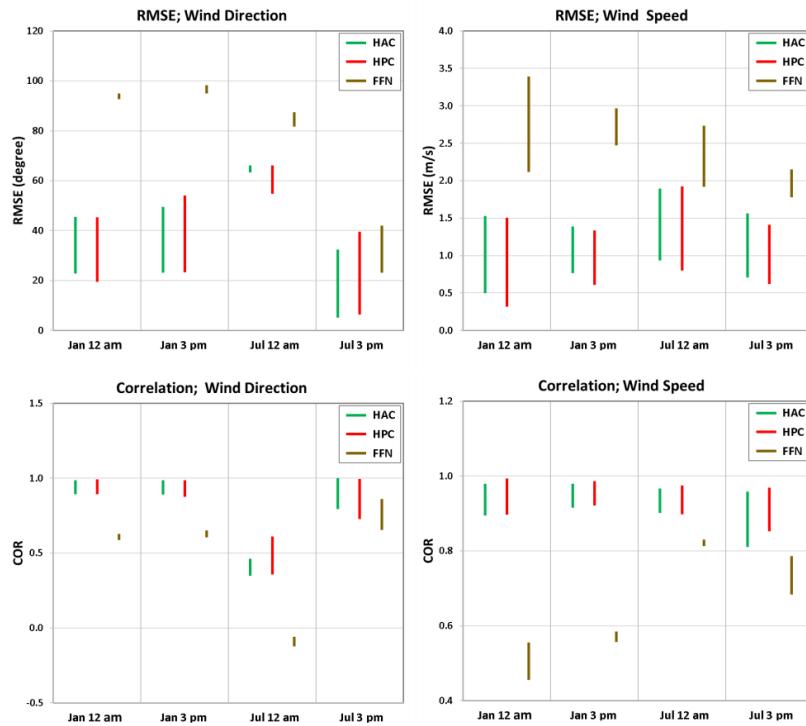
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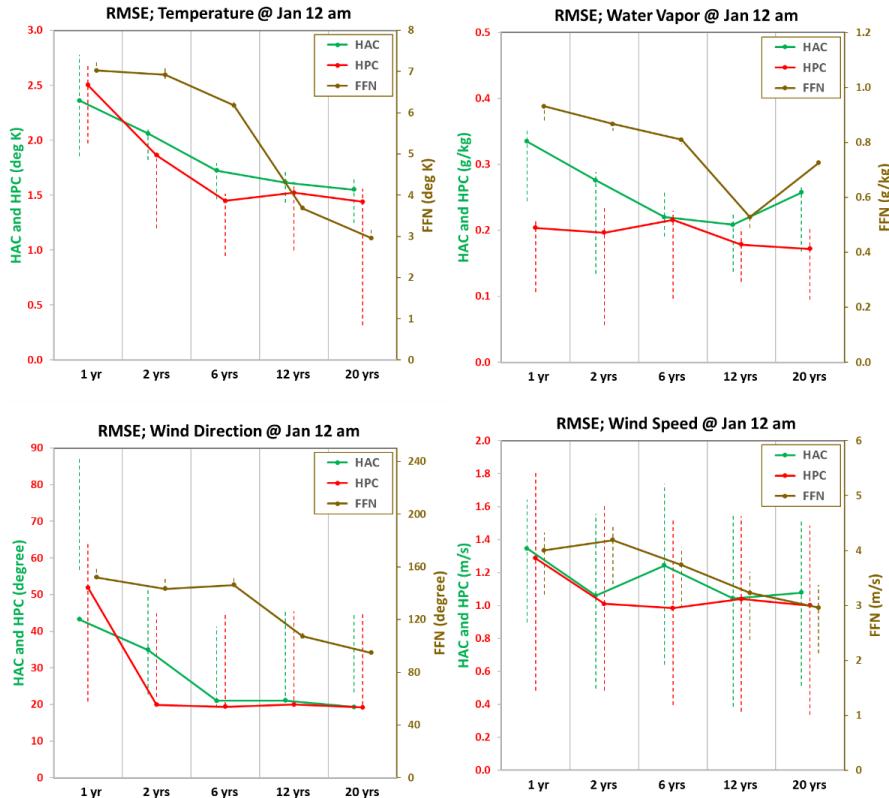
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565 **Figure 4: Same as Figure 2 but for wind direction and wind speed.**



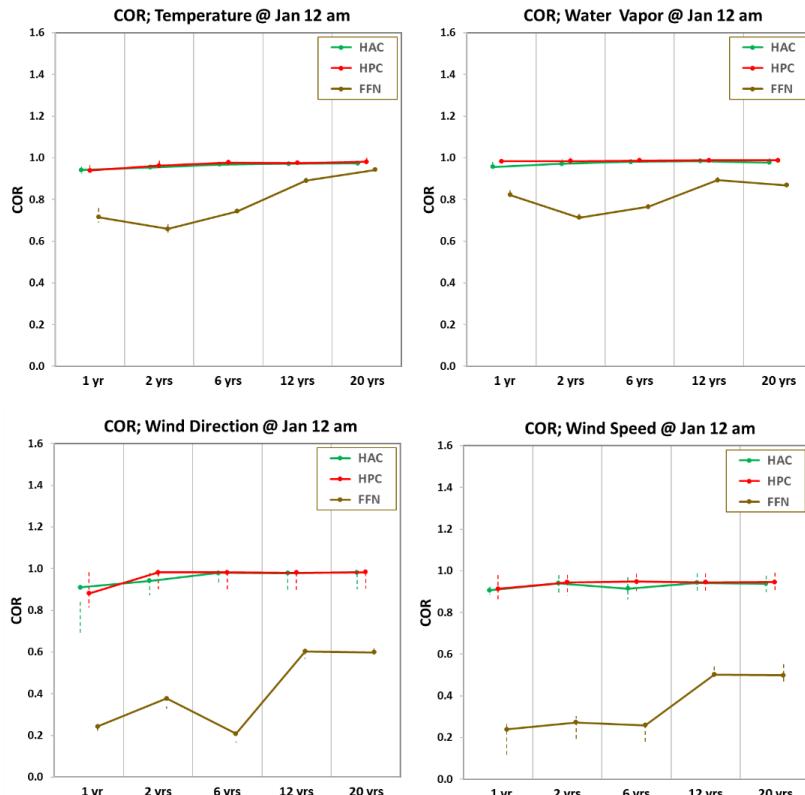
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568

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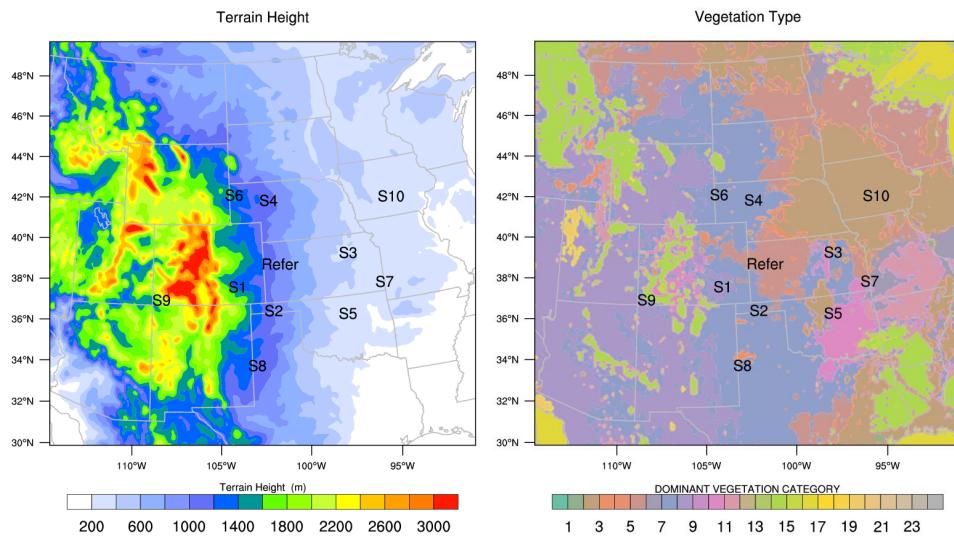


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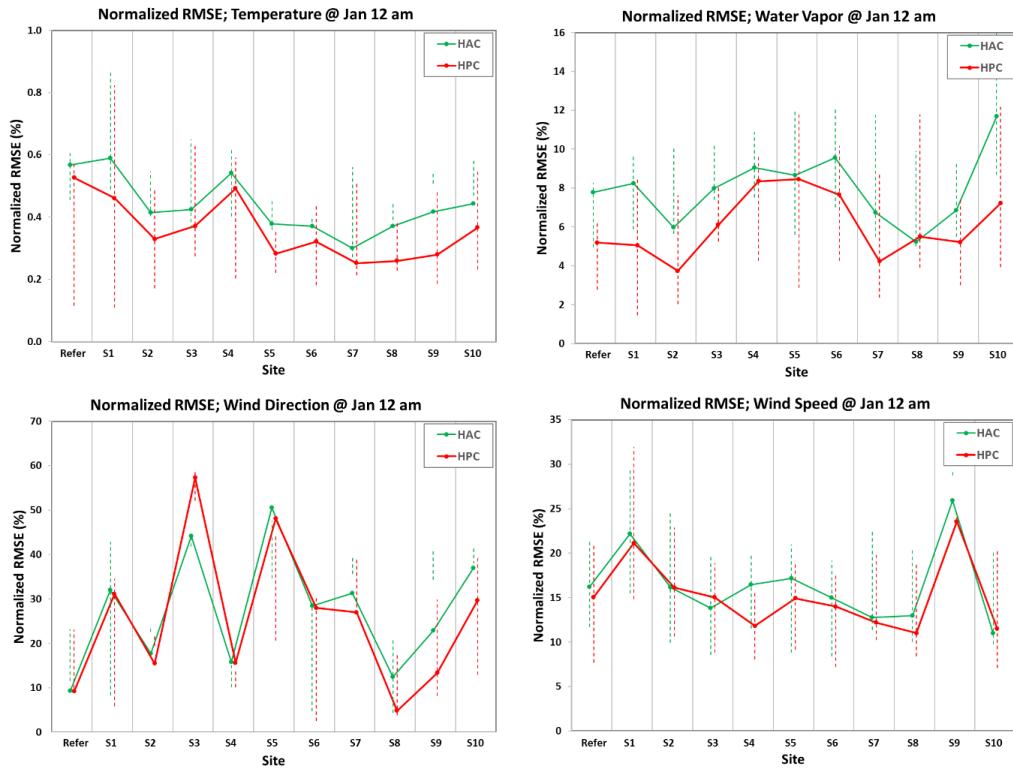
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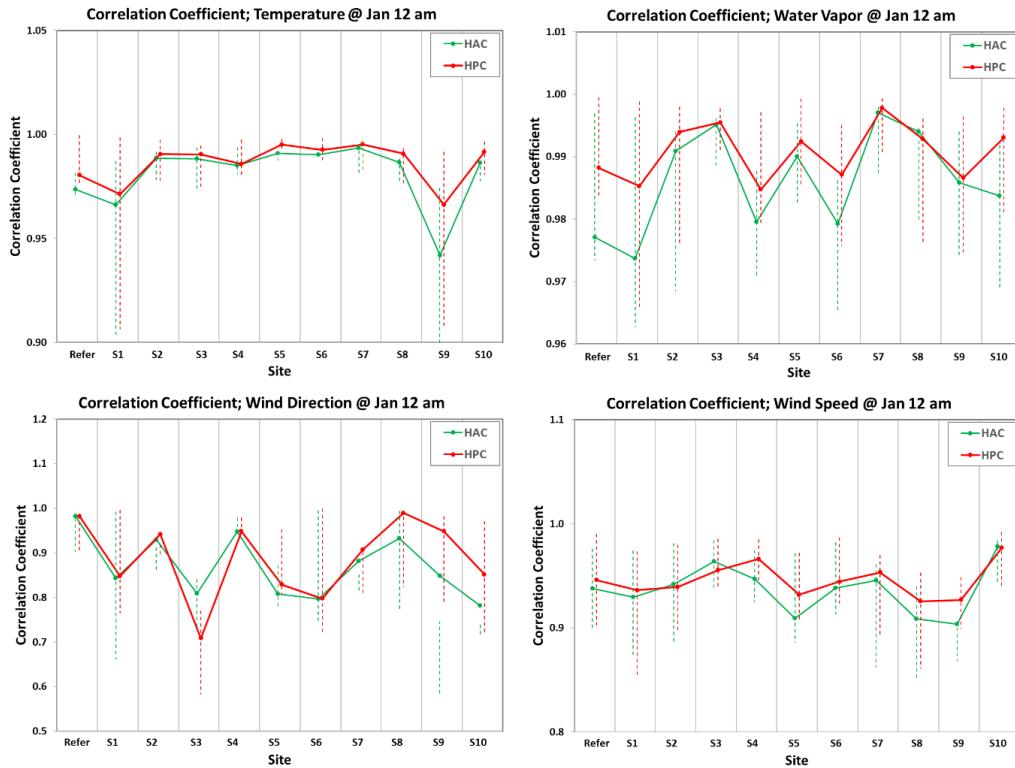


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